EE 303, Quiz 6, Spring 2017, Dr. McCalley; Name:_

Time: 20 minutes, closed book, closed notes

1. (32 pts) A transmission line having R=0.005 pu and X=0.05 pu (charging capacitance is negligible) is operating so that the voltage magnitudes and angles at its terminals are given by the data below:

Voltage Magnitude	Voltage Angle	Voltage Magnitude	Voltage Angle
for p-bus	for p-bus	for q-bus	for q-bus
(pu)	(deg)	(pu)	(deg)
1.15	10	0.95	0

All per unit values are given on a 100 MVA base. A relation that may be helpful to you is this:

$$P_{pq} = V_p^2 G - V_p V_q G \cos(\varphi_p - \varphi_q) + V_p V_q B \sin(\varphi_p - \varphi_q)$$

Compute:

(a) (22 pts) the real power flowing into and out of the line, in MW;

Solution:

$$P_{pq} = V_p^2 G - V_p V_q G \cos(\varphi_p - \varphi_q) + V_p V_q B \sin(\varphi_p - \varphi_q)$$

= 1.15²(1.98) - (1.15)(0.95)(1.98) cos(10°) + (1.15)(0.95)(19.80) sin(10°) = 4.2445

So real power into line = 100(4.245) = 424.5 MW

$$P'_{pq} = -P_{qp} = -\left[V_q^2 G - V_q V_p G \cos\left(\varphi_q - \varphi_p\right) + V_q V_p B \sin\left(\varphi_q - \varphi_p\right)\right]$$

$$= -[.95^{2}(1.98) - (0.95)(1.15)(1.98)\cos(-10^{\circ}) + (1.15)(0.95)(19.8)\sin(-10^{\circ})] = 4.0996$$

So real power out of the line = 100(4.0996) = 409.96 MW

(b) (10 pts) the real power absorbed by the transmission line impedance.

Solution:

$$P_{loss} = P_{pq} - P'_{pq} = 424.5 - 409.96 = 14.49 \text{ MW}$$

- 2. (36 pts) Short answers on transmission lines:
 - (a) If a transmission line is bundled so that it requires a total of 12 conductors, how many conductors per phase are being used?

Solution: 4

(b) Which is larger for a transmission circuit: capacitance between the phases or capacitance between phases and ground?

Solution: Capacitance between the phases.

(c) What is the range for the ratio X_L/R for a typical conductor?

Solution: About 10. I would accept any number or range between 2 and 20.

(d) If a transmission line has impedance of Z = R + jX = 2 + j5, is it true that $G=Re\{Y\}=1/R=0.5$?

Solution: No, it is not true.

 $G=Re\{Y\}=Re\{1/Z\}=Re\{1/(2+j5)\}=Re\{0.69-j0.1724]=0.69$

- 3. (32 pts) True/false on the power flow problem.
 - a. In the power flow problem, the engineer inputs the flows on all of the circuits, and MW and MVAR generation and load values are computed for all buses in the network.
 - b. A generator capability curve, which specifies a boundary for operating a synchronous generator in terms of MW and MVAR output, is approximated within a power flow program as a rectangular region specified by Q_{max} , Q_{min} , and P_{max} for each generator.
 - ____c. A bus "k" with load but no generator would satisfy: $P_{inj,k} < 0$.
 - ____d. All buses with loads only are type "PV."

Solutions:

- a. F
- b. T
- c. T
- d. F