

## 1 Topics from Chapter 4

- Sections 4.1, 4.2, 4.5, 4.6
- Moment Generating Functions
- Sums of Independent Random Variables: Convolution
- Covariance and Correlation

## 2 Moment Generating Functions

- Grey box on page 219 and on page 210
- Moment Generating Function (MGF), defined for both PDF and for PMF on page 210.
- Example 4.1, 4.2, 4.3, 4.4, 4.5
- Computing the moments,  $E[X]$  or  $E[X^2], \dots, E[X^k]$  and the central moments, e.g.  $var[X] = E[X^2] - (E[X])^2$ , from the MGF, page 213.
- Example 4.6
- Inverting the MGF to get back the PMF (usually done by inspection): Example 4.7, 4.8
- Mixture of two distributions: Computing MGF of the Mixture: Example 4.9
- MGF of a sum of independent random variables, Page 217
- Examples 4.10, 4.11

## 3 Sums of Independent Random Variables: Convolution

- Discrete case, page 221
- Example 4.13, also see one of the HW7 problems.
- Continuous case, page 222
- Example 4.14, a few others done in class and in quizzes

## 4 Covariance and Correlation

- Covariance define: Grey box on page 238-239.
- Uncorrelated rvs have  $cov(X,Y) = 0$
- Independent rvs are always uncorrelated
- Correlation coefficient define: Grey box on page 238-239.
- Variance of a sum of random variables (when not independent): page 239
- Example 4.26

## 5 Least Squares Estimation

- Read pages 240-247.
- Least squares estimate of  $X$  given  $Y$  is given by  $E[X|Y]$ . Grey box on Page 243  
Read the book for the meaning of least squares estimate.
- Linear least squares: Grey boxes on Page 247.
  - $E[X|Y]$  is difficult to compute in many cases.
  - But often we are happy with a sub-optimal solution: the best **linear** least squares estimate, i.e. we say that  $\hat{X} = aY + b$  and find the value of  $a$  and  $b$  that minimizes the expected value of squared error between  $X$  and  $\hat{X}$
- Grey boxes on page 243 and 247.
- Properties of estimation error (Page 244, 245) will be discussed in Thursday's class.