

# Production Cost Model Fundamentals

Midwest ISO

# Outline

- What is a Production Cost Model?
- Basics of Security Constrained Economic Dispatch
- What is PROMOD?
- PowerBase Database
- PROMOD Input Files and Assumptions
- PROMOD Output
- Economic Benefits Calculation
- PROMOD GUI Demo

# What is a Production Cost Model?

# What is a Production Cost Model?

- Captures all the costs of operating a fleet of generators
  - Originally developed to manage fuel inventories and budget in the mid 1970's
- Developed into an hourly chronological security constrained unit commitment and economic dispatch simulation
  - Minimize costs while simultaneously adhering to a wide variety of operating constraints.
  - Calculate hourly production costs and location-specific market clearing prices.

# What Are the Advantages of Production Cost Models?

- Allows simulation of all the hours in a year, not just peak hour as in power flow models.
- Allows us to look at the net energy price effects through
  - LMP's and its components.
  - Production cost.
- Enables the simulation of the market on a forecast basis
- Allows us to look at all control areas simultaneously and evaluate the economic impacts of decisions.

# Disadvantages of Production Cost Models

- Require significant amounts of data
- Long processing times
- New concept for many Stakeholders
- Require significant benchmarking
- Time consuming model building process
  - Linked to power flow models
- Do not model reliability to the same extent as power flow

# Production Cost Model vs. Power Flow

## ■ Production Cost Model

- SCUC&ED:  
very detailed
- All hours
- DC Transmission
- Selected security  
constraints
- Market analysis/  
Transmission  
analysis/planning

## ■ Power Flow

- Hand dispatch (merit  
Order)
- One hour at a time
- AC and DC
- Large numbers of  
security constraints
- Basis for transmission  
reliability &  
operational planning

# Basics of Security Constrained Economic Dispatch

## What is covered in this section

- Understanding constrained dispatch
- Shift factor concept
- Shadow price of constraints
- LMP calculation and its components;

# Economic Dispatch Formulation

$$\text{Min} \sum_{i=1}^N C_i \cdot P_{gi}, \quad \text{Objective function – total cost}$$

*S.T.*

$$\sum_{i=1}^N P_{gi} - \sum_{j=1}^L P_{lj} - \text{Loss} = 0, \quad \text{System Balance}$$

$$\sum_1^N S_{ki} \cdot P_{gi} \leq T_k^{\max}, \quad k = 1, 2, \dots, K, \quad \text{Transmission Constraints}$$

$$P_{gi}^{\min} \leq P_{gi} \leq P_{gi}^{\max}, \quad i = 1, 2, \dots, N, \quad \text{Capacity Constraints}$$

Where  $S_{ki}$  is a shift factor of branch  $k$  to the generator  $i$ ,  
 $C_i$  is an incremental price of energy at the  
generator  $i$ .

# Economic Dispatch Solution

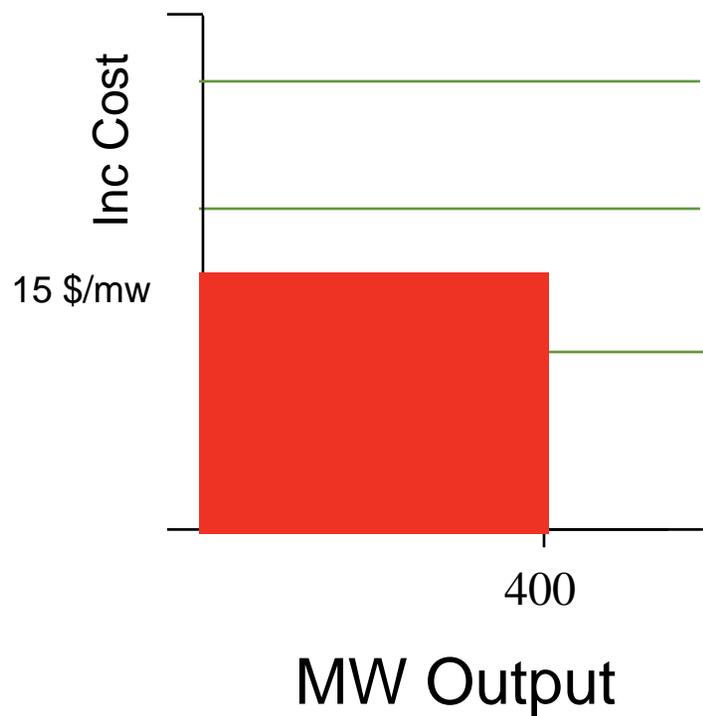
- Non-linear optimization problem
- Quick Solution Using Linear Programming (LP)
- Desired generation dispatch for every dispatchable generator.
- Shadow prices corresponding to each constraint.
- Binding constraints

# Shift Factor

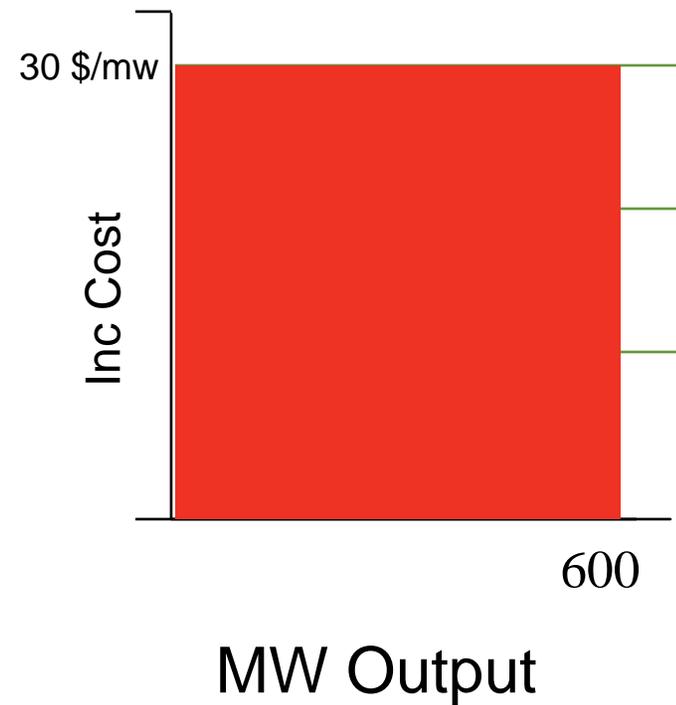
- Shift Factor (SF) shows how the flow in the branch will change if the injection at the bus changes by one (1) MW.
- All shift factors are computed relative to the reference bus, shift factor is dependent on the location of the reference bus.
- The shift factor at the reference bus equals to zero.
- Shift factors are solely dependent on the network topology and impedance.

# Five Bus System Example - Generation Cost

Incremental Cost Unit 1



Incremental Cost Unit 5



## Economic Dispatch (No Transmission)

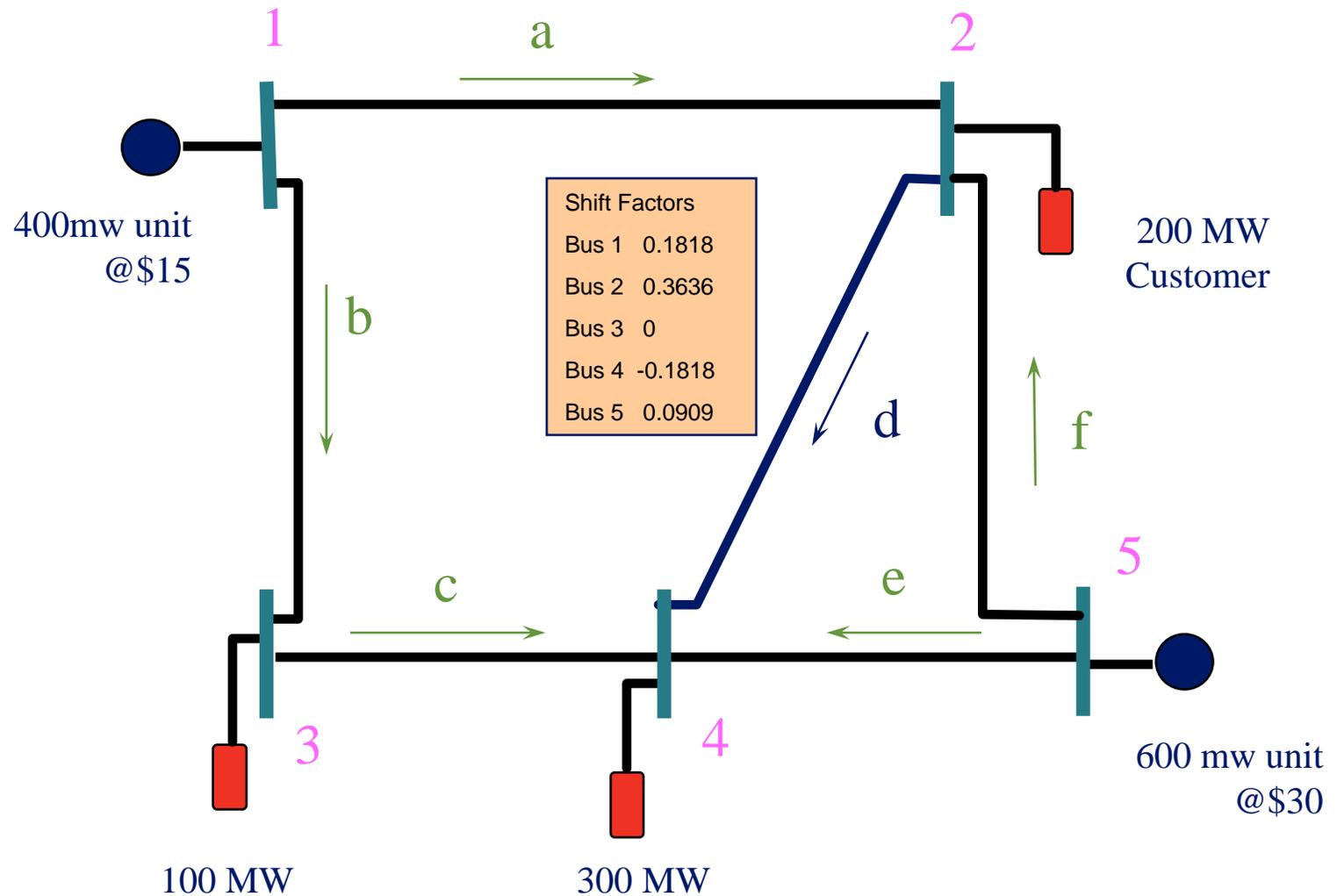
Load: 600 MW

$$G_1 = 400 \text{ MW}$$

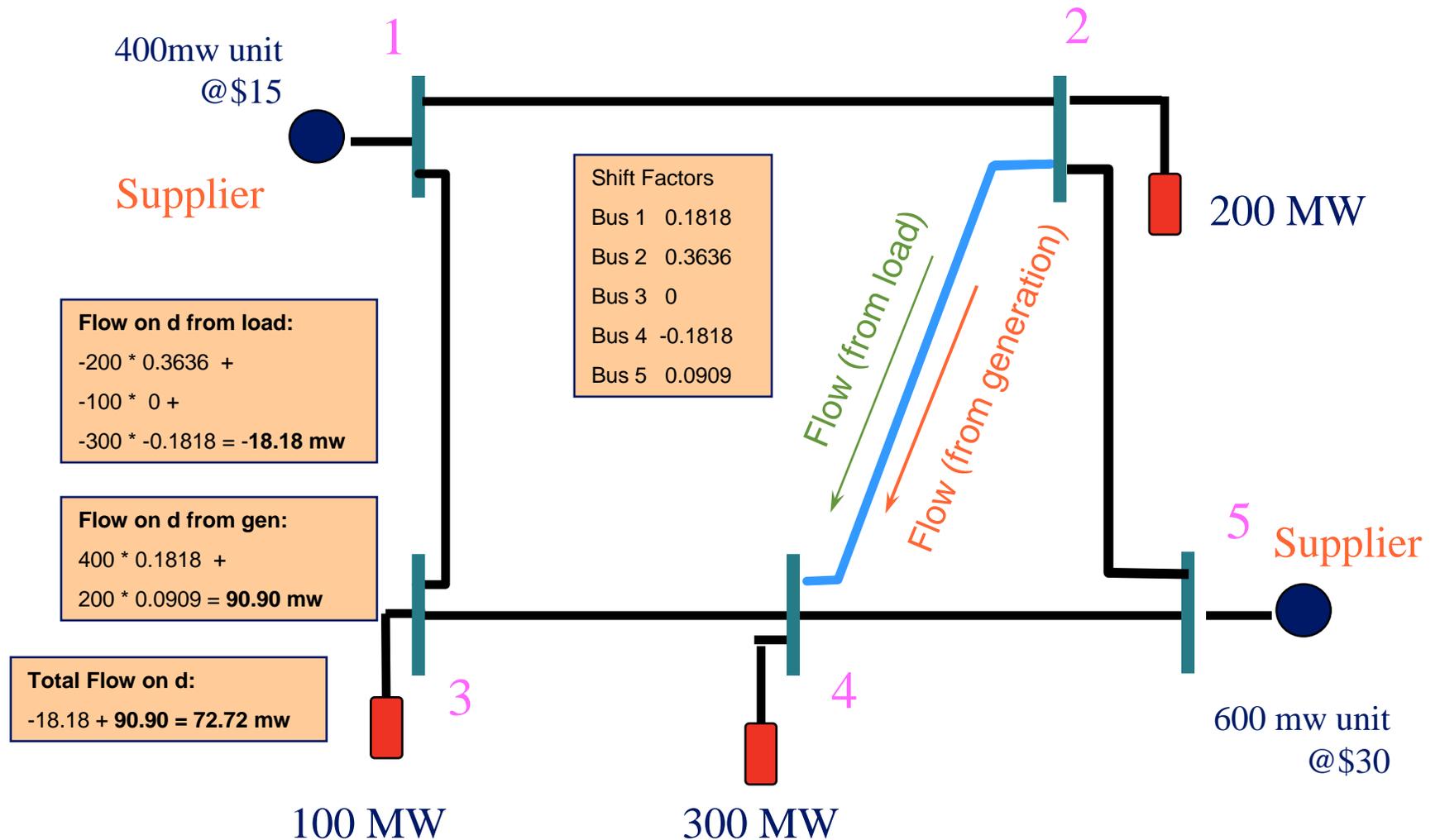
$$G_5 = 200 \text{ MW (Marginal)}$$

$$\text{Cost} = 400 \times \$15 + 200 \times \$30 = \$12,000$$

# 5 Bus Power Network



# 5 Bus Power Network



# Flow “d” Components

	Load Component	Shift Factors	
Flow on Line d	= -18.18	+ .1818 G <sub>1</sub>	+ .0909 G <sub>5</sub>
	= -18.18	+ .1818 400	+ .0909 200
	= -18.18	+ 72.73	+ 18.18
	= 72.73	Megawatts total flow	

# Transmission Constraint Applied

If  $d_{\max} = 50$  MW , the dispatch is *not acceptable!*

Flow:  $d = -18.18 + .1818 G_1 + .0909 G_5 = 50$

Load Balance:  $G_1 + G_5 = 600$

$$G_1 = 150$$

$$G_5 = 450$$

$$\text{Cost} = \$15,750$$



*Both Marginal !*

## Constraint Shadow Price

- What if the constraint were 51 mw?
- The *incremental increase* in cost is the shadow price

$$\text{Flow:} \quad d = -18.18 \quad +.1818 G_1 \quad + .0909 G_5 = 51$$

$$\text{Load Balance:} \quad G_1 + G_5 = 600$$

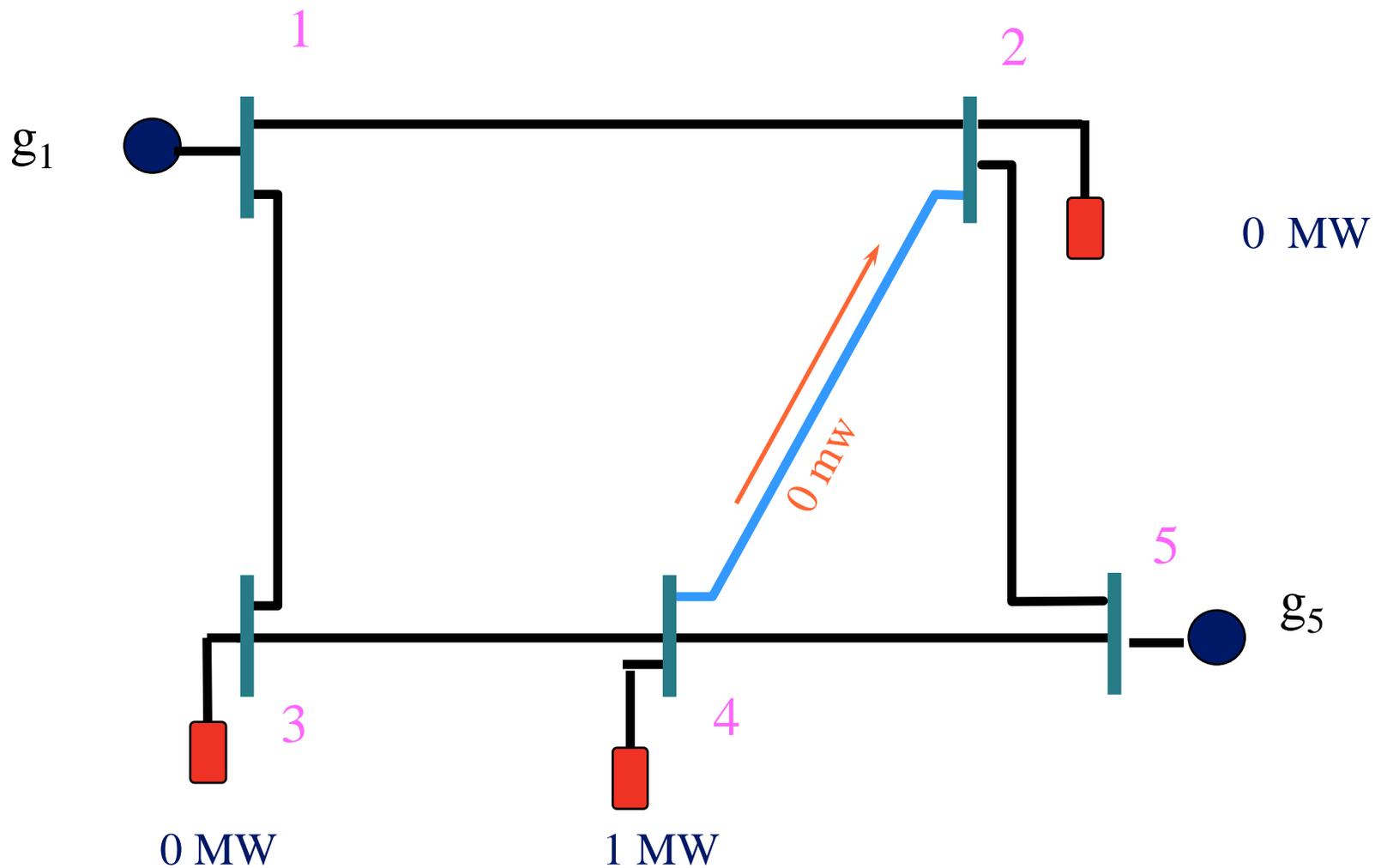
$$\text{Cost} = \$15,585 \quad G_1=161\text{MW}, \quad G_5=439\text{MW}$$

$$\text{Shadow price} = 15,585 - 15,750 = -165 \text{ \$/mw}$$

# Bus Locational Marginal Prices

- How much will the next mw *of load* cost?
  - Is it simply the marginal unit cost?
  
- LMP definition:
  - A change in the total cost of production due to increment of load at this location.
  
- Bus LMPs can be calculated by adding one MW of load at each bus and determining the corresponding change in the total production cost

# 5 Bus System Incremental Network



## The Incremental Flow Equation

- The change in generation must result in zero flow change
- Power changes at the marginal units, and at the load bus
- The sum of power change must be zero

Bus 4: Add 1 MW Load  
New flow equation...

$$.1818 g_1 + .0909 g_5 - .1818 (-1) = 0$$

## Incremental Equations

$$\text{Load Balance:} \quad g_1 \quad + \quad g_5 \quad = \quad 1$$

$$\text{Flow "d" :} \quad .1818 g_1 \quad + \quad .0909 g_5 \quad = \quad -.1818$$

$$\text{Solution:} \quad g_1 \quad = \quad -3$$

$$g_5 \quad = \quad +4 \quad (\text{wow !})$$

$$\text{Imp} = -3 \times \$15 + 4 \times \$30 = 75 \text{ \$/mw}$$

## Price at Bus 2

Bus 2: Add 1 MW Demand.  
New equations...

$$.1818 g_1 + .0909 g_5 + .3636 (-1) = 0$$

$$g_1 + g_5 = 1$$

Solution:  $g_1 = 3$

$$g_5 = -2$$

$$\text{Imp} = 3 \times 15 - 2 \times 30 = -15 \text{ \$/mw (!)}$$

## What about Bus 3 (slack bus)?

Bus 3: Add 1 MW Demand.  
New equations...

$$\begin{array}{rcl} .1818 g_1 + .0909 g_5 + .0000 (-1) & = & 0 \\ g_1 + g_5 & = & 1 \end{array}$$

Solution:  $g_1 = -1$

$g_5 = +2$

$Imp = (-1 * 15) + (2 * 30) = 45 \text{ \$/mw}$

## Buses 1 and 5?

- These are the “price setting buses”
- LMP at these buses will be the gen price
- $LMP_1 = \$15$
- $LMP_5 = \$30$

# LMP Calculation

- LMP at any location is calculated based on the shadow prices out of LP solution.
- The following fundamental formula is used to calculate LMPs. For any node  $i$ :

$$\lambda_i = \underbrace{\lambda}_{\text{Energy Component}} - \underbrace{LF_i \cdot \lambda}_{\text{Loss Component}} + \underbrace{\sum_{k=1}^K S_{ik} \cdot \mu_k}_{\text{Congestion Component}}$$

The diagram illustrates the decomposition of the LMP formula into three components. The first term,  $\lambda$ , is labeled as the Energy Component. The second term,  $LF_i \cdot \lambda$ , is labeled as the Loss Component. The third term,  $\sum_{k=1}^K S_{ik} \cdot \mu_k$ , is labeled as the Congestion Component.

where  $\lambda$  is a shadow price of the system balance constraint.

# 5 Bus System – LMP Calculation using Shadow Price

Bus	Shift Factor
1	0.1818
2	0.3636
3	0.0000
4	-0.1818
5	0.0909

-165	45
-30.000	15.000
-60.000	-15.000
0.000	45.000
30.000	75.000
-15.000	30.000

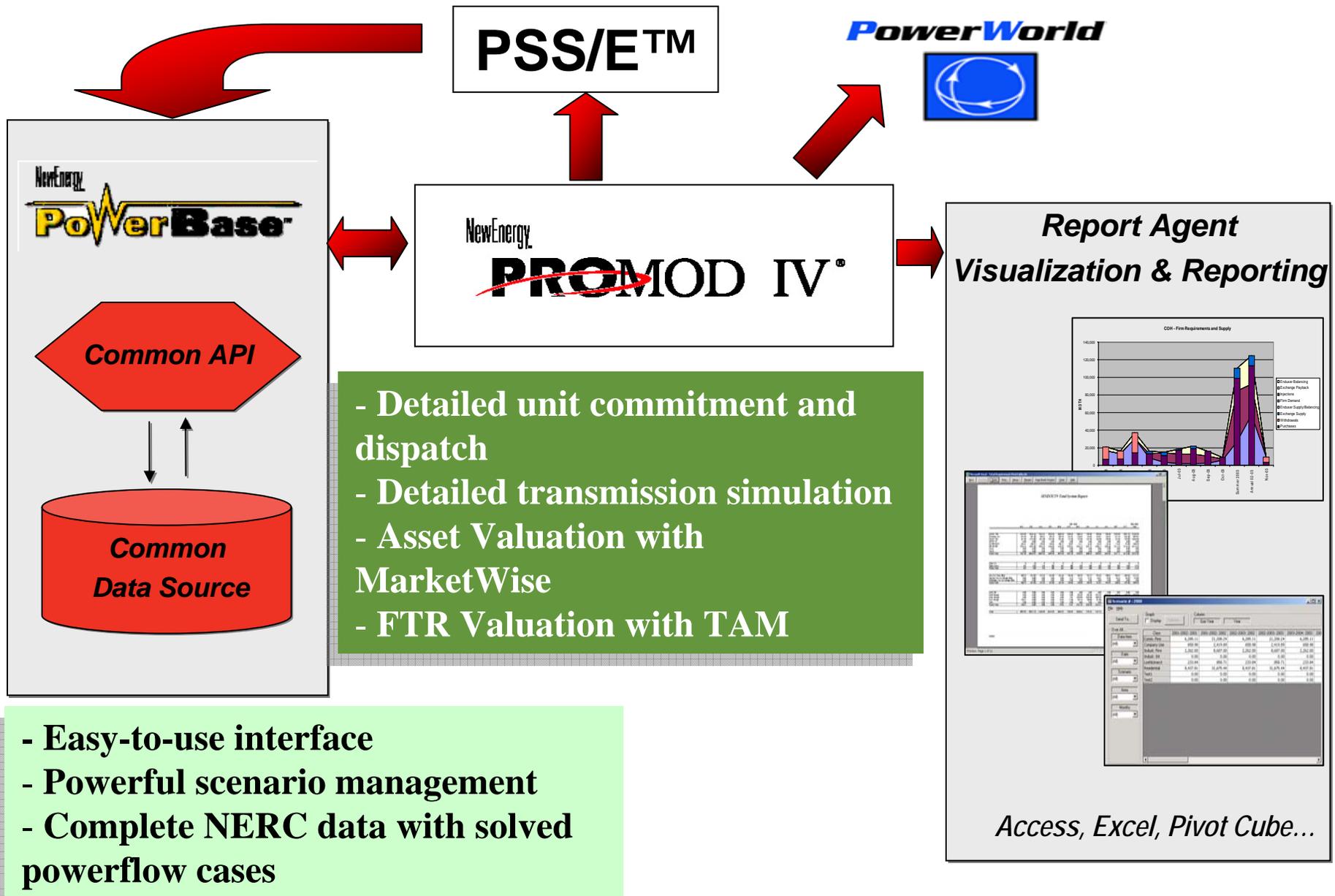
$$\lambda_i = \lambda - LF_i \cdot \lambda + \sum_{k=1}^K S_{ik} \cdot \mu_k,$$

# What is PROMOD

## Background

- PROMOD is a Production Cost Model developed by Ventyx (Formerly known as NewEnergy Associates, A Siemens Company).
- Detailed generator portfolio modeling, with both region zonal price and nodal LMP forecasting and transmission analysis including marginal losses

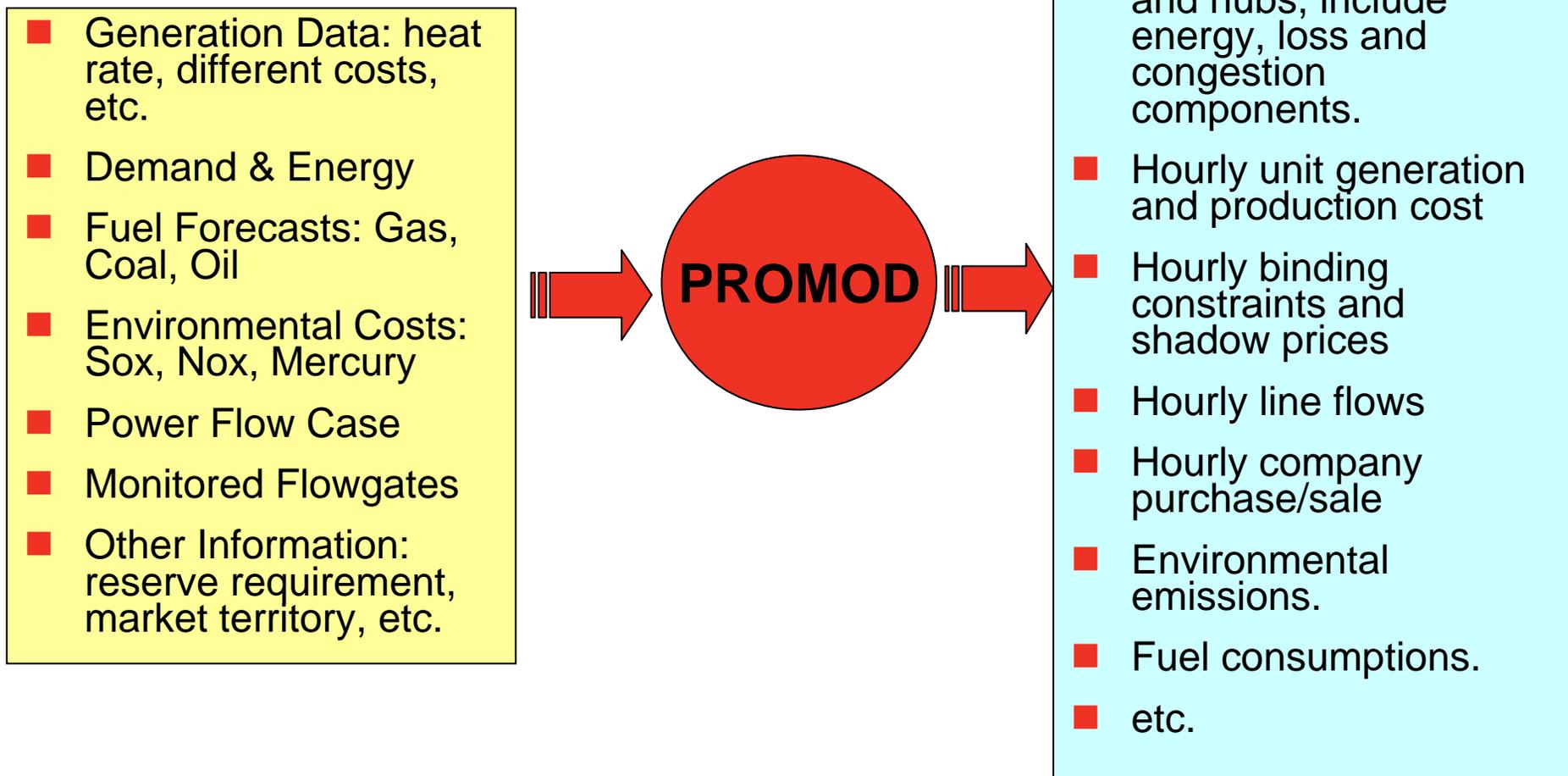
# How PROMOD Works - PROMOD Structure



- Detailed unit commitment and dispatch
- Detailed transmission simulation
- Asset Valuation with MarketWise
- FTR Valuation with TAM

- Easy-to-use interface
- Powerful scenario management
- Complete NERC data with solved powerflow cases

# How PROMOD Works – Input and Output of PROMOD



# Magnitude of the Challenge

## Real System Dimensions – MTEP 08 PROMOD Cases

- Footprint: East interconnection excluding FRCC
- Generators: ~ 4,700
- Buses: ~ 47,500
- Branches: ~ 60,000
- Monitored Lines: ~ 1,500
- Contingencies: ~ 500
- Run Time: 60-90 Hrs (for one year 8760 hours)

# Powerbase Database

# Data in PowerBase

- Generation
- Demand & Energy
- Transmission Network Data
- Fuel Forecasts
  - Coal, Uranium, Gas, Coal, Oil
- Environmental Effluent and Costs
  - CO<sub>2</sub>, Sox, Nox, Mercury

# PROMOD Input Files and Assumptions

# PROMOD input files

## ■ PFF file

- Main input file, includes units, fuels, environmental and transmission data, pool configuration, reserve requirement, run option switches, etc.

## ■ Load data file

- Hourly load profiles for each company for a selected study period.
- Based on the 8760 hour load shape and each year's peak load and annual energy for each company defined in PowerBase.

## ■ Gen Outage Library and automatic maintenance schedule

- Same outage library and maintenance schedule used by all cases

# PROMOD input files

## ■ Event files

- Define the monitored line/contingency pairs which are the transmission constraints
- Combine MISO and NERC Book of Flowgates
- Modify existing events or add new events according to member's comments.
- Create new events which have the potential of overflow using PAT tool

# PROMOD Assumptions

## ■ Study Footprint

- East interconnection excluding Florida
- Hourly fixed transactions modeled to include the influence of external areas to the study footprint
  - ❖ SETRANS sale to Florida

# PROMOD Assumptions (Cont')

## ■ Pool Definition

- a group of companies in which all its generators are dispatched together to meet its loads.
- Hurdle rates are defined between pools to allow the energy exchange between pools.
- Hurdle rates are based on the filed transmission through-and-out rates, plus a market inefficiency adder.
- In current MISO cases, 11 pools are defined: MISO, PJM, TVA, MRO, East Canada, SPP, IMO, MHEB, ISONE, NYISO, SERC

## PROMOD Assumptions (Cont')

### ■ Loss Calculation

- Option 1: Load is equal to actual load plus loss. Loss and LMP loss component are not calculated.
- Option 2: Load is equal to actual load plus loss. Loss is not calculated while LMP loss component is calculated using an approximation method – Single Pass Loss Calculation.
- Option 3: Load is equal to actual load. Loss and LMP loss component are calculated – Multi Pass Loss Calculation. Run time is 4 times of Option 2.

**Option 2 is used in MISO PROMOD cases.**

## PROMOD Assumptions (Cont')

- Wind Units – fixed load modifier transactions
  - Set at a same capacity factor for every hour (~ 33%);
  - Set different capacity factors for different months (15% for summer months, and 20% for winter months);
  - Set hourly profile for each unit to capture geographical diversity.
  
- Smelter Loads modeled as transactions

# PROMOD Output

## PROMOD Output

- LMPs (include the energy, loss and congestion components):
  - ❖ Hourly LMP of selected buses, defined hubs.
  - ❖ Hourly Load Weighted and Gen Weighted LMP of defined zones.
  
- Constraints:
  - ❖ Hourly shadow price;
  - ❖ Number of hours at  $P_{max}$ , total shadow price at  $P_{max}$ ;
  - ❖ Number of hours at  $P_{min}$ , total shadow price at  $P_{min}$ ;

## PROMOD Output (Cont')

### ■ Generators:

- ❖ Hourly generation
- ❖ Hourly production cost (sum of fuel, variable O&M, environmental cost)
- ❖ Hourly fuel consumption, BTU consumption
- ❖ Hours on line, hours of startup, hours at margin, Hours profitable.
- ❖ Monthly variable O&M cost, fuel cost, emission, and emission cost.

## PROMOD Output (Cont')

### ■ Fuel:

- ❖ Hourly fuel consumption.

### ■ Power Flow:

- ❖ Hourly flow for selected lines, interfaces, and DC lines.
- ❖ Monthly transmission losses (only for marginal loss calculation option)

### ■ Company:

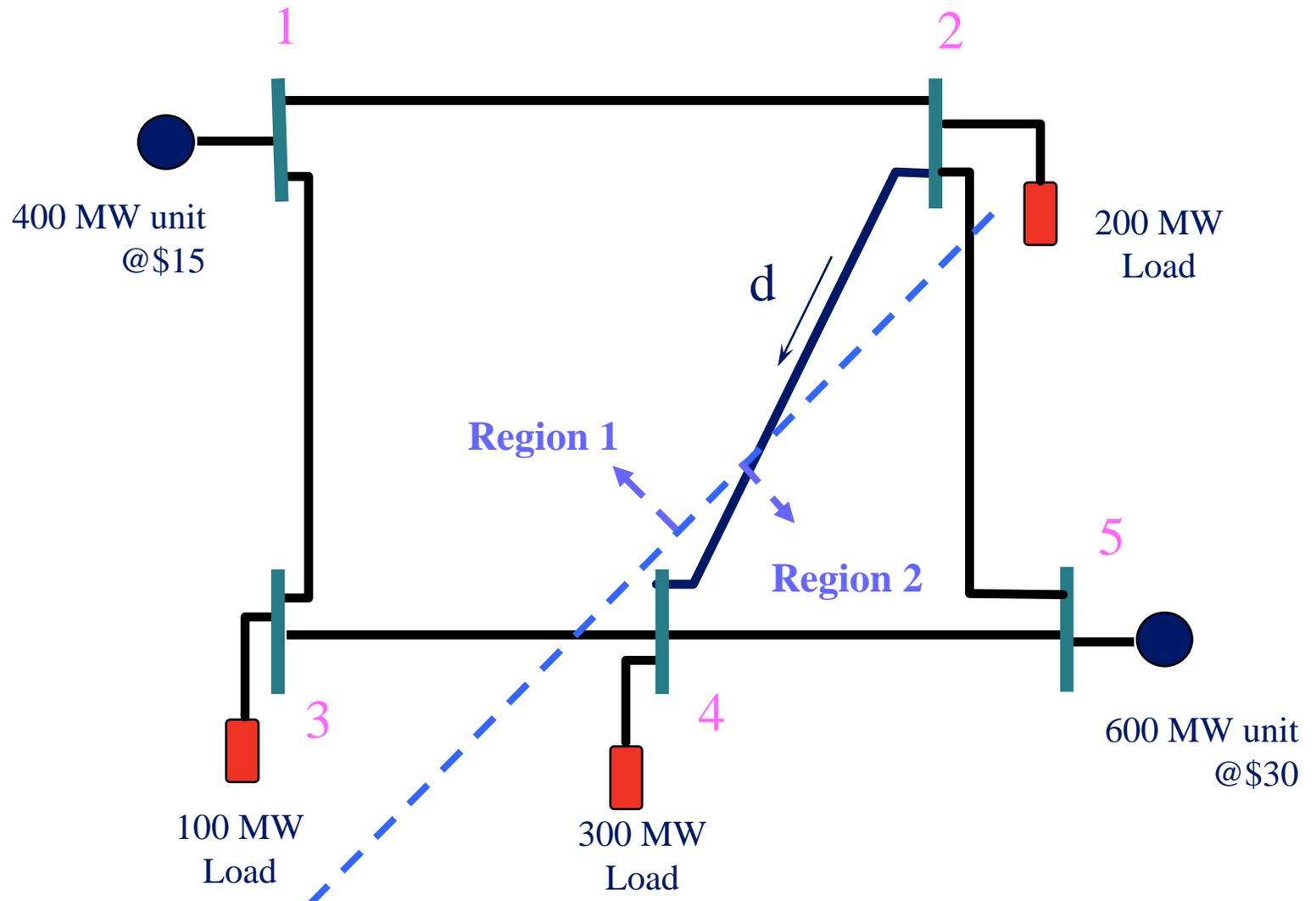
- ❖ Hourly purchase/sale.
- ❖ Hourly dump and emergency energy.

# Economic Benefits Calculation

# Economic Benefit

- To capture the economic benefit of transmission upgrade: run two PROMOD cases, one with transmission upgrade, one without. For each case, calculate (for each region):
  - $\text{Load Cost} = \text{Load LMP} * \text{Load}$
  - $\text{Adjusted Production Cost} = \text{Production Cost} + \text{Import} * \text{Load Weighted LMP (or)} - \text{Export} * \text{Gen Weighted LMP}$
- Economic Benefit:
  - Load Cost Saving: Load Cost difference between two cases;
  - Adjusted Production Cost Saving: Adjusted Production Cost difference between two cases
  - RECB II Benefit = sum over all regions ( $30\% * \text{Load Cost Saving} + 70\% * \text{Adjusted Production Cost Saving}$ )

# Example: 5 Bus Power Network



# 5 Bus Power Network (Original) – PROMOD result

Gen: 150 MW  
LMP: 15\$/MWH  
Prod. Cost: 2,250\$

Load: 200 MW  
LMP: -15\$/MWH  
Load Cost: -3,000\$

## Region 1:

Import: 150 MWH  
Load Weighted LMP =  
 $(-3,000 + 4,500) / (100 + 200)$   
= 5\$/MWH  
Load Cost = -3,000 + 4,500  
= 1,500\$  
Adjusted Production Cost =  
 $2,250$ + 150\text{MWH} * 5\$/\text{MWH}$   
= 3,000\$

Line is binding

50 MW

## Region 2:

Export: 150 MWH  
Gen Weighted LMP  
= 30\$/MWH  
Load Cost = 22,500\$  
Adjusted Production  
Cost = 13,500\$  
- 150MWH \* 30\$/MWH  
= 9,000\$

Load: 100 MW  
LMP: 45\$/MWH  
Load Cost: 4,500\$

Load: 300 MW  
LMP: 75\$/MWH  
Load Cost: 22,500\$

Gen: 450 MW  
LMP: 30\$/MWH  
Prod. Cost: 13,500\$

# 5 Bus Power Network (After upgrade) – PROMOD result

Gen: 400 MW  
LMP: 30\$/MWH  
Prod. Cost: 6,000\$

Load: 200 MW  
LMP: 30\$/MWH  
Load Cost: 6,000\$

## Region 1:

Export: 100 MWH  
Gen Weighted LMP =  
=30\$/MWH  
Load Cost = 6,000 + 3,000  
= 9,000\$  
Adjusted Production Cost =  
6,000\$ - 100MWH \* 30\$/MWH  
= 3,000\$

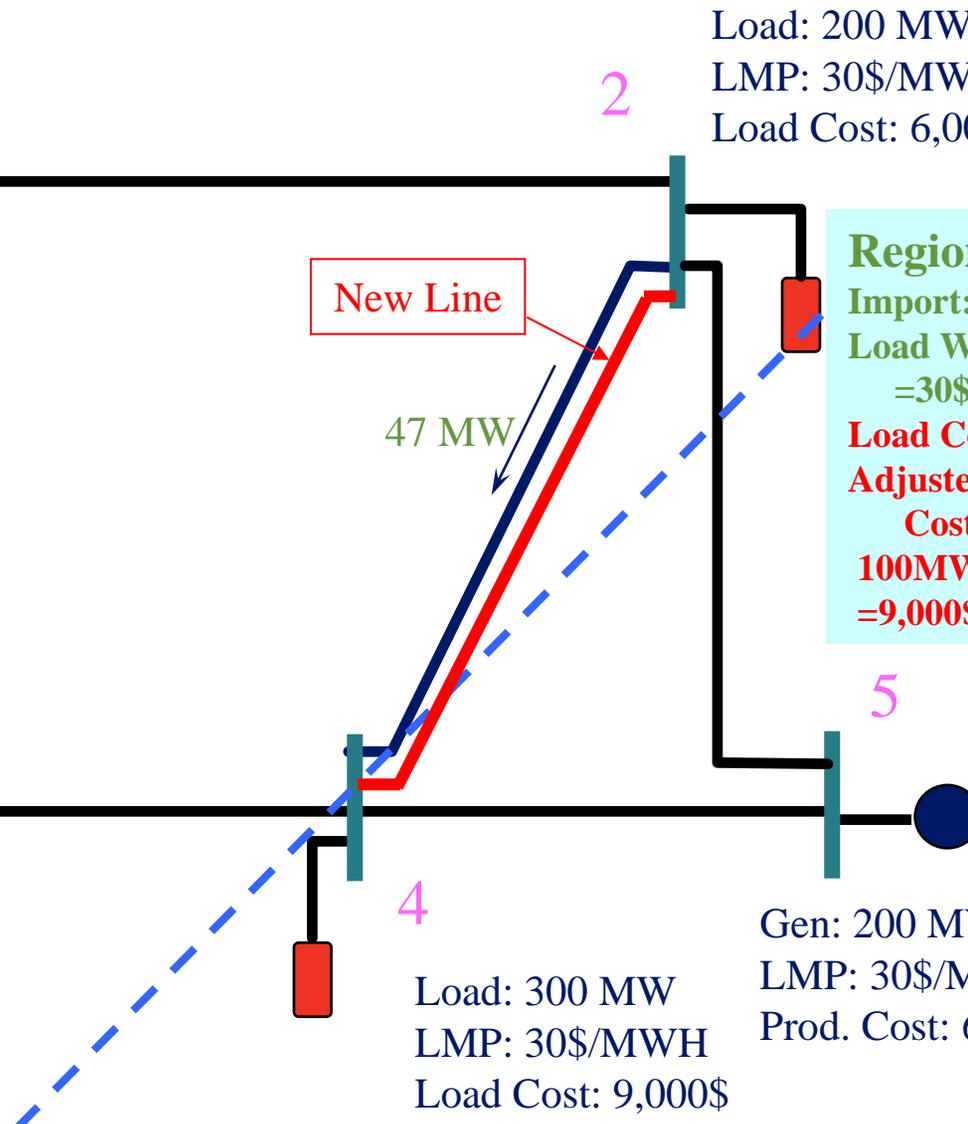
## Region 2:

Import: 100 MWH  
Load Weighted LMP  
=30\$/MWH  
Load Cost = 9,000\$  
Adjusted Production  
Cost = 6,000\$ +  
100MWH \* 30\$/MWH  
= 9,000\$

Load: 100 MW  
LMP: 30\$/MWH  
Load Cost: 3,000\$

Load: 300 MW  
LMP: 30\$/MWH  
Load Cost: 9,000\$

Gen: 200 MW  
LMP: 30\$/MWH  
Prod. Cost: 6,000\$



# 5 Bus Power Network – New Transmission RECB II Benefit

		Original Case	Case with New Line	Saving
Region 1	Load Cost	\$1,500	\$9,000	-\$7,500
	Adjusted Production Cost	\$3,000	\$3,000	\$0
Region 2	Load Cost	\$22,500	\$9,000	\$13,500
	Adjusted Production Cost	\$9,000	\$9,000	\$0

**RECB II Benefit = 70% \* 0 + 30% \* (-7,500+13,500) = \$1,800**