

1. Suppose that $X \sim U(0, \theta)$, a uniform distribution over $(0, \theta)$. Note that $\log p(x; \theta)$ is differentiable for all $\theta > x$ and we can define $\partial \log p(x; \theta) / \partial \theta$. (Here, $\log(\cdot)$ denotes natural logarithm.) Show that, however,

(a)

$$\mathbb{E}_{p(x; \theta)} \left[\frac{\partial \log p(X; \theta)}{\partial \theta} \right] = -\frac{1}{\theta} \neq 0$$

(b)

$$\text{var}_{p(x; \theta)} \left(\frac{\partial \log p(X; \theta)}{\partial \theta} \right) = 0$$

and the information bound is infinite.

Yet, show that $2X$ is an unbiased estimator of θ and has finite variance.

2. Problem 3.2 in Kay-I.
3. Problem 3.3 in Kay-I.
4. Problem 3.12 in Kay-I.
5. Problem 3.15 in Kay-I.