

CprE 2810: Digital Logic

Instructor: Alexander Stoytchev

<http://www.ece.iastate.edu/~alexs/classes/>

The Intersection Between Hardware and Software

CprE 2810: Digital Logic
Iowa State University, Ames, IA
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Administrative Stuff

- The FINAL exam is scheduled for
- **Wednesday** Dec 18 @ 2:15 – 4:15 PM

Final Exam Format

- **The exam will cover: Chapter 1 to Chapter 6, and Sections 7.1-7.2, register machines, and i281 CPU**
- **Emphasis will be on Chapter 5, 6, and 7**
- **The exam will be closed book but open notes.**
- **You can bring up to 5 pages of handwritten or typed notes.**

Final Exam Format

- The exam will be out of 135 points
- You need 95 points to get an A on this exam
- It will be great if you can score more than 100 points.
 - but you can't roll over your extra points ☹️

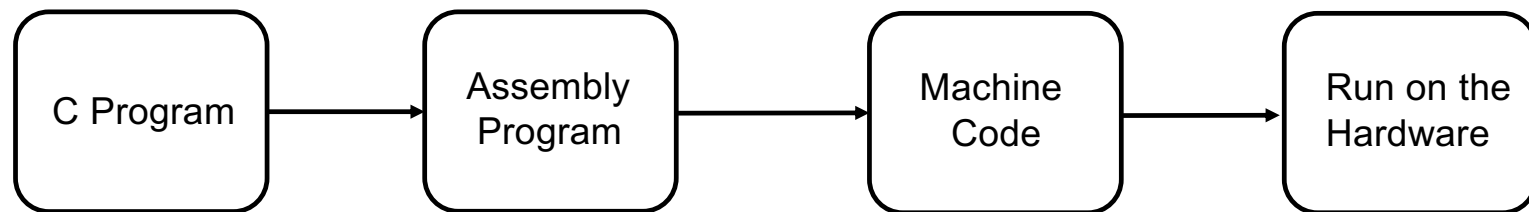
Topics for the Final Exam

- **K-maps for 2, 3, and 4 variables**
- **Multiplexers (circuits and function)**
- **Synthesis of logic functions using multiplexers**
- **Shannon's Expansion Theorem**
- **1's complement and 2's complement representation**
- **Addition and subtraction of binary numbers**
- **Circuits for adding and subtracting**
- **Serial adder**
- **Latches (circuits, behavior, timing diagrams)**
- **Flip-Flops (circuits, behavior, timing diagrams)**
- **Counters (up, down, synchronous, asynchronous)**
- **Registers and Register Files**

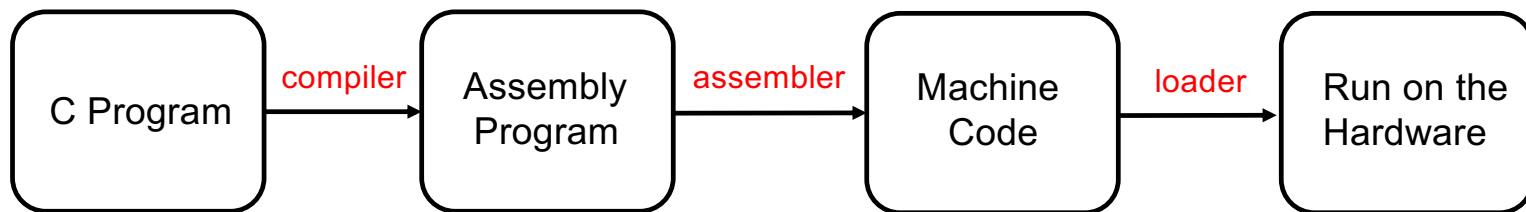
Topics for the Final Exam

- **Synchronous Sequential Circuits**
- **FSMs**
- **Moore Machines**
- **Mealy Machines**
- **State diagrams, state tables, state-assigned tables**
- **State minimization**
- **Designing a counter**
- **Arbiter Circuits**
- **Reverse engineering a circuit**
- **ASM Charts**
- **Register Machines and programs for them**
- **ALU, PC, and control for a simple processor (i281 CPU)**
- **Assembly and machine language (i281 assembly)**
- **Something from Star Wars**

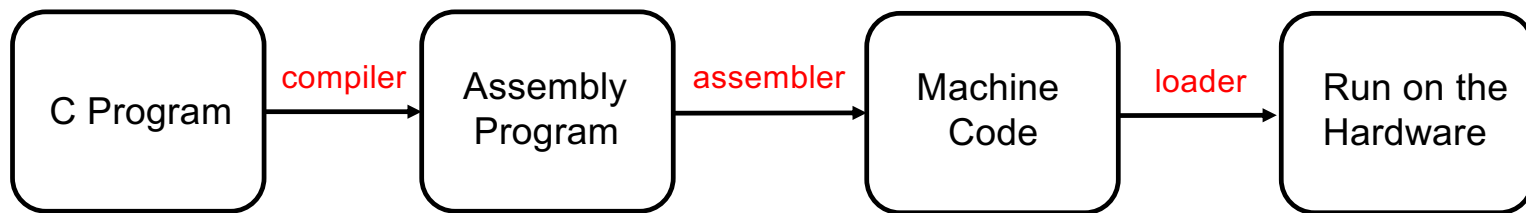
Writing and Running a Program



Writing and Running a Program

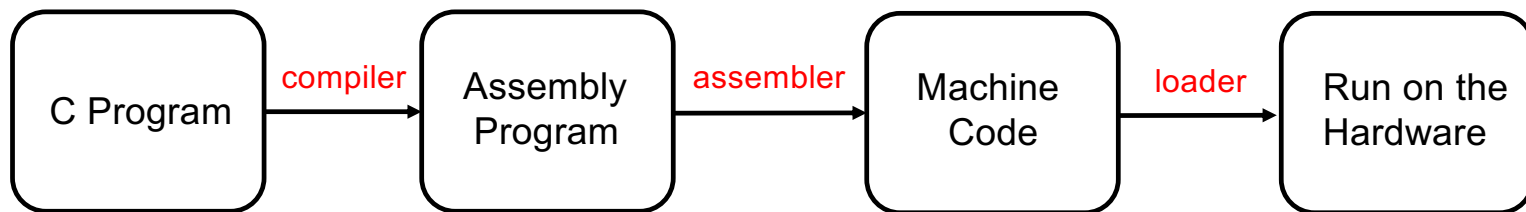


Writing and Running a Program



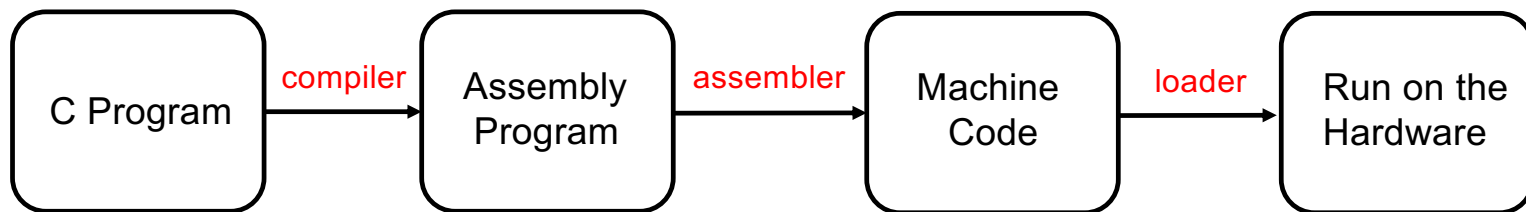
The programmer only writes this in a text editor.

Writing and Running a Program



Nerds skip the first step and start here.

Writing and Running a Program



CPU designers
start here.

i281 Example:
Add the numbers from 1 to 5

**i281 Example:
Add the numbers from 1 to 5**

C Language v.s. Assembly Language

C Version

```
// C Version
//
// Add the numbers from 1 to 5 using a for loop.

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++)
        sum+=i;

    // printf("%d\n", sum);
}
```

i281 Assembly Version

```
.data
N      BYTE    5
i      BYTE    ?
sum    BYTE    ?

.code

        LOADI  B, 0      ; sum=0
        LOADI  A, 1      ; i=1
        LOAD   D, [N]    ; register_D=N
Loop:   CMP    A, D      ; i<=N ?
        BRG   End       ; exit if i>N
Add:    ADD   B, A      ; sum+=i
        ADDI  A, 1      ; i++
        JUMP  Loop      ; next iteration
End:    STORE  [sum], B  ; update the memory for sum

; Register allocation:
; A: i
; B: sum
; C: <not used>
; D: N
```


i281 Assembly Version

```
.data
N      BYTE    5
i      BYTE    ?
sum    BYTE    ?

.code

        LOADI  B, 0      ; sum=0
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Add:    ADD    B, A      ; sum+=i
        ADDI   A, 1      ; i++
        JUMP   Loop     ; next iteration
End:    STORE  [sum], B  ; update the memory for sum

; Register allocation:
; A: i
; B: sum
; C: <not used>
; D: N
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
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Add:    ADD     B, A        ; sum+=i
        ADDI   A, 1        ; i++
        JUMP   Loop        ; next iteration
End:    STORE   [sum], B    ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N          BYTE    5
i          BYTE    ?
sum        BYTE    ?

.code

        LOADI   B, 0        ; sum=0
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// using a for loop

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    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI   A, 1        ; i=1
        LOAD    D, [N]      ; register_D=N
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Add the numbers from 1 to 5

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// using a for loop

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    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI   A, 1        ; i=1
        LOAD    D, [N]      ; register_D=N
Loop:   CMP     A, D        ; i<=N ?
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// using a for loop

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    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N      BYTE    5
i      BYTE    ?
sum    BYTE    ?

.code

        LOADI  B, 0      ; sum=0
        LOADI  A, 1      ; i=1
        LOAD   D, [N]    ; register_D=N
Loop:   CMP    A, D      ; i<=N ?
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Add:    ADD    B, A      ; sum+=i
        ADDI  A, 1      ; i++
        JUMP  Loop      ; next iteration
End:    STORE [sum], B  ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

`i=1`

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI  A, 1        ; i=1
        LOAD    D, [N]     ; register_D=N
Loop:   CMP     A, D        ; i<=N ?
        BRG     End        ; exit if i>N
Add:    ADD     B, A        ; sum+=i
        ADDI   A, 1        ; i++
        JUMP   Loop        ; next iteration
End:    STORE  [sum], B    ; write B to sum
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Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

This has no analog in the C version,
which is written in a high-level language.

```
; Assembly Version

.data
N      BYTE    5
i      BYTE    ?
sum    BYTE    ?

.code

        LOADI  B, 0      ; sum=0
        LOADI  A, 1      ; i=1
        LOAD   D, [N]    ; register_D=N
Loop:   CMP    A, D      ; i<=N ?
        BRG    End      ; exit if i>N
Add:    ADD    B, A      ; sum+=i
        ADDI   A, 1      ; i++
        JUMP   Loop     ; next iteration
End:    STORE  [sum], B  ; write B to sum
```

Load the value of N into register D.

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N      BYTE    5
i      BYTE    ?
sum    BYTE    ?

.code

        LOADI   B, 0      ; sum=0
        LOADI   A, 1      ; i=1
        LOAD    D, [N]    ; register_D=N
Loop:   CMP     A, D      ; i<=N ?
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Add:    ADD    B, A      ; sum+=i
        ADDI   A, 1      ; i++
        JUMP   Loop      ; next iteration
End:    STORE  [sum], B  ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI   A, 1        ; i=1
        LOAD    D, [N]      ; register_D=N
Loop:   CMP     A, D        ; i<=N ?
        BRG     End        ; exit if i>N
Add:    ADD     B, A        ; sum+=i
        ADDI   A, 1        ; i++
        JUMP   Loop        ; next iteration
End:    STORE  [sum], B    ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI   A, 1        ; i=1
        LOAD    D, [N]      ; register_D=N
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        ADDI   A, 1        ; i++
        JUMP   Loop        ; next iteration
End:    STORE   [sum], B    ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI   A, 1        ; i=1
        LOAD    D, [N]      ; register_D=N
Loop:   CMP     A, D        ; i<=N ?
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Add:    ADD     B, A        ; sum+=i
        ADDI   A, 1        ; i++
        JUMP   Loop        ; next iteration
End:    STORE   [sum], B    ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

i=2

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI   A, 1        ; i=1
        LOAD    D, [N]      ; register_D=N
Loop:   CMP     A, D        ; i<=N ?
        BRG     End        ; exit if i>N
Add:    ADD     B, A        ; sum+=i
        ADDI   A, 1        ; i++
        JUMP   Loop        ; next iteration
End:    STORE   [sum], B    ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI   A, 1        ; i=1
        LOAD    D, [N]      ; register_D=N
Loop:   CMP     A, D        ; i<=N ?
        BRG     End        ; exit if i>N
Add:    ADD     B, A        ; sum+=i
        ADDI   A, 1        ; i++
        JUMP   Loop        ; next iteration
End:    STORE   [sum], B    ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI   A, 1        ; i=1
        LOAD    D, [N]      ; register_D=N
Loop:   CMP     A, D        ; i<=N ?
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Add:    ADD     B, A        ; sum+=i
        ADDI   A, 1        ; i++
        JUMP   Loop        ; next iteration
End:    STORE  [sum], B    ; write B to sum
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Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N      BYTE    5
i      BYTE    ?
sum    BYTE    ?

.code

        LOADI  B, 0      ; sum=0
        LOADI  A, 1      ; i=1
        LOAD   D, [N]    ; register_D=N
Loop:   CMP    A, D      ; i<=N ?
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Add:    ADD   B, A      ; sum+=i
        ADDI  A, 1      ; i++
        JUMP  Loop     ; next iteration
End:    STORE [sum], B  ; write B to sum
```


Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

i=3

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI   A, 1        ; i=1
        LOAD    D, [N]      ; register_D=N
Loop:   CMP     A, D        ; i<=N ?
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Add:    ADD     B, A        ; sum+=i
        ADDI   A, 1        ; i++
        JUMP   Loop        ; next iteration
End:    STORE  [sum], B    ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
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}
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```
; Assembly Version

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N        BYTE    5
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Add:    ADD     B, A        ; sum+=i
        ADDI   A, 1        ; i++
        JUMP   Loop        ; next iteration
End:    STORE   [sum], B    ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
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    int N=5;
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```
; Assembly Version

.data
N      BYTE    5
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        LOADI   B, 0      ; sum=0
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Add the numbers from 1 to 5

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.data
N        BYTE    5
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```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

i=4

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI   A, 1        ; i=1
        LOAD    D, [N]      ; register_D=N
Loop:   CMP     A, D        ; i<=N ?
        BRG     End        ; exit if i>N
Add:    ADD     B, A        ; sum+=i
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        JUMP   Loop        ; next iteration
End:    STORE   [sum], B    ; write B to sum
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Add the numbers from 1 to 5

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        JUMP   Loop     ; next iteration
End:    STORE  [sum], B  ; write B to sum
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Add the numbers from 1 to 5

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// using a for loop

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```
; Assembly Version

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N        BYTE    5
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// using a for loop

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```
; Assembly Version

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        BRG     End        ; exit if i>N
Add:    ADD     B, A        ; sum+=i
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Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

i=5

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI   A, 1        ; i=1
        LOAD    D, [N]      ; register_D=N
Loop:   CMP     A, D        ; i<=N ?
        BRG     End        ; exit if i>N
Add:    ADD    B, A        ; sum+=i
        ADDI   A, 1        ; i++
        JUMP   Loop        ; next iteration
End:    STORE  [sum], B    ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N      BYTE    5
i      BYTE    ?
sum    BYTE    ?

.code

        LOADI   B, 0      ; sum=0
        LOADI   A, 1      ; i=1
        LOAD    D, [N]    ; register_D=N
Loop:   CMP     A, D      ; i<=N ?
        BRG     End      ; exit if i>N
Add:    ADD     B, A      ; sum+=i
        ADDI   A, 1      ; i++
        JUMP   Loop     ; next iteration
End:    STORE  [sum], B  ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI   A, 1        ; i=1
        LOAD    D, [N]      ; register_D=N
Loop:   CMP     A, D        ; i<=N ?
        BRG     End        ; exit if i>N
Add:    ADD     B, A        ; sum+=i
        ADDI   A, 1        ; i++
        JUMP   Loop        ; next iteration
End:    STORE   [sum], B    ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N      BYTE    5
i      BYTE    ?
sum    BYTE    ?

.code

        LOADI   B, 0      ; sum=0
        LOADI   A, 1      ; i=1
        LOAD    D, [N]    ; register_D=N
Loop:   CMP     A, D      ; i<=N ?
        BRG     End      ; exit if i>N
Add:    ADD     B, A      ; sum+=i
        ADDI   A, 1      ; i++
        JUMP   Loop     ; next iteration
End:    STORE   [sum], B  ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

i=6

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI   A, 1        ; i=1
        LOAD    D, [N]      ; register_D=N
Loop:   CMP     A, D        ; i<=N ?
        BRG     End        ; exit if i>N
Add:    ADD     B, A        ; sum+=i
        ADDI   A, 1        ; i++
        JUMP   Loop        ; next iteration
End:    STORE   [sum], B    ; write B to sum
```

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

.data
N        BYTE    5
i        BYTE    ?
sum      BYTE    ?

.code

        LOADI   B, 0        ; sum=0
        LOADI   A, 1        ; i=1
        LOAD    D, [N]      ; register_D=N
Loop:   CMP     A, D        ; i<=N ?
        BRG     End        ; exit if i>N
Add:    ADD     B, A        ; sum+=i
        ADDI   A, 1        ; i++
        JUMP   Loop        ; next iteration
End:    STORE  [sum], B   ; write B to sum
```

**i281 Example:
Add the numbers from 1 to 5**

Assembly Language v.s. Machine Language

i281 Assembly Code

.data

```
N      BYTE    5
i      BYTE    ?
sum    BYTE    ?
```

.code

```
      LOADI   B, 0      ; sum=0
      LOADI   A, 1      ; i=1
      LOAD    D, [N]    ; register_D=N
Loop:  CMP     A, D      ; i<=N ?
      BRG     End      ; exit if i>N
Add:   ADD    B, A      ; sum+=i
      ADDI   A, 1      ; i++
      JUMP   Loop      ; next iteration
End:   STORE  [sum], B  ; update the memory for sum
```


i281 Assembly Code

```
.data
N      BYTE    5
i      BYTE    ?
sum    BYTE    ?

.code
      LOADI   B, 0
      LOADI   A, 1
      LOAD    D, [N]
Loop:  CMP     A, D
      BRG     End
Add:   ADD     B, A
      ADDI   A, 1
      JUMP   Loop
End:   STORE  [sum], B
```

Mapping Assembly to Machine Code

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011010000000000
	LOADI	A, 1	0011000000000001
	LOAD	D, [N]	1000110000000000
Loop:	CMP	A, D	1101001100000000
	BRG	End	1111001000000011
Add:	ADD	B, A	0100010000000000
	ADDI	A, 1	0101000000000001
	JUMP	Loop	1110000011111011
End:	STORE	[sum], B	1010010000000010

Assembly Language

Machine Language

Mapping Assembly to Machine Code

```
.data
N      BYTE    5
i      BYTE    ?
sum    BYTE    ?

.code
      LOADI   B, 0
      LOADI   A, 1
      LOAD    D, [N]
Loop:  CMP     A, D
      BRG     End
Add:   ADD    B, A
      ADDI   A, 1
      JUMP   Loop
End:   STORE  [sum], B
```

Assembly Language

Data Memory:

```
0000 0101
0000 0000
0000 0000
```

Code Memory:

```
0011 0100 0000 0000
0011 0000 0000 0001
1000 1100 0000 0000
1101 0011 0000 0000
1111 0010 0000 0011
0100 0100 0000 0000
0101 0000 0000 0001
1110 0000 1111 1011
1010 0100 0000 0010
```

Machine Language
in Binary

Mapping Assembly to Machine Code

.data

N **BYTE** **5**
i **BYTE** **?**
sum **BYTE** **?**

Data Memory:

0 **5**
0 **0**
0 **0**

.code

LOADI **B, 0**
 LOADI **A, 1**
 LOAD **D, [N]**
Loop: **CMP** **A, D**
 BRG **End**
Add: **ADD** **B, A**
 ADDI **A, 1**
 JUMP **Loop**
End: **STORE** **[sum], B**

Code Memory:

3 **4** **0** **0**
3 **0** **0** **1**
8 **C** **0** **0**
D **3** **0** **0**
F **2** **0** **3**
4 **4** **0** **0**
5 **0** **0** **1**
E **0** **F** **B**
A **4** **0** **2**

Assembly Language

Machine Language
in Binary

Mapping Assembly to Machine Code

.data			Data Memory:
N	BYTE	5	05
i	BYTE	?	00
sum	BYTE	?	00
.code			Code Memory:
	LOADI	B, 0	34 00
	LOADI	A, 1	30 01
	LOAD	D, [N]	8C 00
Loop:	CMP	A, D	D3 00
	BRG	End	F2 03
Add:	ADD	B, A	44 00
	ADDI	A, 1	50 01
	JUMP	Loop	E0 FB
End:	STORE	[sum], B	A4 02

Assembly Language

Machine Language
in Hexadecimal

i281 Example:
Add the numbers from 1 to 5

Bit Mapping for OPCODEs

Mapping Assembly to Machine Code

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011010000000000
	LOADI	A, 1	0011000000000001
	LOAD	D, [N]	1000110000000000
Loop:	CMP	A, D	1101001100000000
	BRG	End	1111001000000011
Add:	ADD	B, A	0100010000000000
	ADDI	A, 1	0101000000000001
	JUMP	Loop	1110000011111011
End:	STORE	[sum], B	1010010000000010

Assembly Language

Machine Language

Mapping Assembly to Machine Code

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	00110100_00000000
	LOADI	A, 1	00110000_00000001
	LOAD	D, [N]	10001100_00000000
Loop:	CMP	A, D	11010011_00000000
	BRG	End	11110010_00000011
Add:	ADD	B, A	01000100_00000000
	ADDI	A, 1	01010000_00000001
	JUMP	Loop	11100000_11111011
End:	STORE	[sum], B	10100100_00000010

Assembly Language

Machine Language

Mapping Assembly to Machine Code

```
.data
N      BYTE    5
i      BYTE    ?
sum    BYTE    ?

.code
      LOADI   B, 0
      LOADI   A, 1
      LOAD    D, [N]
Loop:  CMP     A, D
      BRG     End
Add:   ADD    B, A
      ADDI   A, 1
      JUMP   Loop
End:   STORE  [sum], B
```

Assembly Language

Data Memory:

```
00000101
00000000
00000000
```

Code Memory:

```
0011_01_00_00000000
0011_00_00_00000001
1000_11_00_00000000
1101_00_11_00000000
1111_00_10_00000011
0100_01_00_00000000
0101_00_00_00000001
1110_00_00_11111011
1010_01_00_00000010
```

Machine Language

Mapping Assembly to Machine Code

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010

Mapping Assembly to Machine Code

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010

Mapping Assembly to Machine Code

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010

Mapping Assembly to Machine Code

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010

OPCODE Mapping

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010

OPCODE Mapping

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010

Register Parameter Mapping

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010

Register Parameter Mapping

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010

Second Register Parameter Mapping

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010

Second Register Parameter Mapping

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010

Value / Address / Offset Mapping

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010

Value / Address / Offset Mapping

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010

“Don’t care” bits ...

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_dd_00000000
	LOADI	A, 1	0011_00_dd_00000001
	LOAD	D, [N]	1000_11_dd_00000000
Loop:	CMP	A, D	1101_00_11_dddddddd
	BRG	End	1111_dd_10_00000011
Add:	ADD	B, A	0100_01_00_dddddddd
	ADDI	A, 1	0101_00_dd_00000001
	JUMP	Loop	1110_dd_dd_11111011
End:	STORE	[sum], B	1010_01_dd_00000010

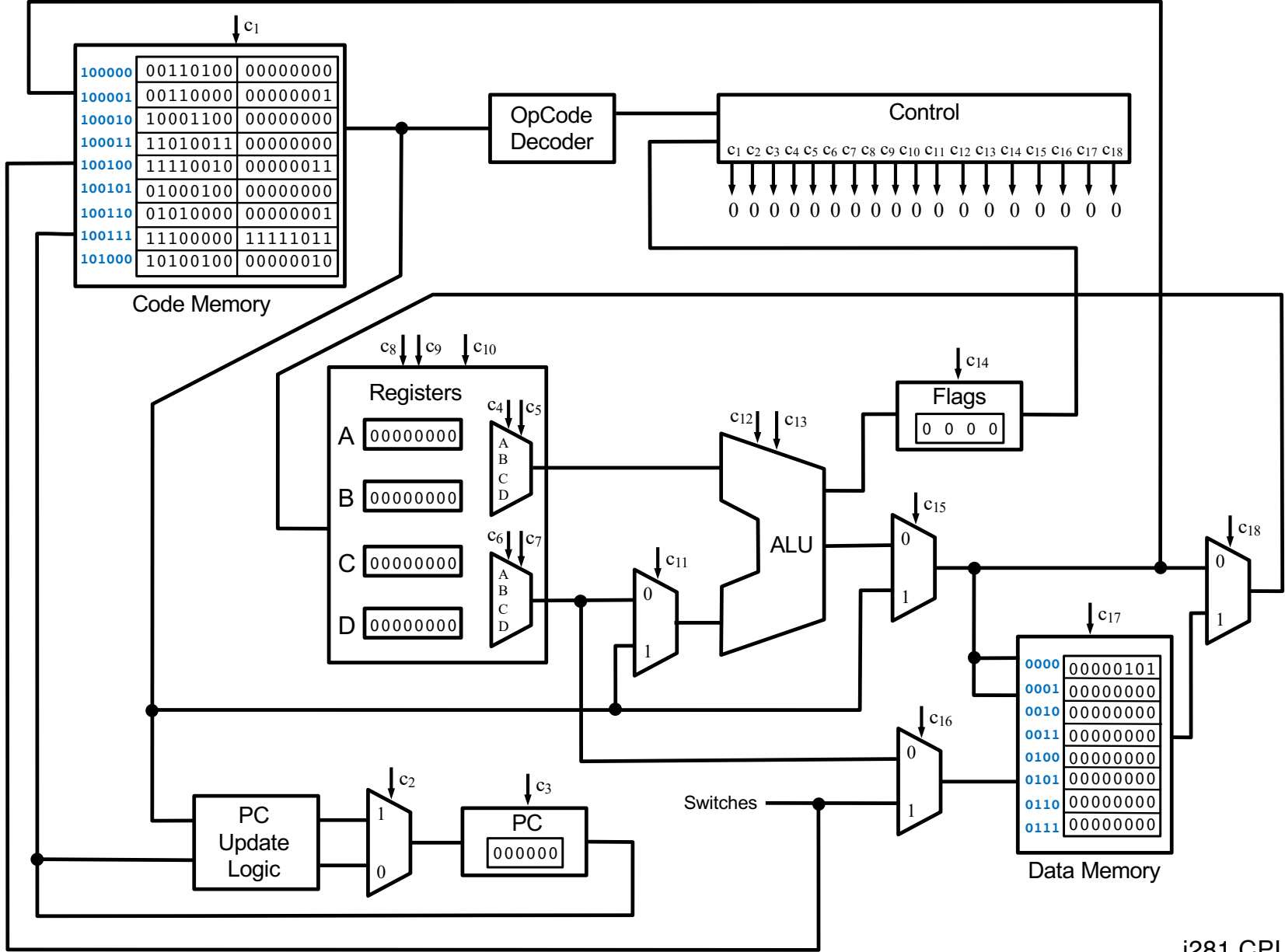
... are mapped to 0 by the Assembler

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010

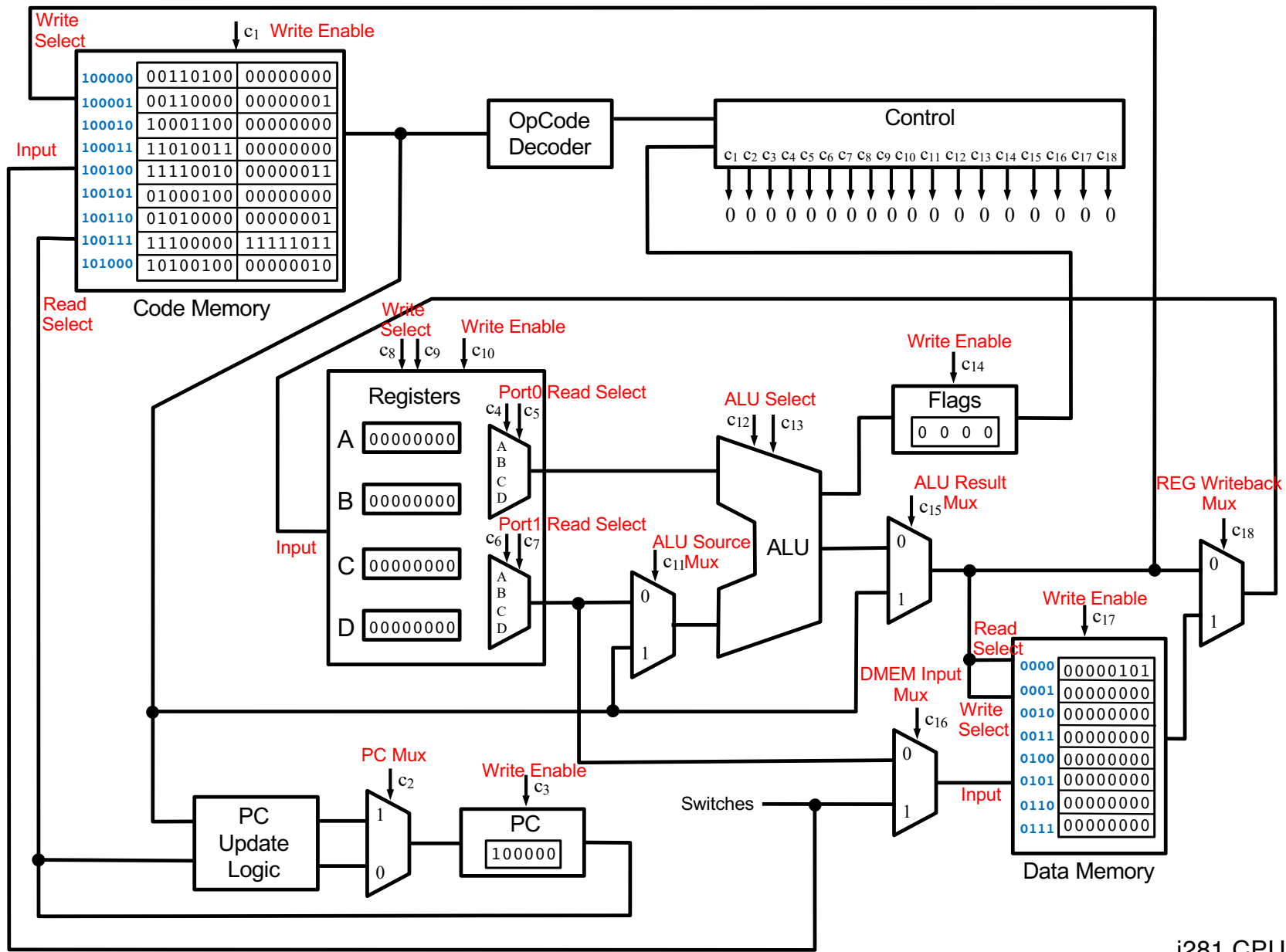
Mapping Assembly to Machine Code

.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010

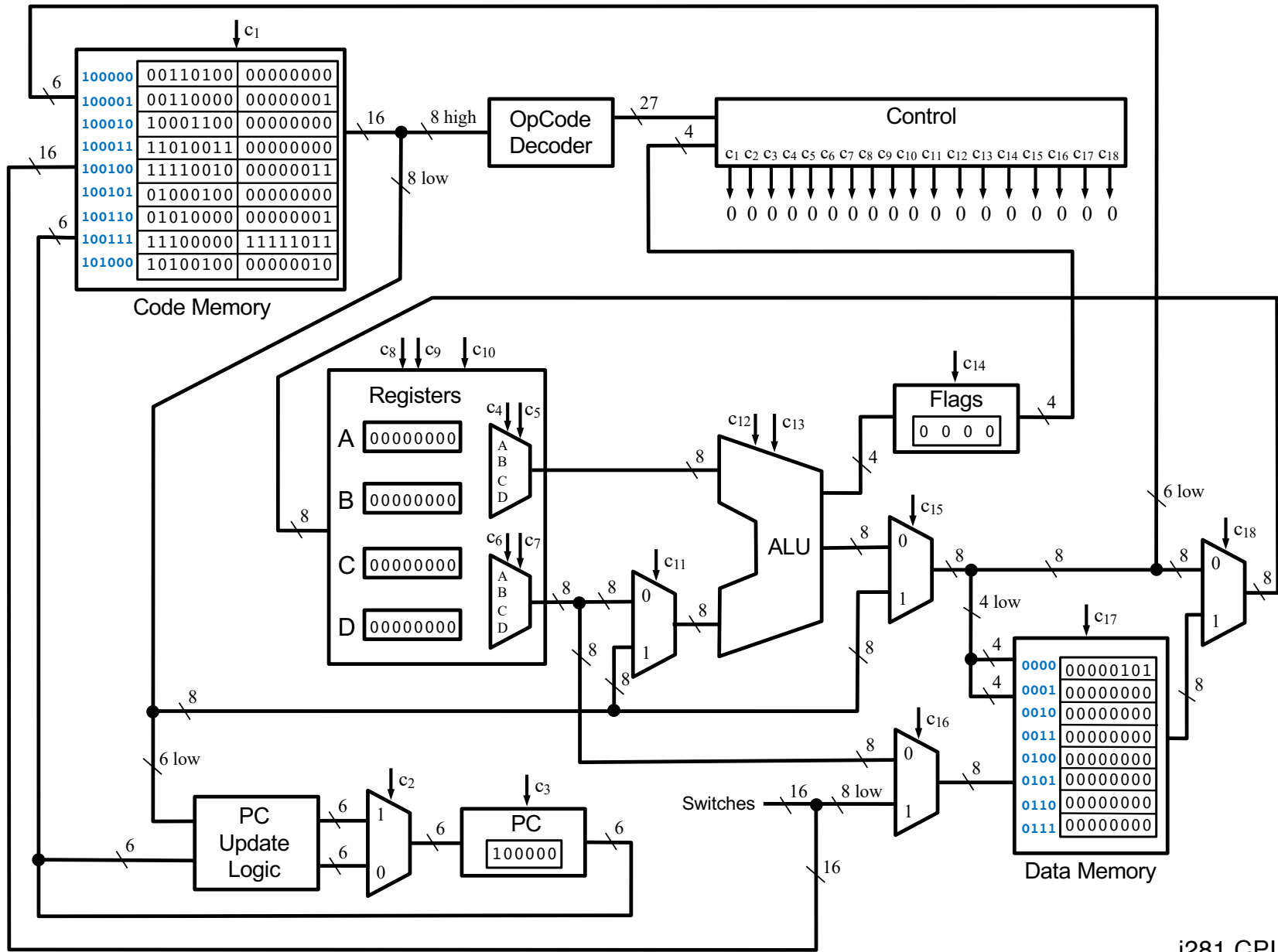
Loading the Program into Memory



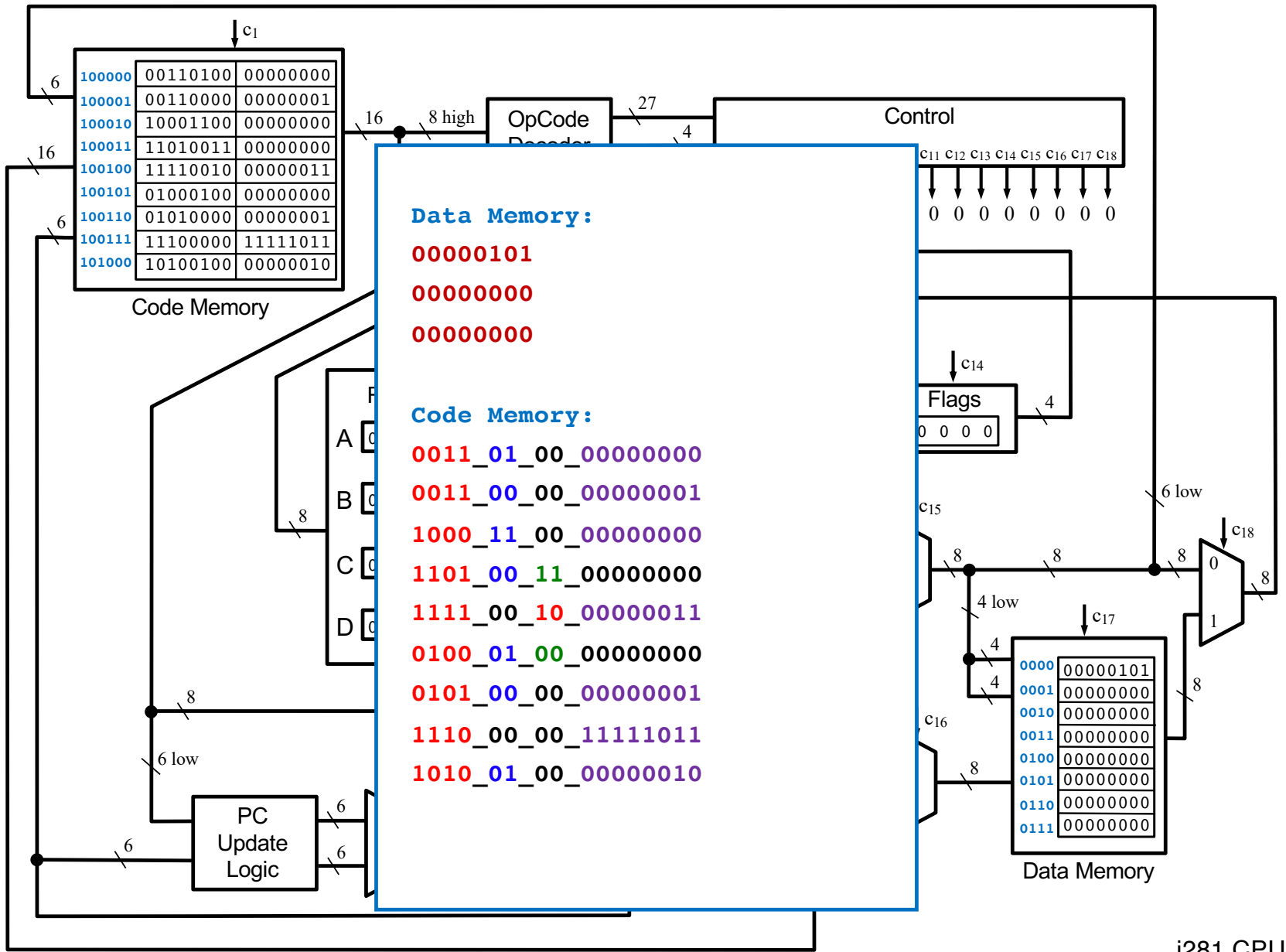
i281 CPU



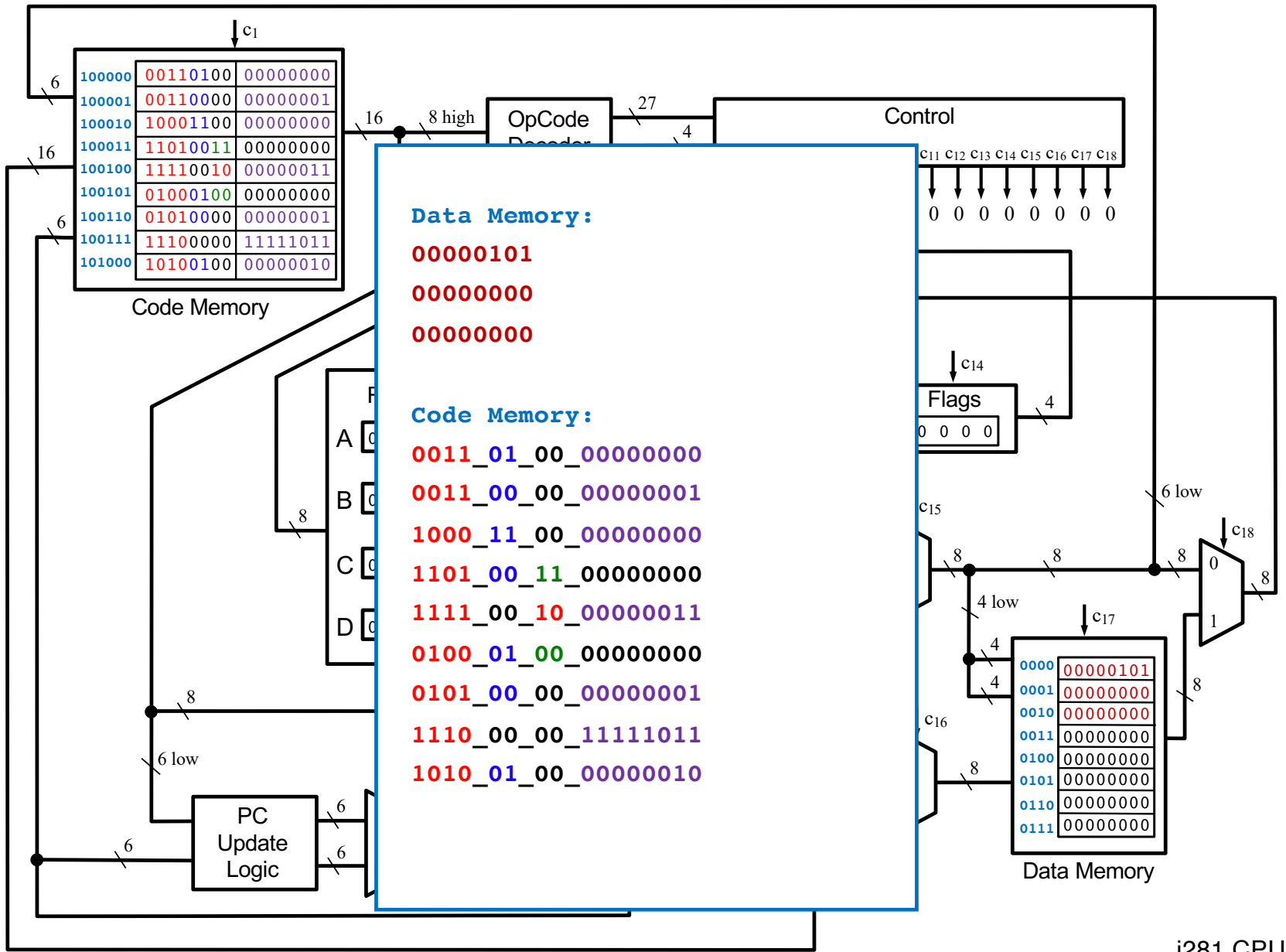
i281 CPU



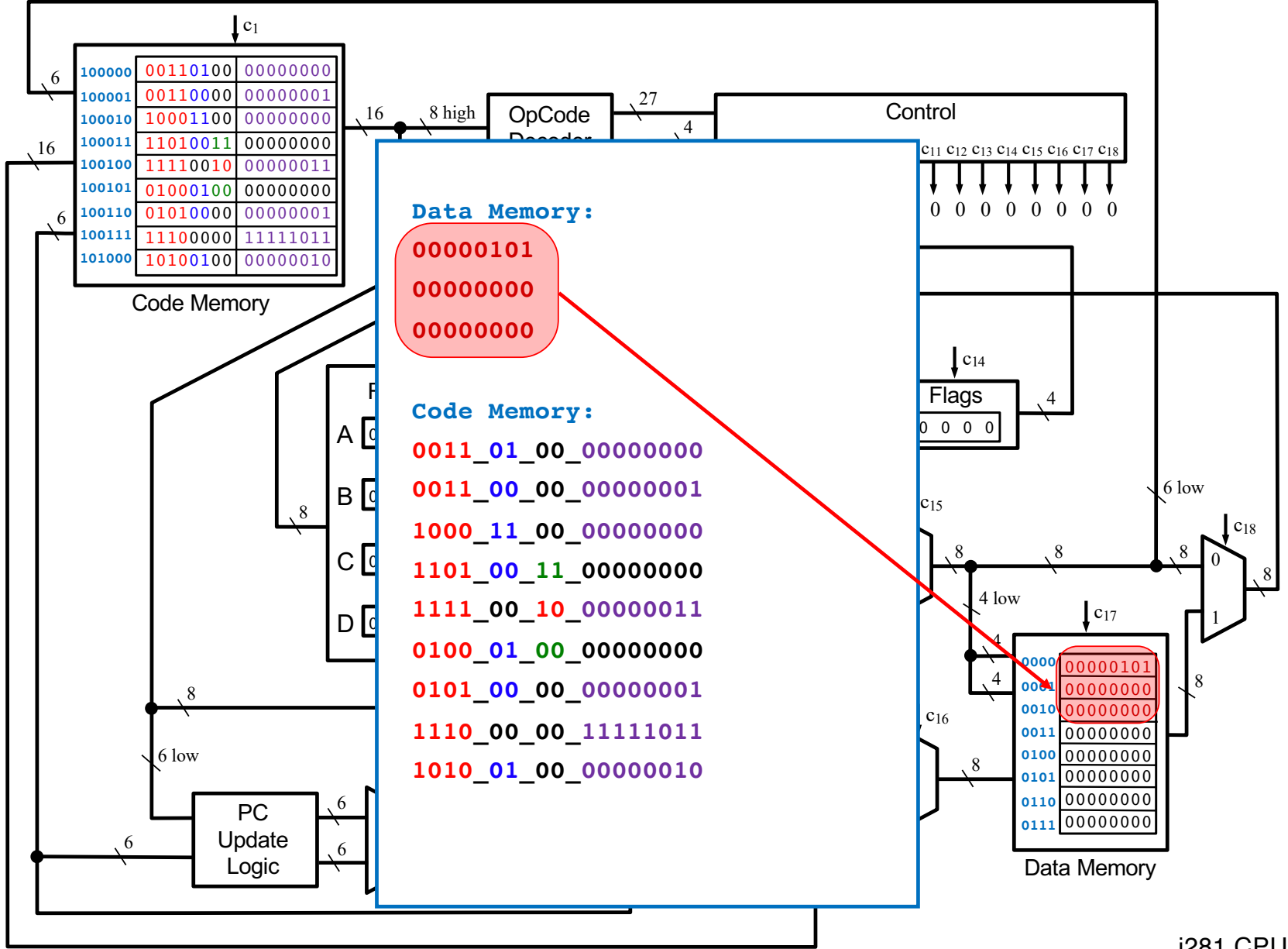
i281 CPU



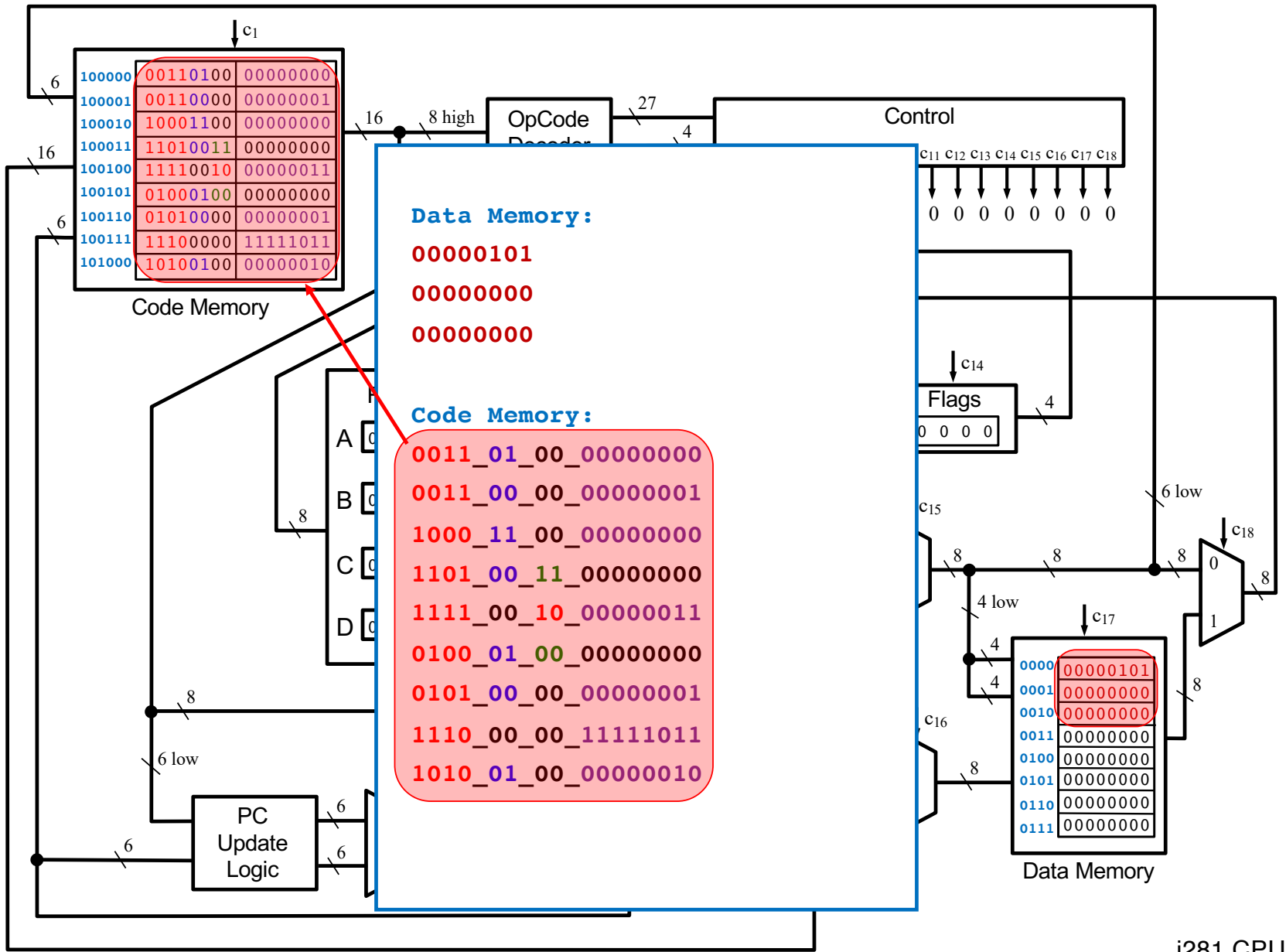
i281 CPU



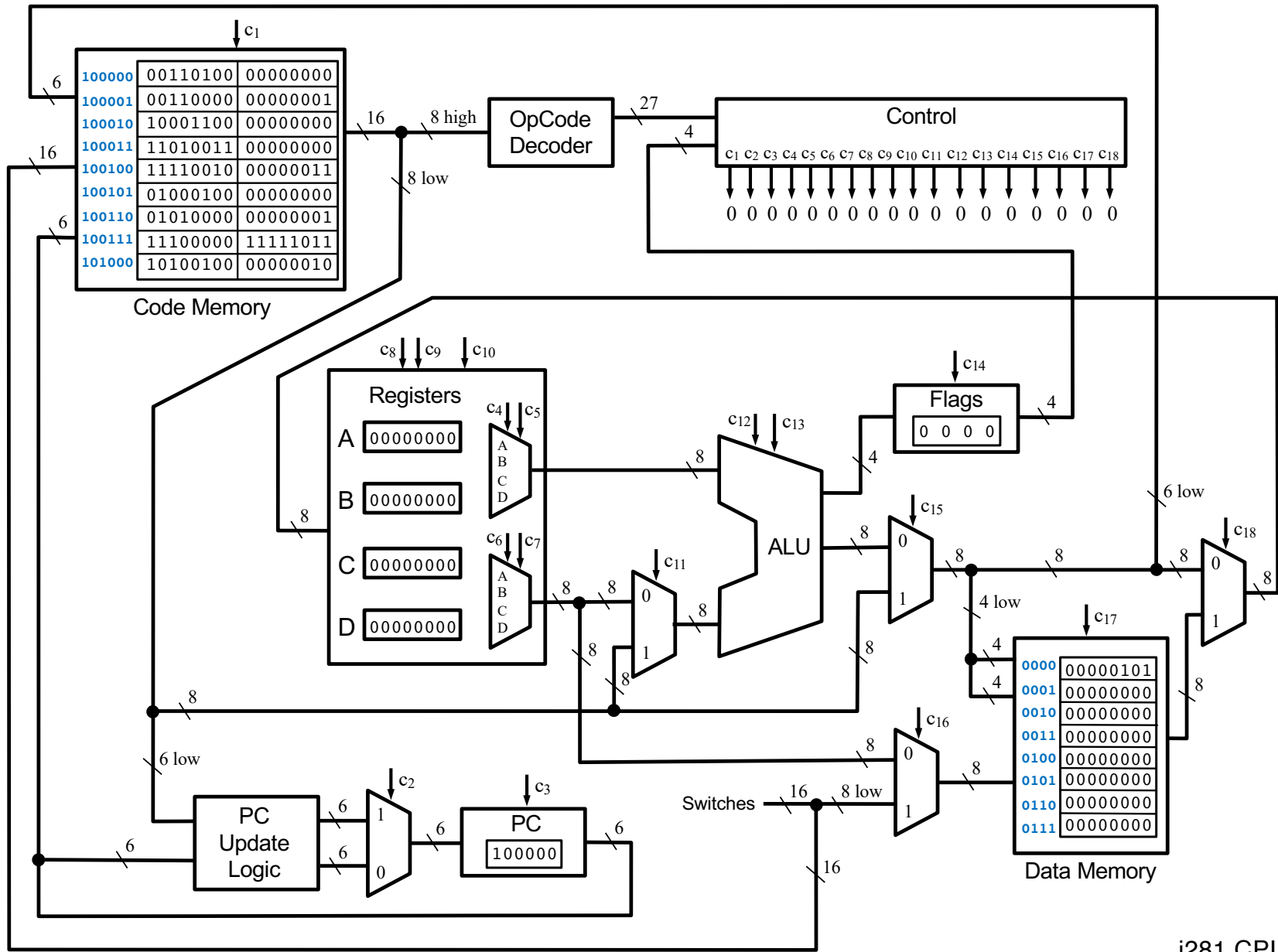
i281 CPU



i281 CPU

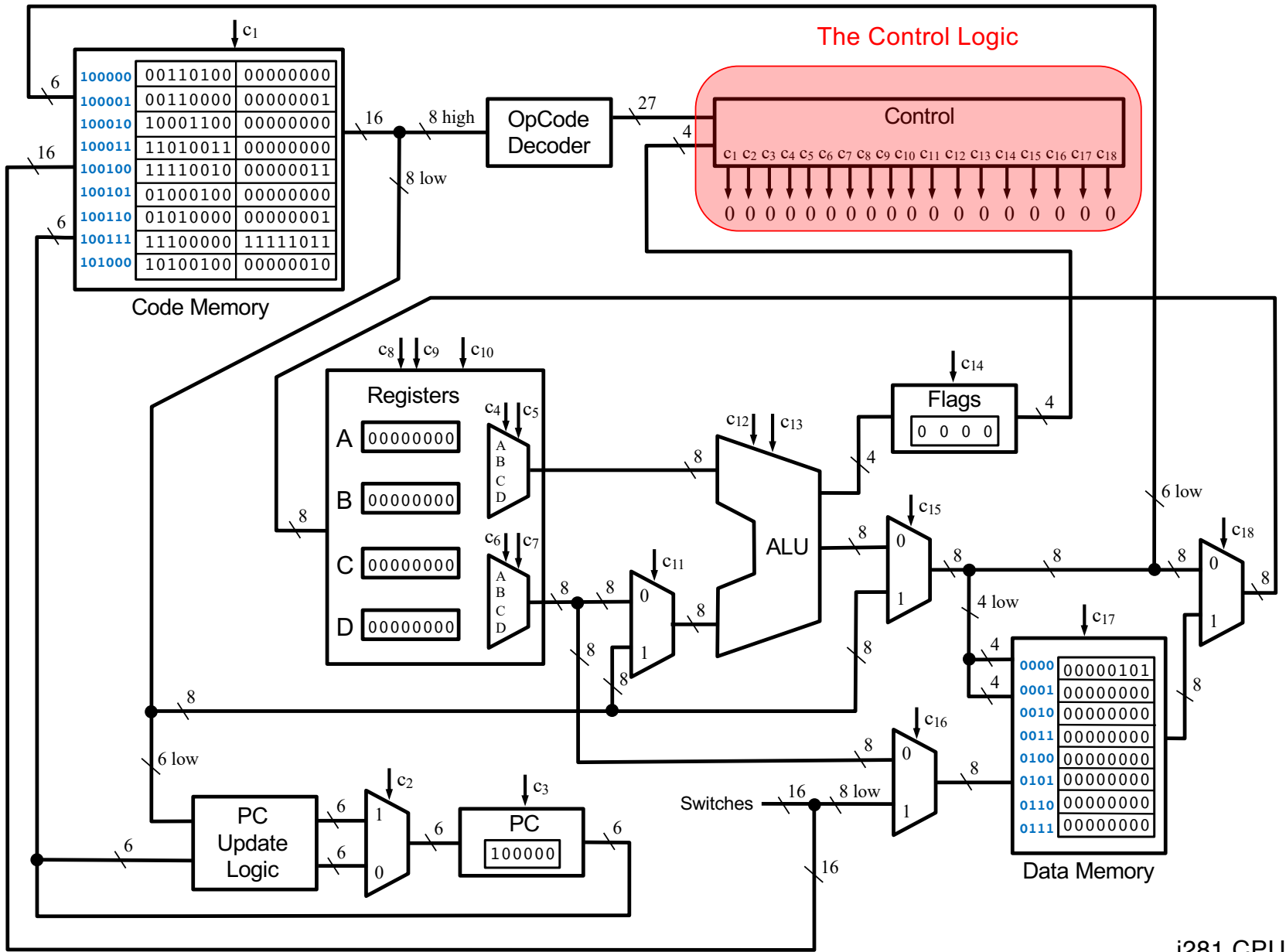


i281 CPU

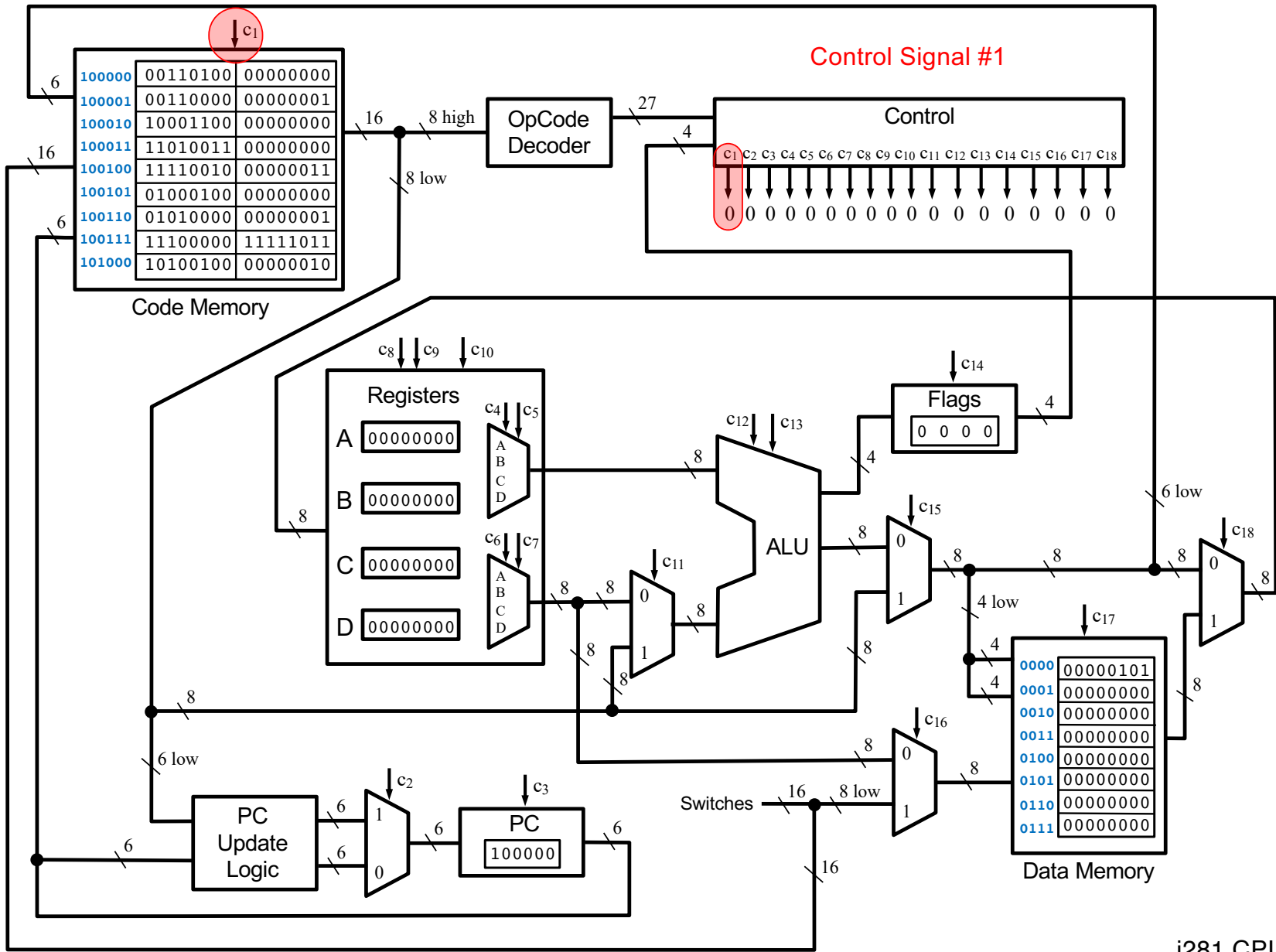


i281 CPU

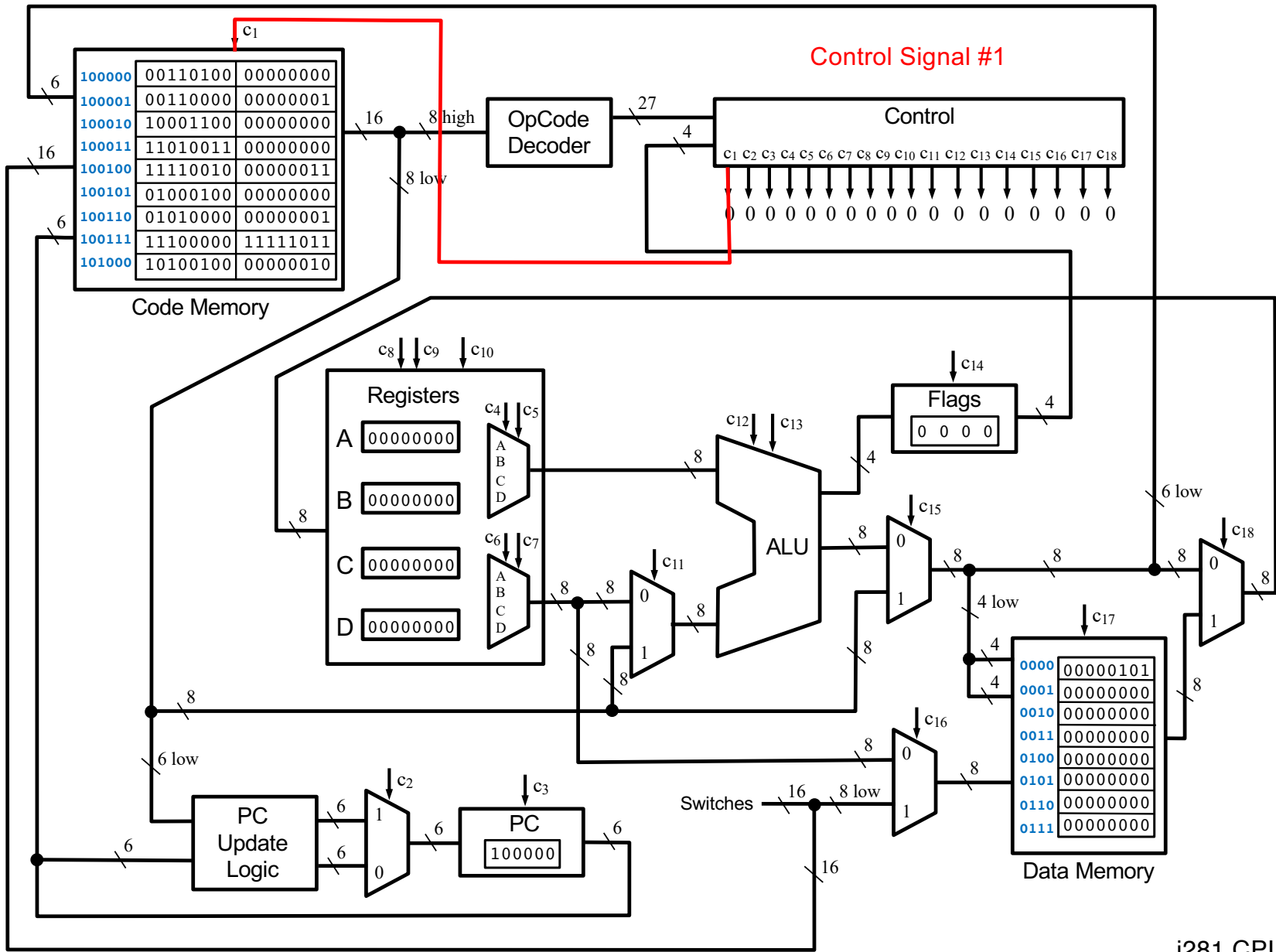
The CPU Control Logic



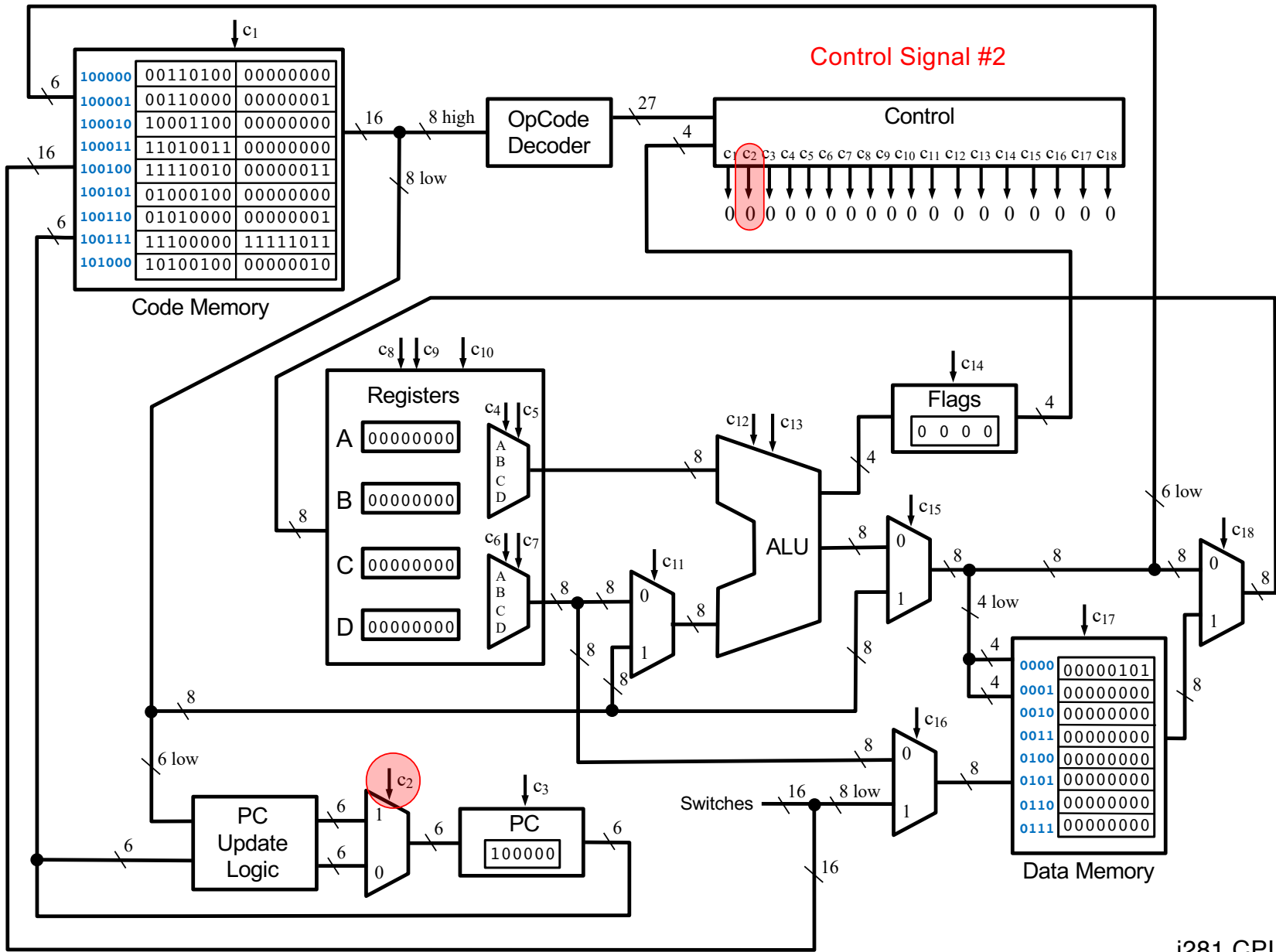
i281 CPU



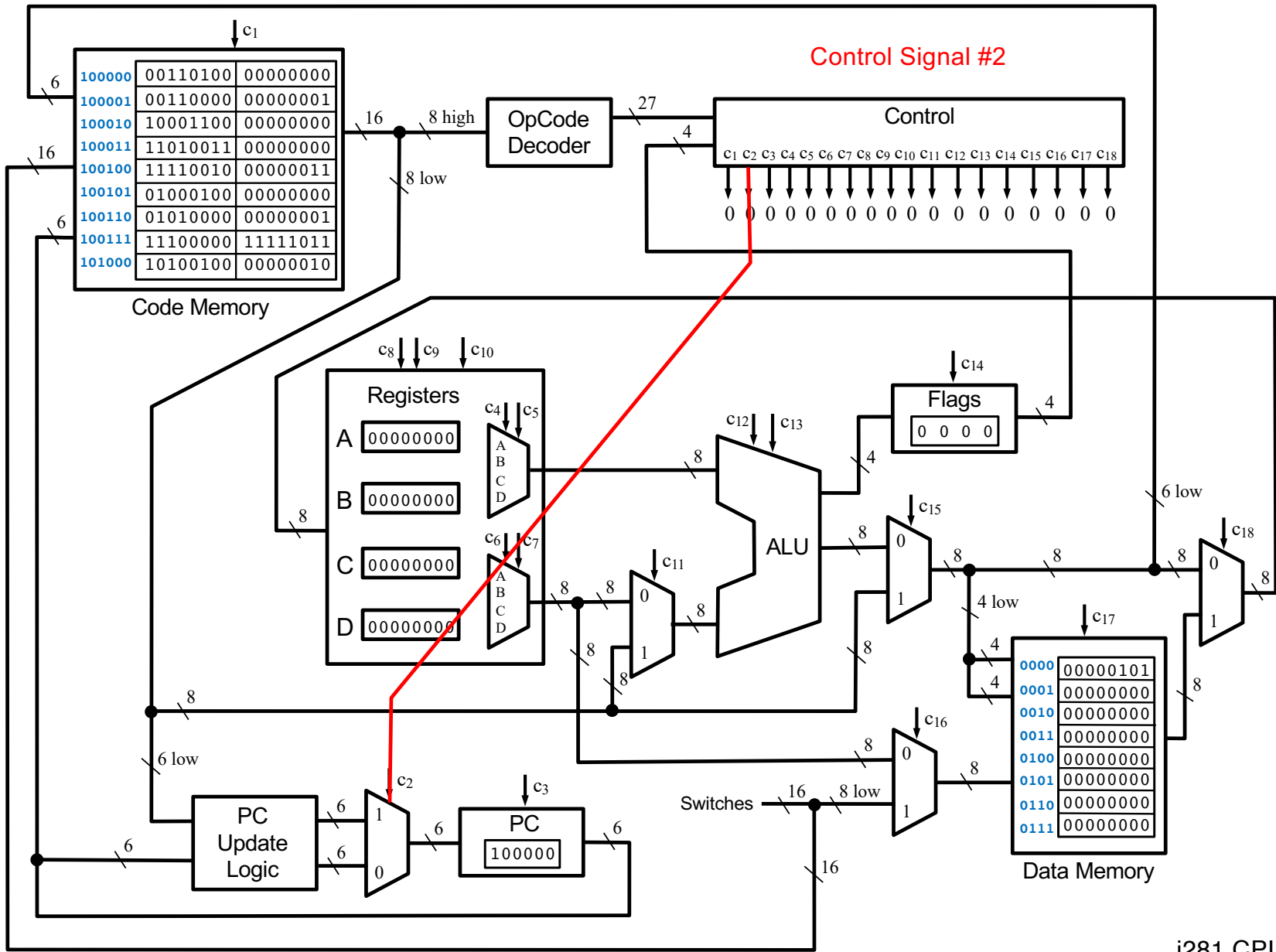
i281 CPU



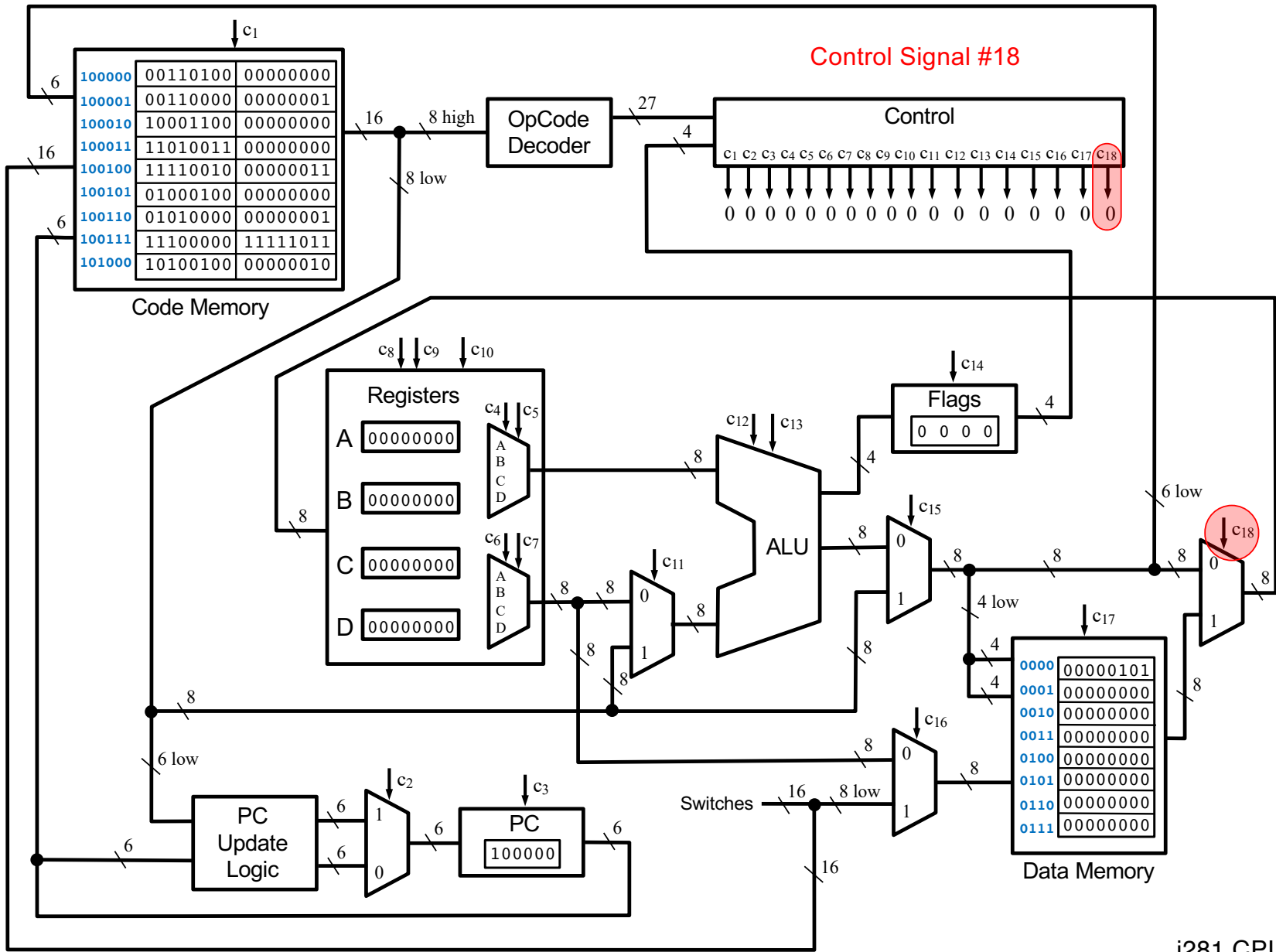
i281 CPU



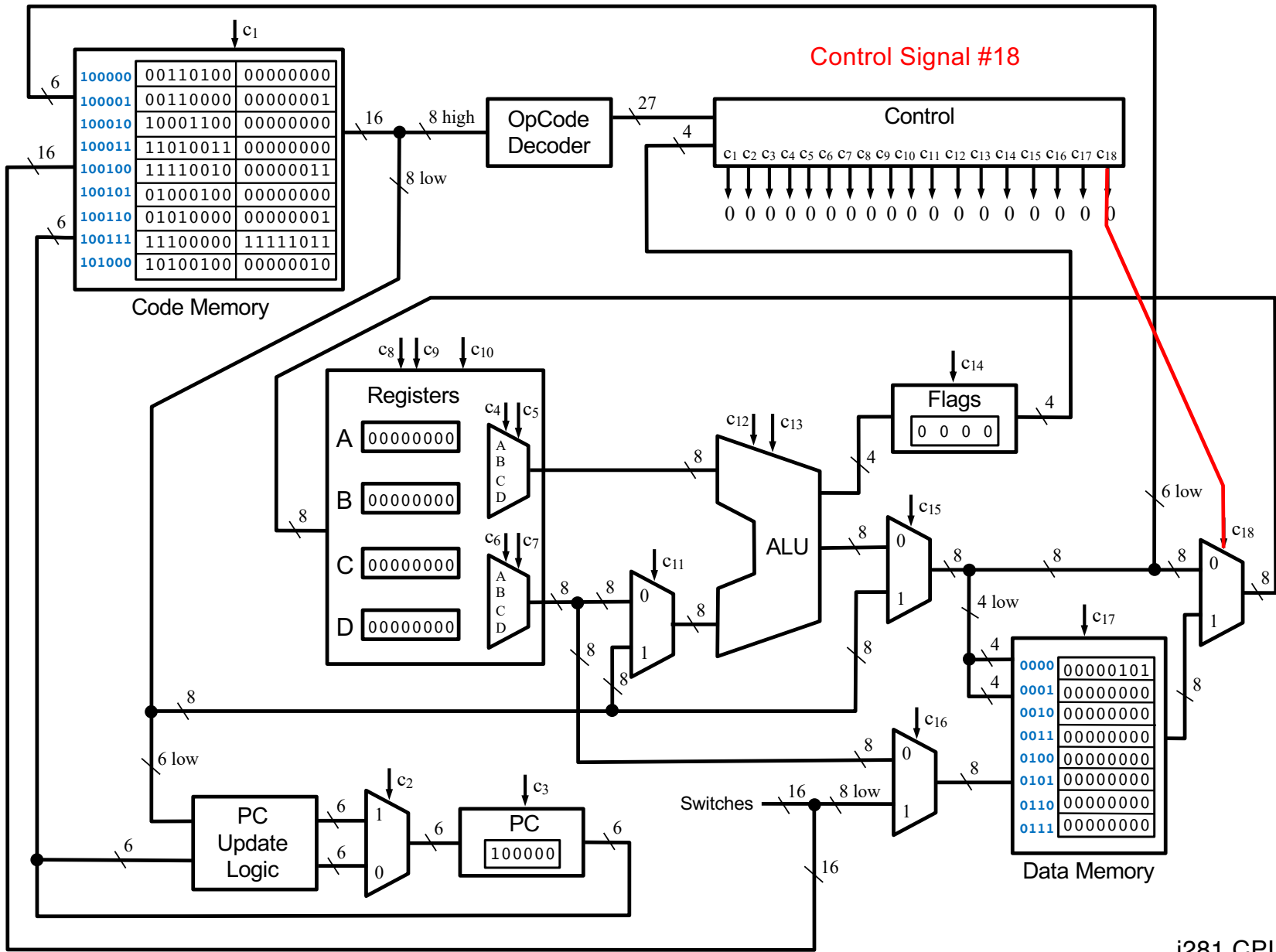
i281 CPU



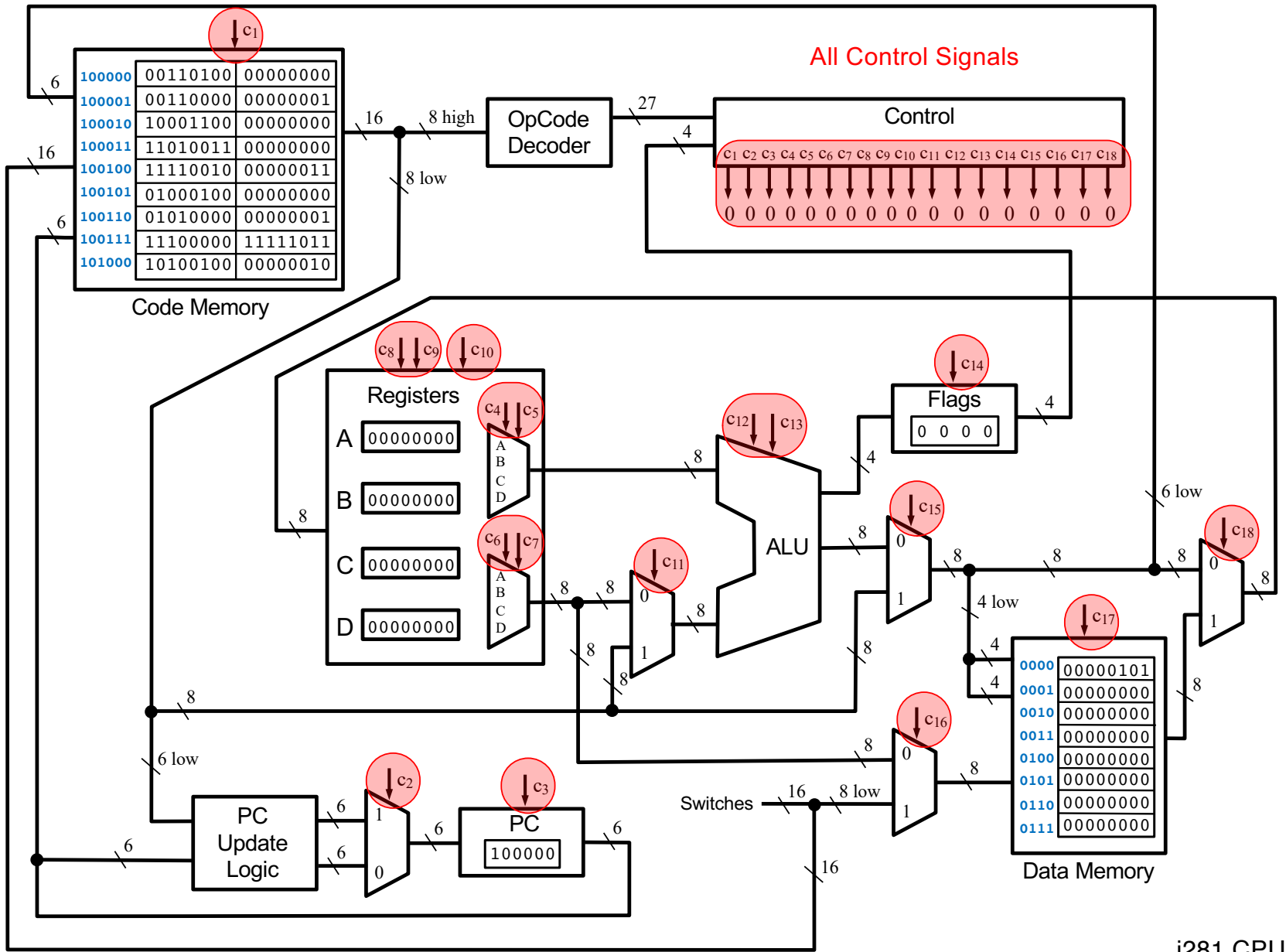
i281 CPU



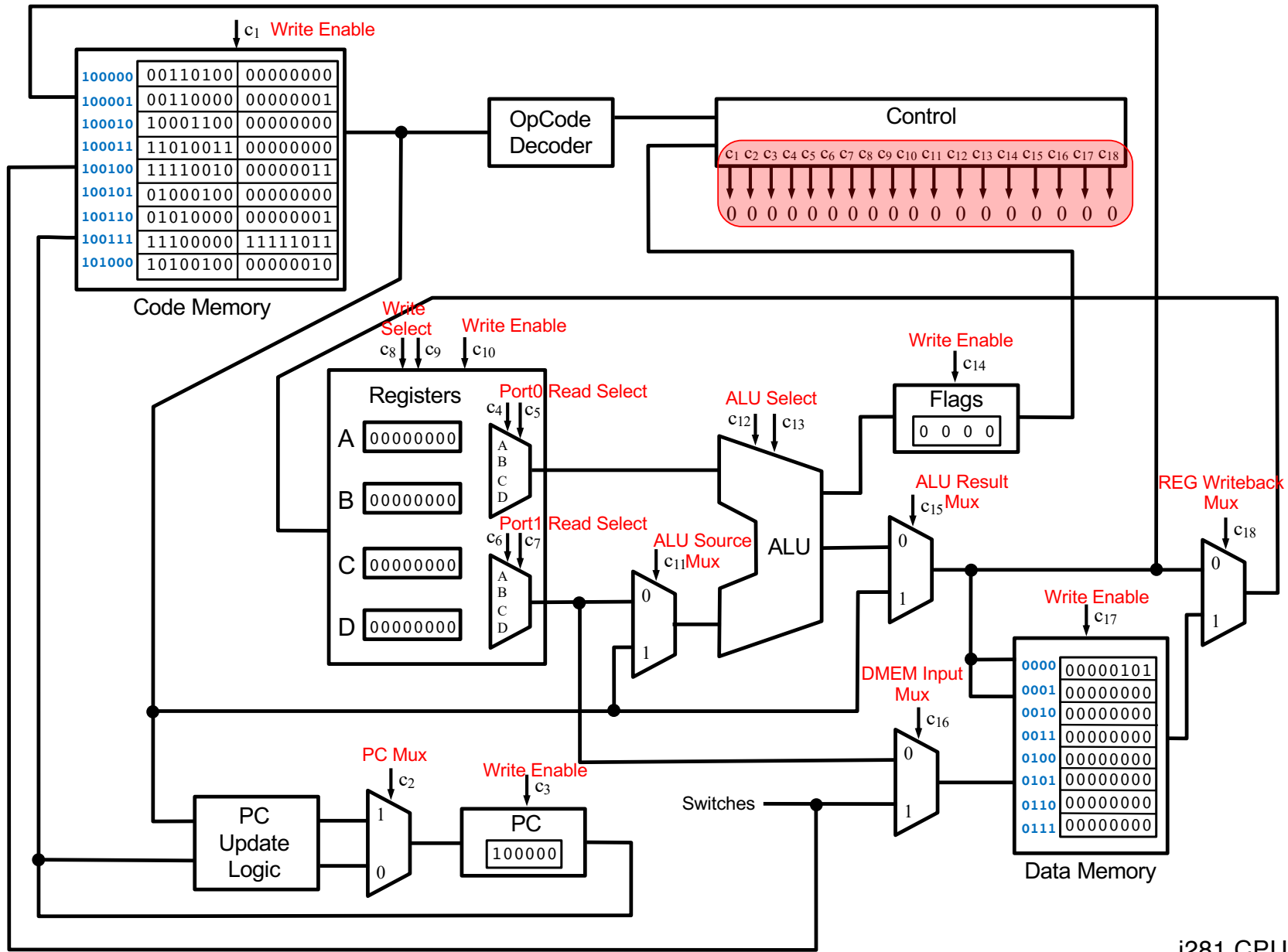
i281 CPU



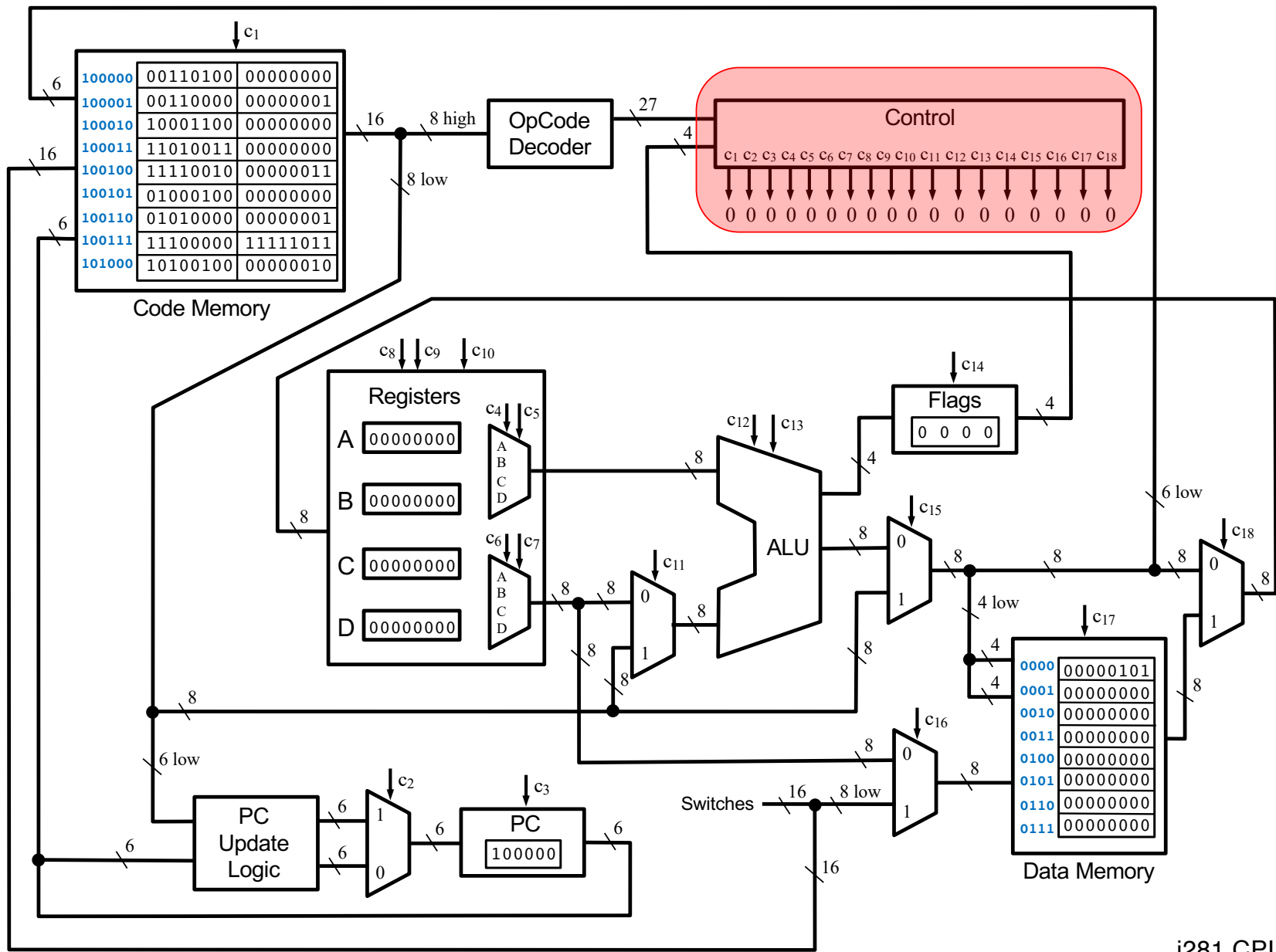
i281 CPU



i281 CPU



i281 CPU

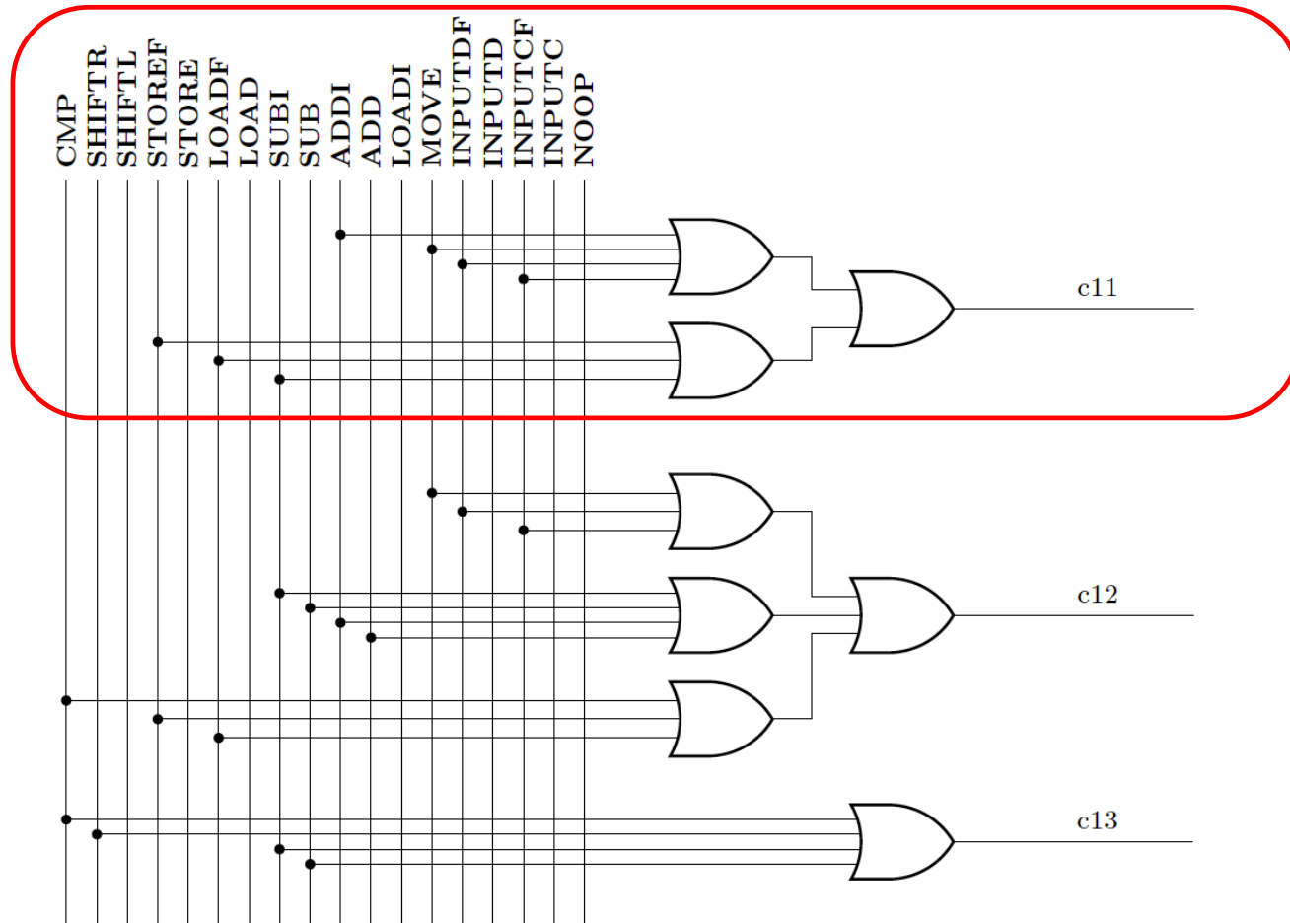


i281 CPU

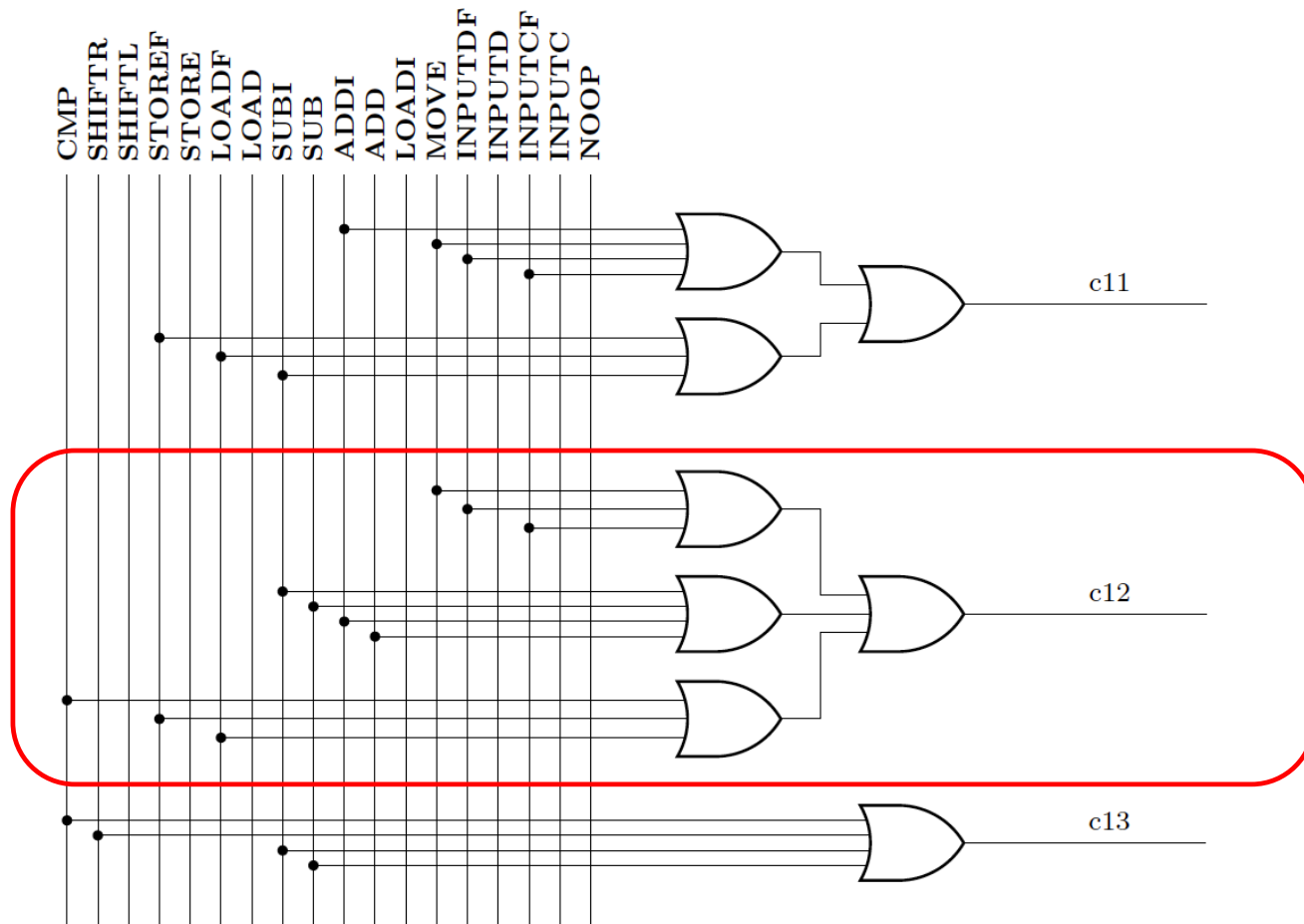
The OPCODEs for this CPU

NOOP	NO OPERATION
INPUTC	INPUT into Code memory
INPUTCF	INPUT into Code memory with offset
INPUTD	INPUT into Data memory
INPUTDF	INPUT into Data memory with offset
MOVE	MOVE the contents of one register into another
LOADI	LOAD Immediate value
LOADP	LOAD Pointer address
ADD	ADD two registers
ADDI	ADD an Immediate value to a register
SUB	SUBtract two registers
SUBI	SUBtract an Immediate value from a register
LOAD	LOAD from a data memory address into a register
LOADF	LOAD with an offset specified by another register
STORE	STORE a register into a data memory address
STOREF	STORE with an offset specified by another register
SHIFTL	SHIFT Left all bits in a register
SHIFTR	SHIFT Right all bits in a register
CMP	CoMPare the values in two registers
JUMP	JUMP unconditionally to a specified address
BRE	BRanch if Equal
BRZ	BRanch if Zero
BRNE	BRanch if Not Equal
BRNZ	BRanch if Not Zero
BRG	BRanch if Greater
BRGE	BRanch if Greater than or Equal

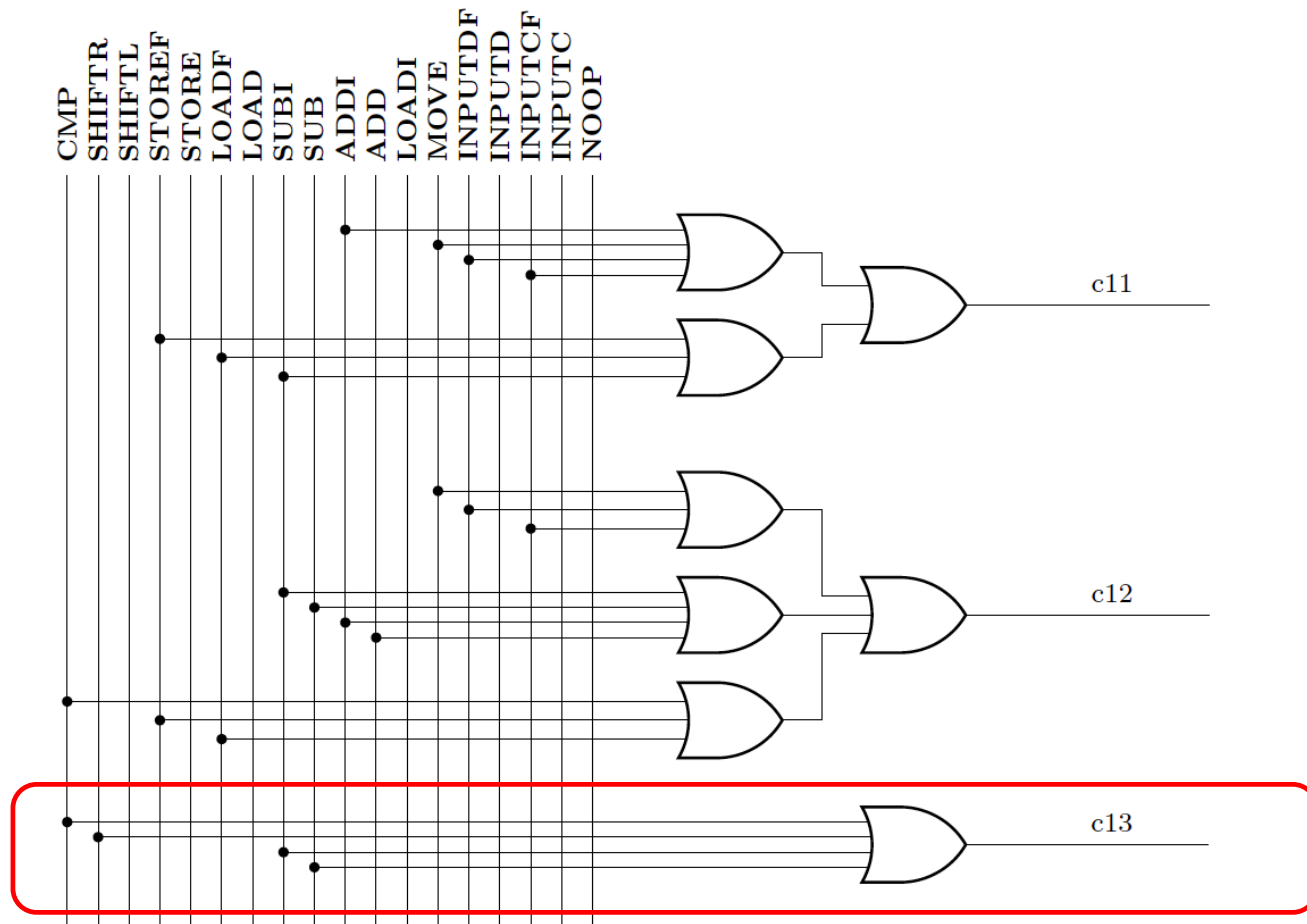
The Wiring Diagram for c_{11}



The Wiring Diagram for c_{12}



The Wiring Diagram for c_{13}



Simulation of the Program Execution

Add the numbers from 1 to 5

```
// C Version
// using a for loop

int main()
{
    int N=5;
    int i, sum;

    sum=0;
    for(i=1; i<=N; i++) {
        sum+=i;
    }

    // printf("%d\n", sum);
}
```

```
; Assembly Version

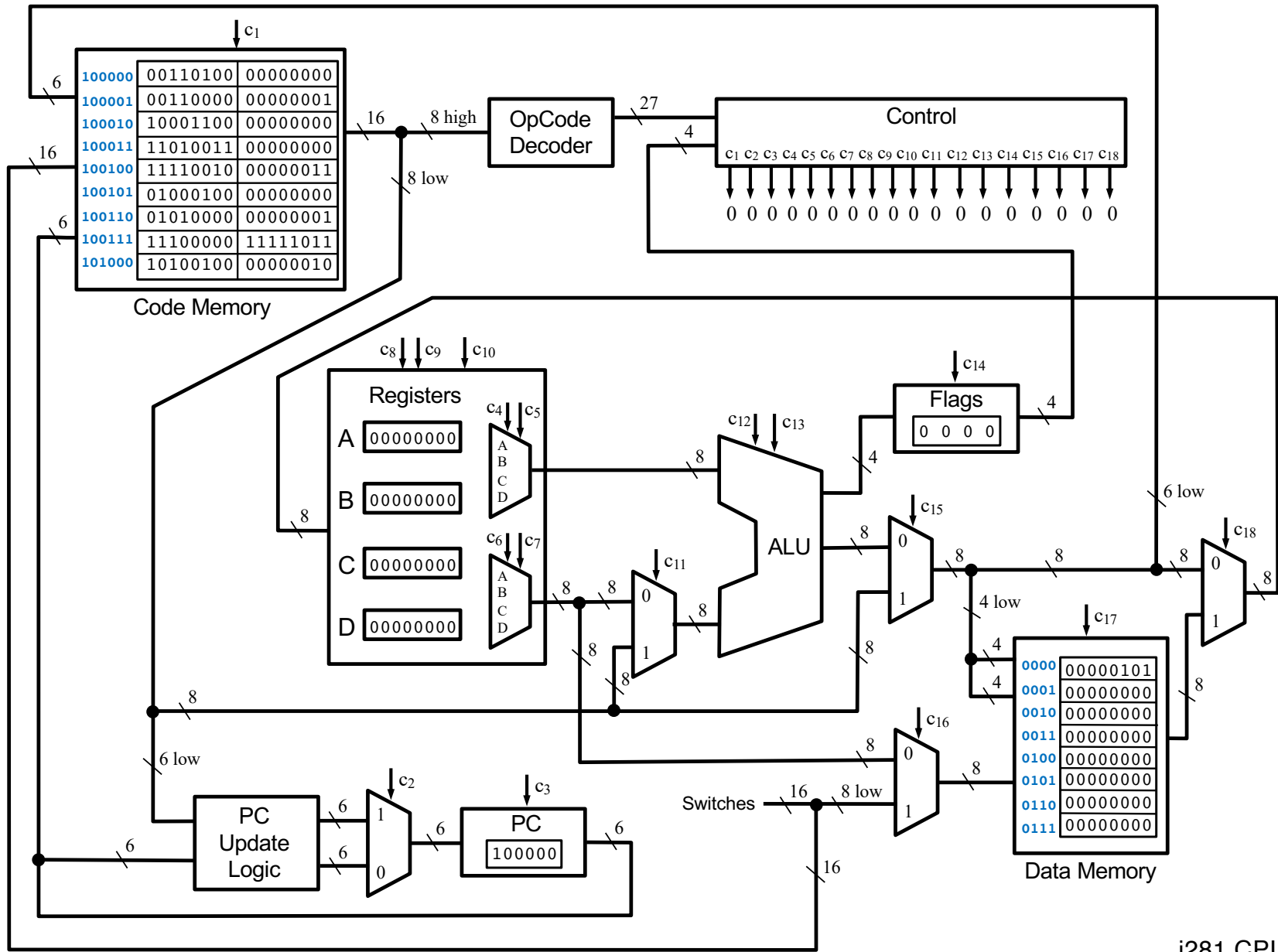
.data
N      BYTE    5
i      BYTE    ?
sum    BYTE    ?

.code

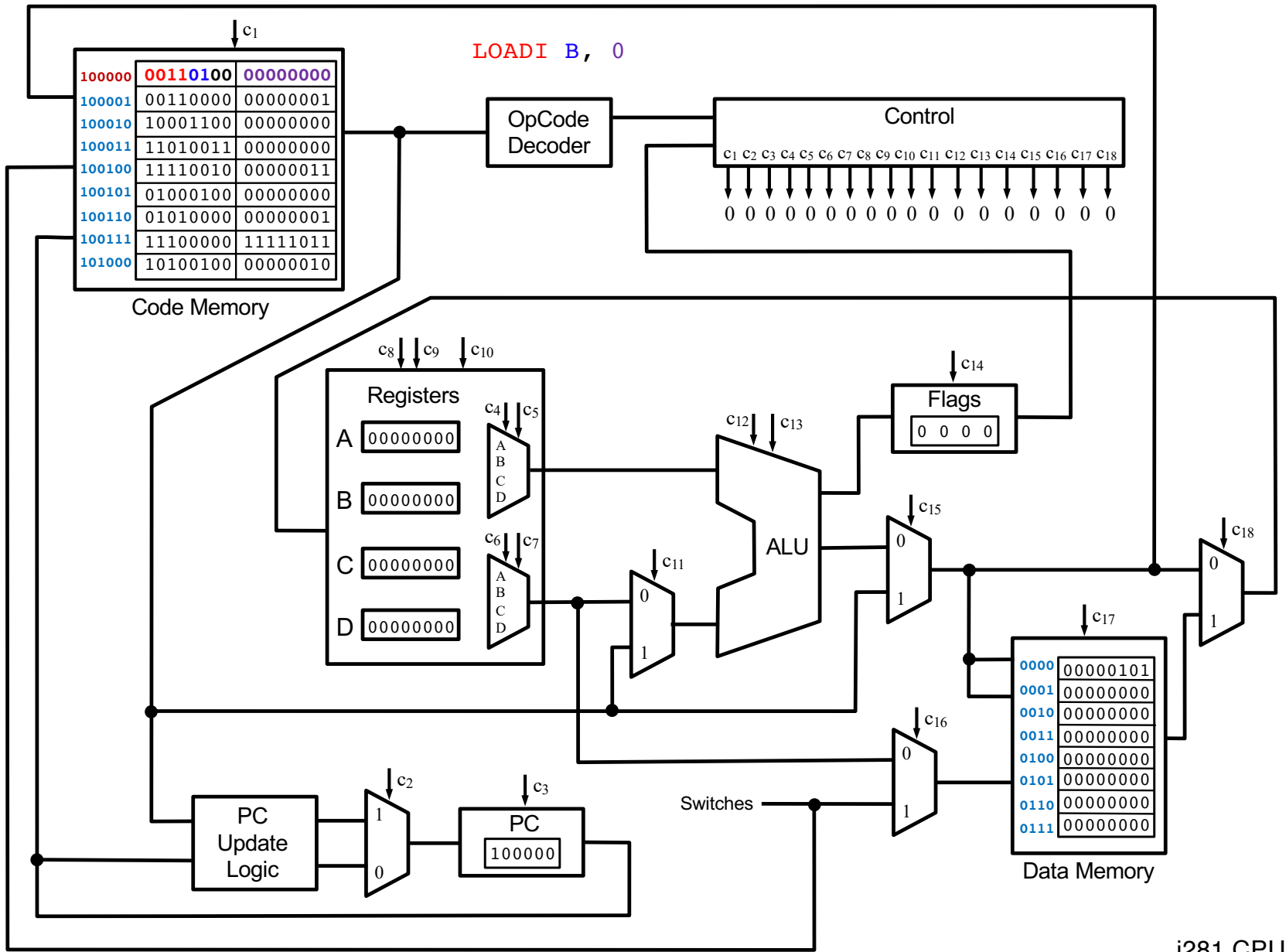
        LOADI  B, 0      ; sum=0
        LOADI  A, 1      ; i=1
        LOAD   D, [N]    ; register_D=N
Loop:   CMP    A, D      ; i<=N ?
        BRG    End      ; exit if i>N
Add:    ADD   B, A      ; sum+=i
        ADDI  A, 1      ; i++
        JUMP  Loop      ; next iteration
End:    STORE [sum], B  ; write B to sum
```

Mapping Assembly to Machine Code

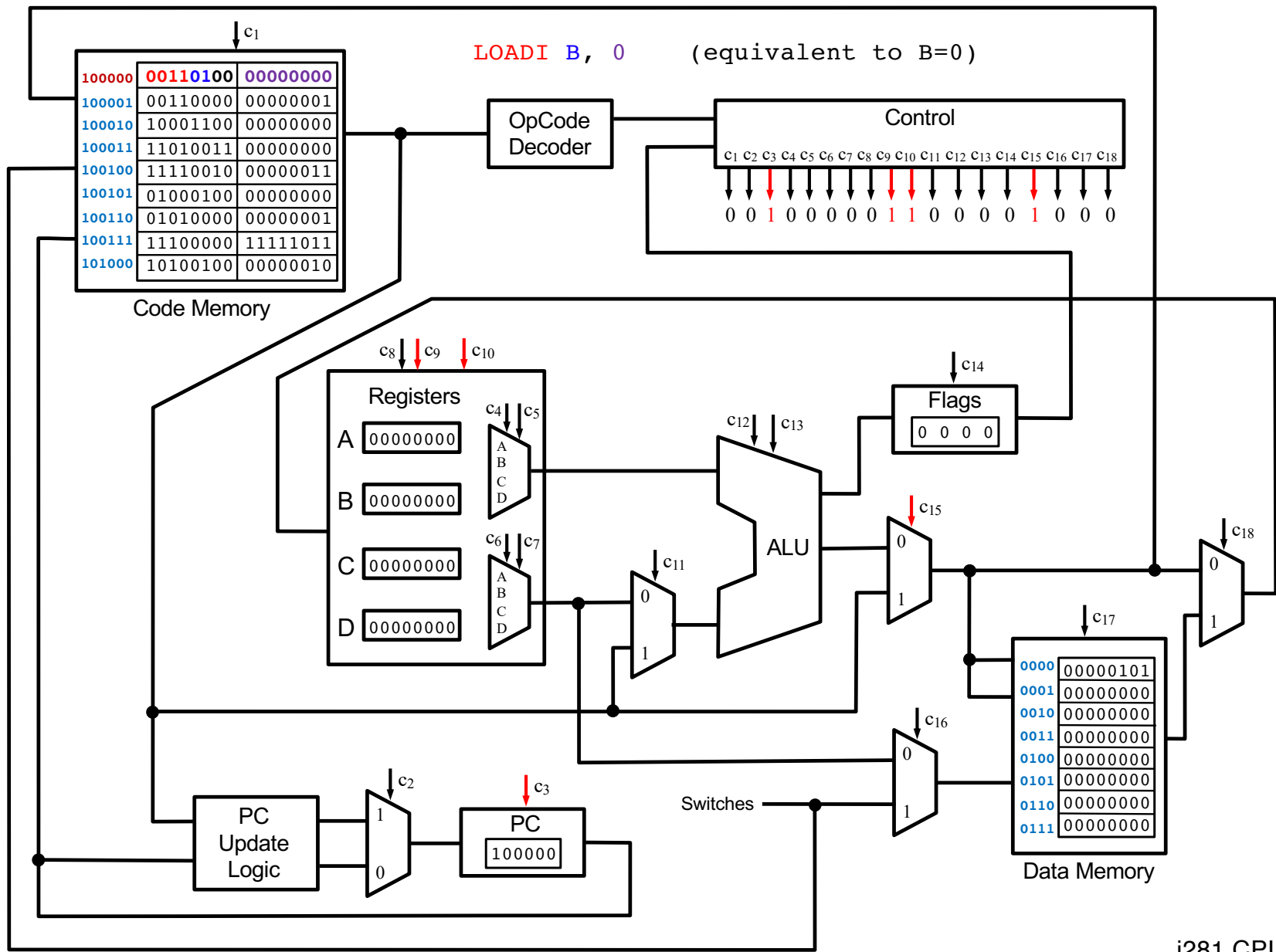
.data			Data Memory:
N	BYTE	5	00000101
i	BYTE	?	00000000
sum	BYTE	?	00000000
.code			Code Memory:
	LOADI	B, 0	0011_01_00_00000000
	LOADI	A, 1	0011_00_00_00000001
	LOAD	D, [N]	1000_11_00_00000000
Loop:	CMP	A, D	1101_00_11_00000000
	BRG	End	1111_00_10_00000011
Add:	ADD	B, A	0100_01_00_00000000
	ADDI	A, 1	0101_00_00_00000001
	JUMP	Loop	1110_00_00_11111011
End:	STORE	[sum], B	1010_01_00_00000010



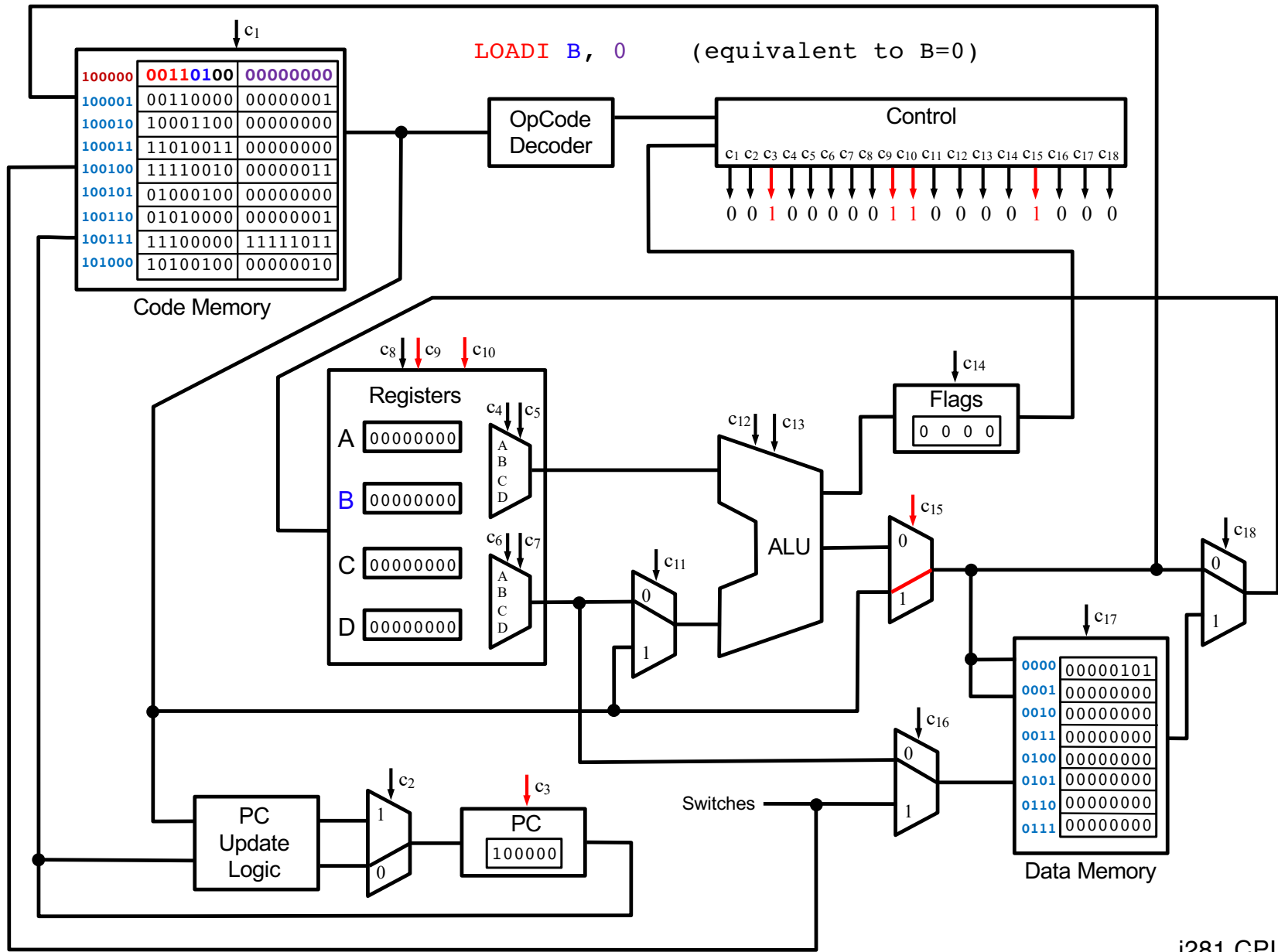
i281 CPU



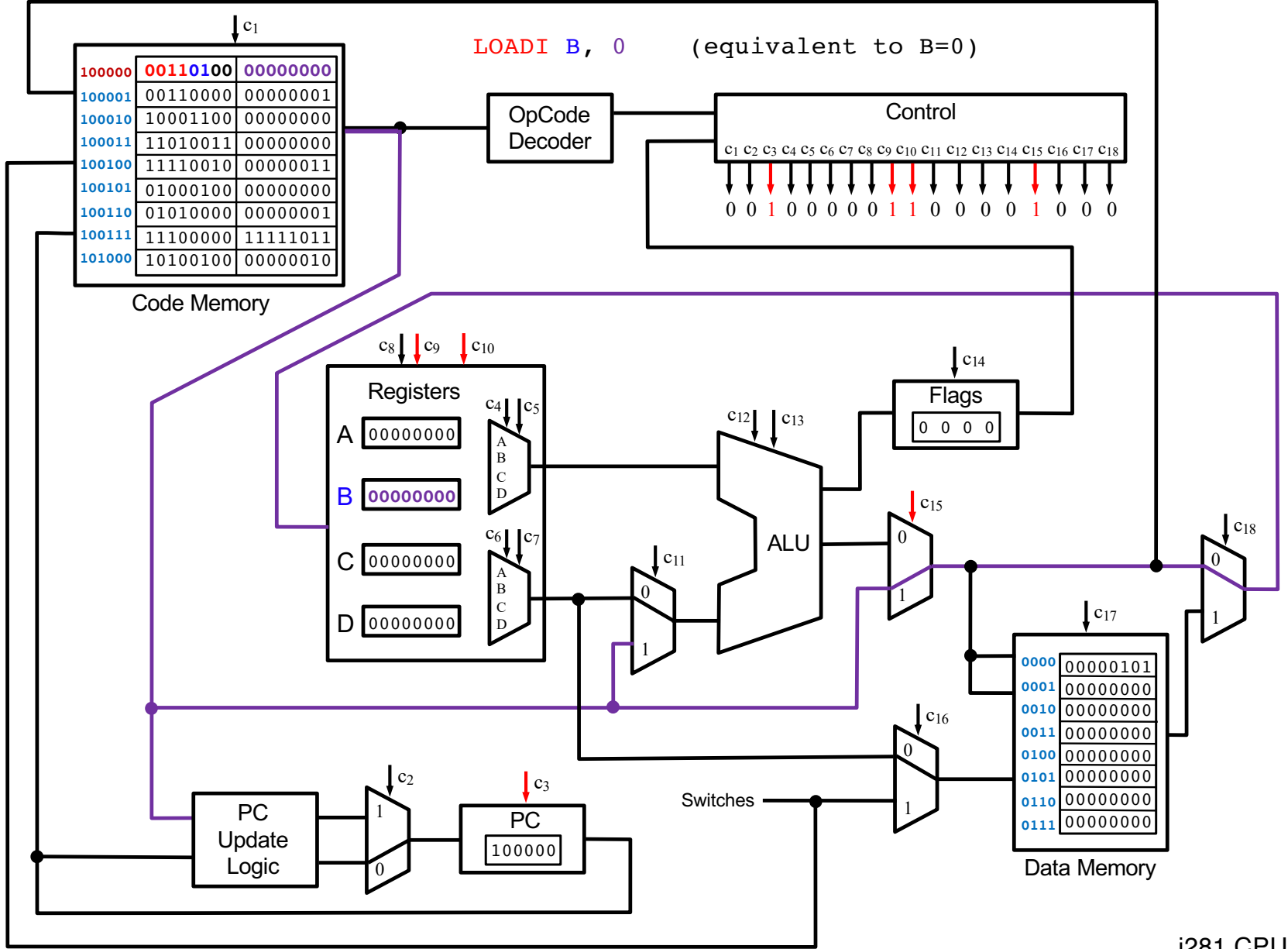
i281 CPU



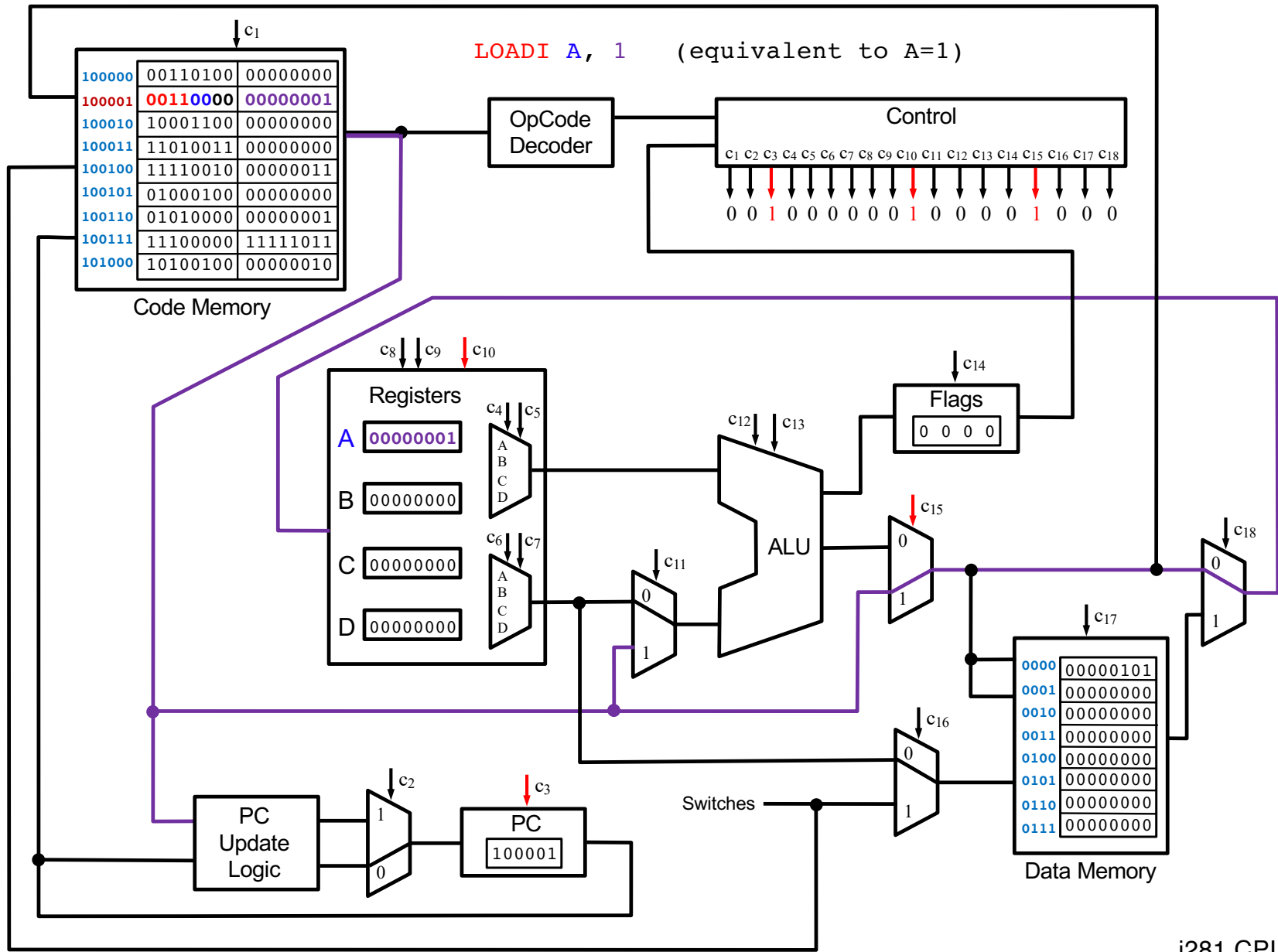
i281 CPU



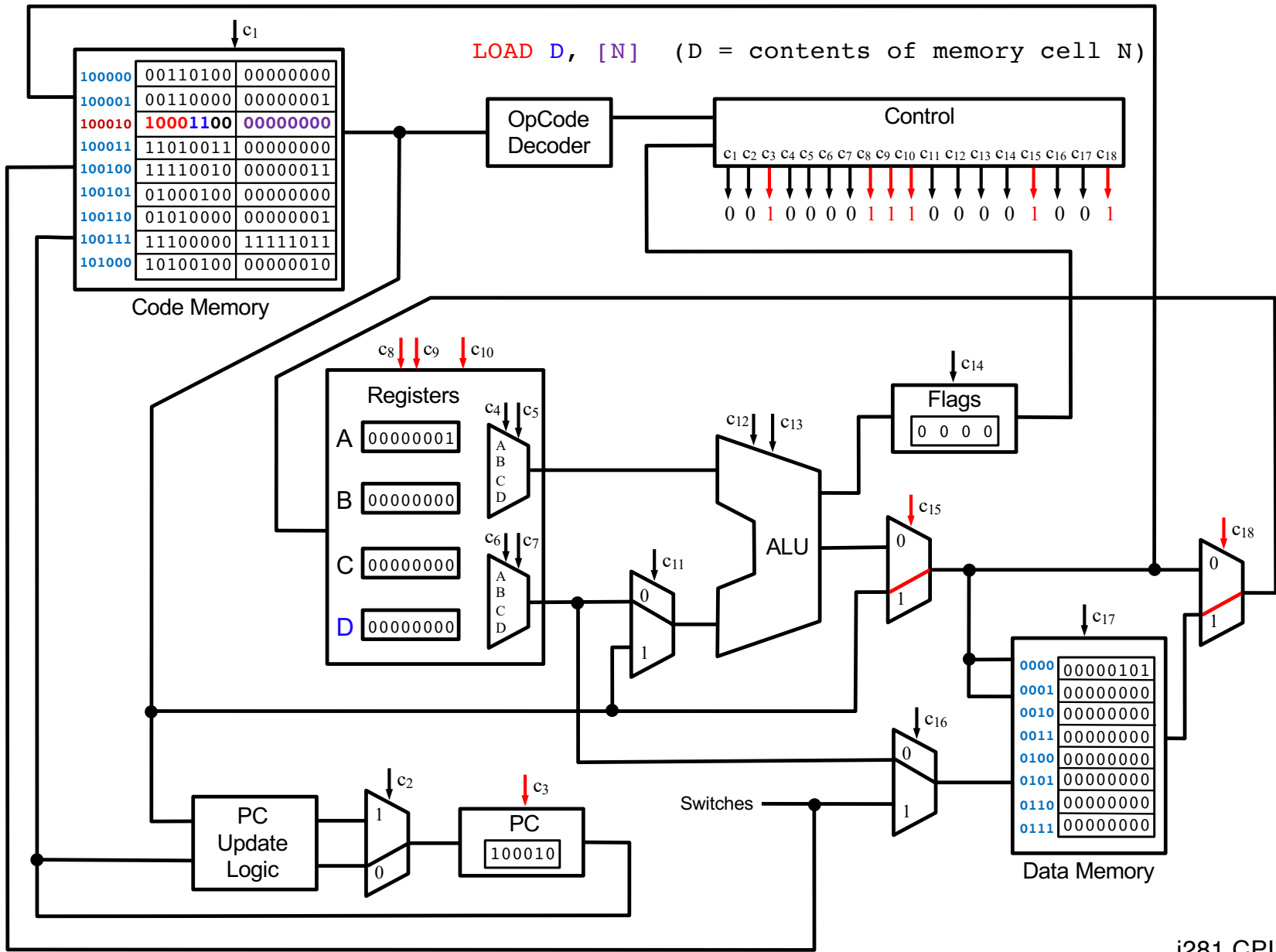
i281 CPU



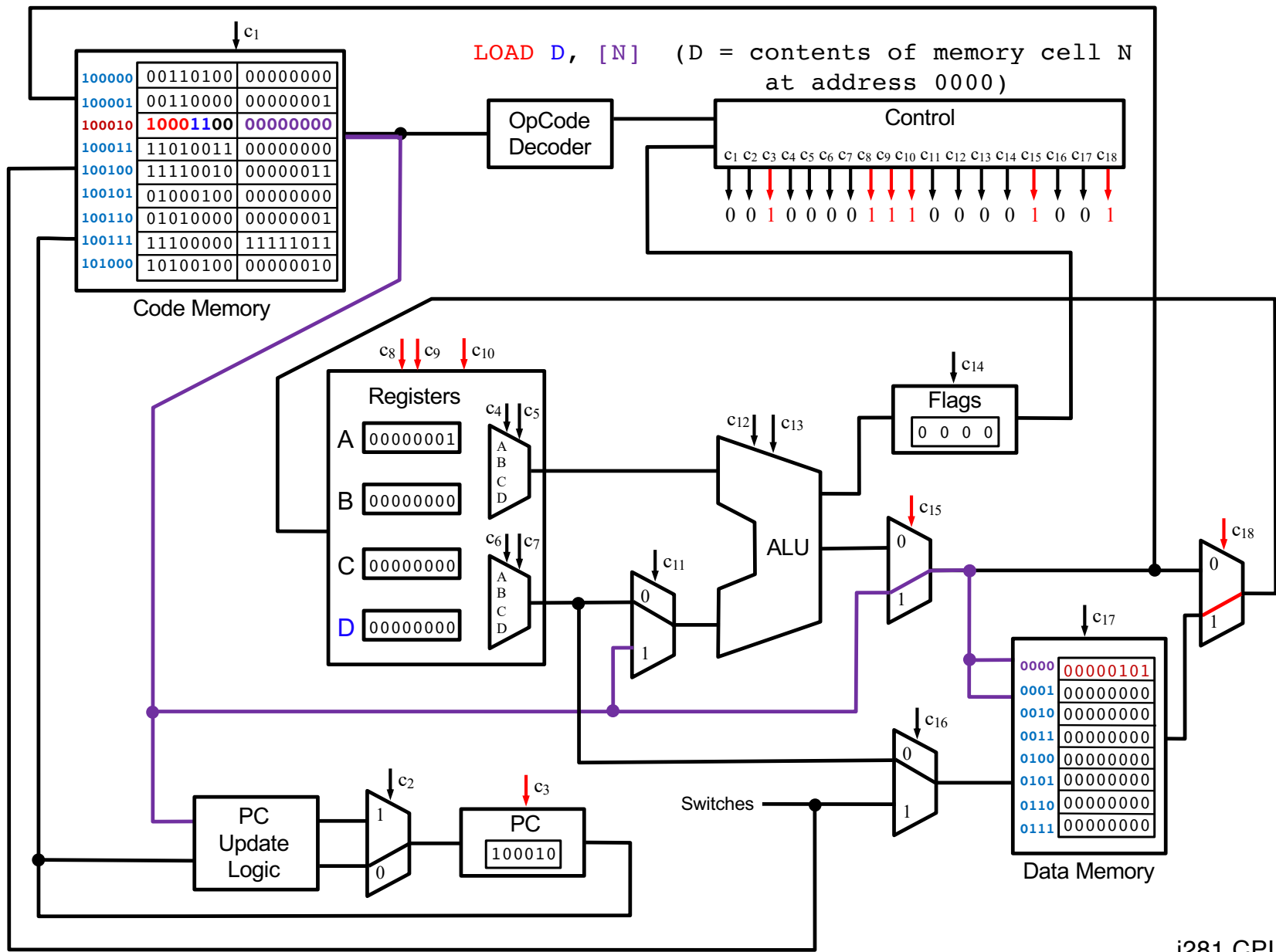
i281 CPU



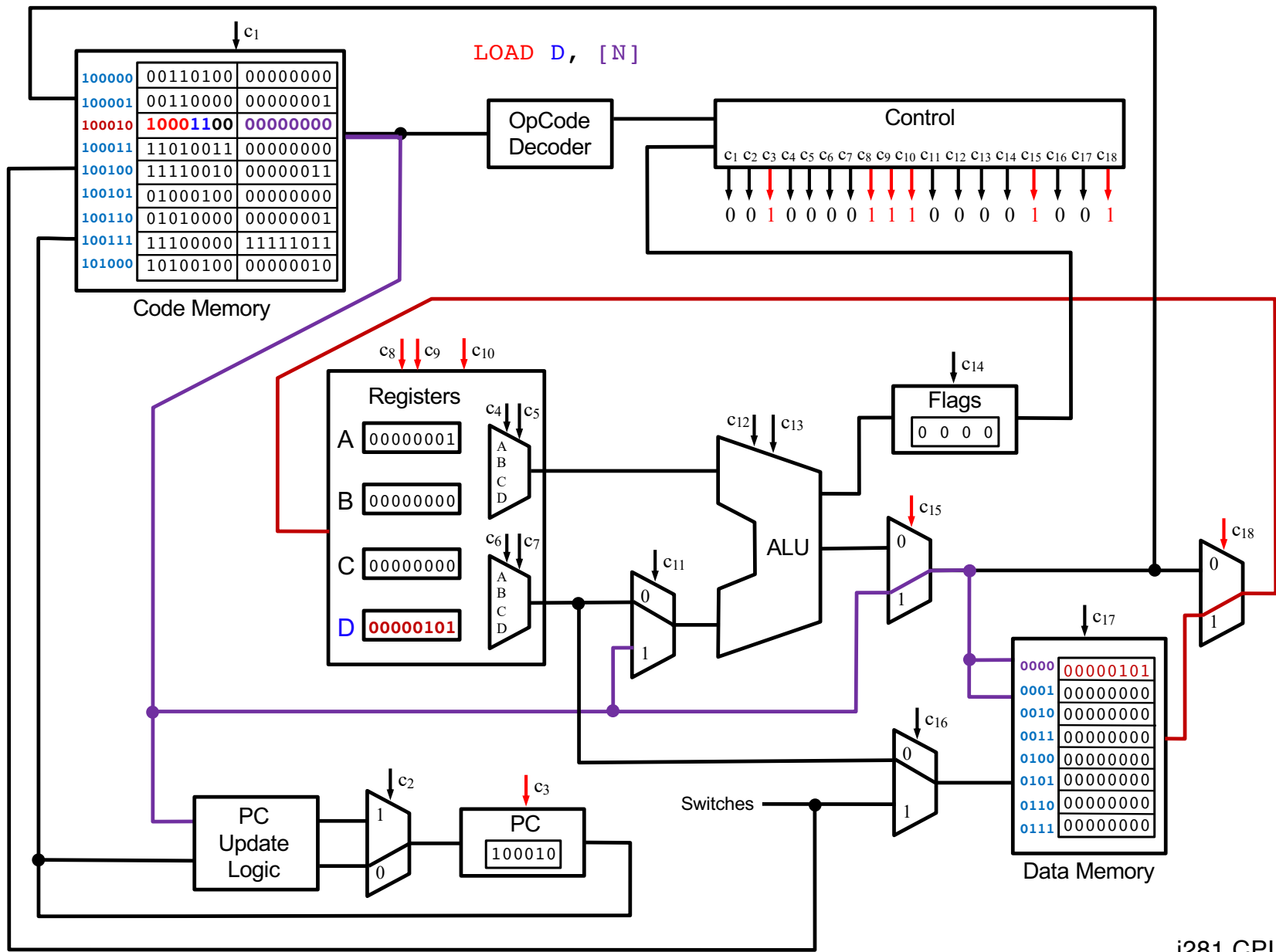
i281 CPU



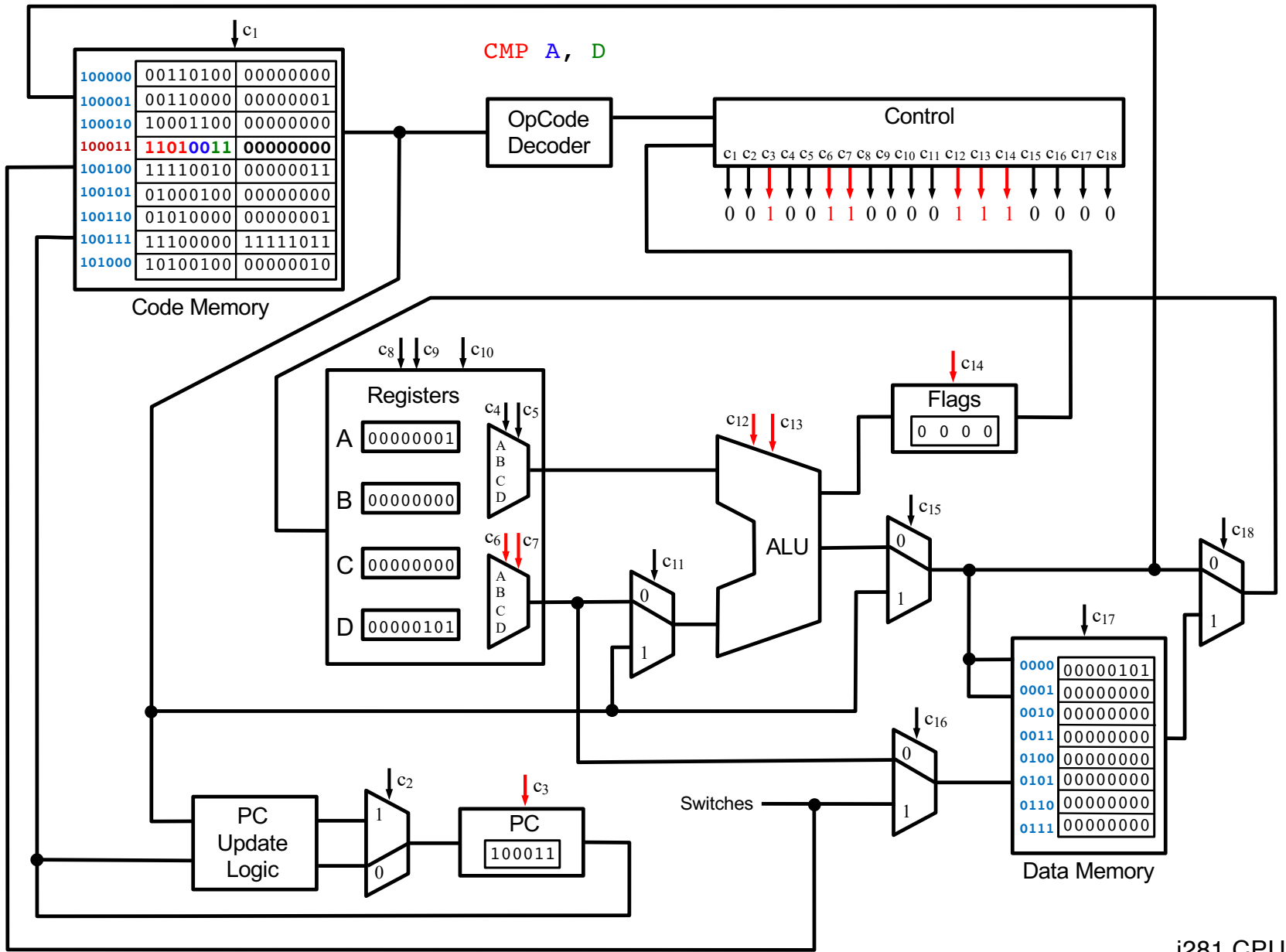
i281 CPU



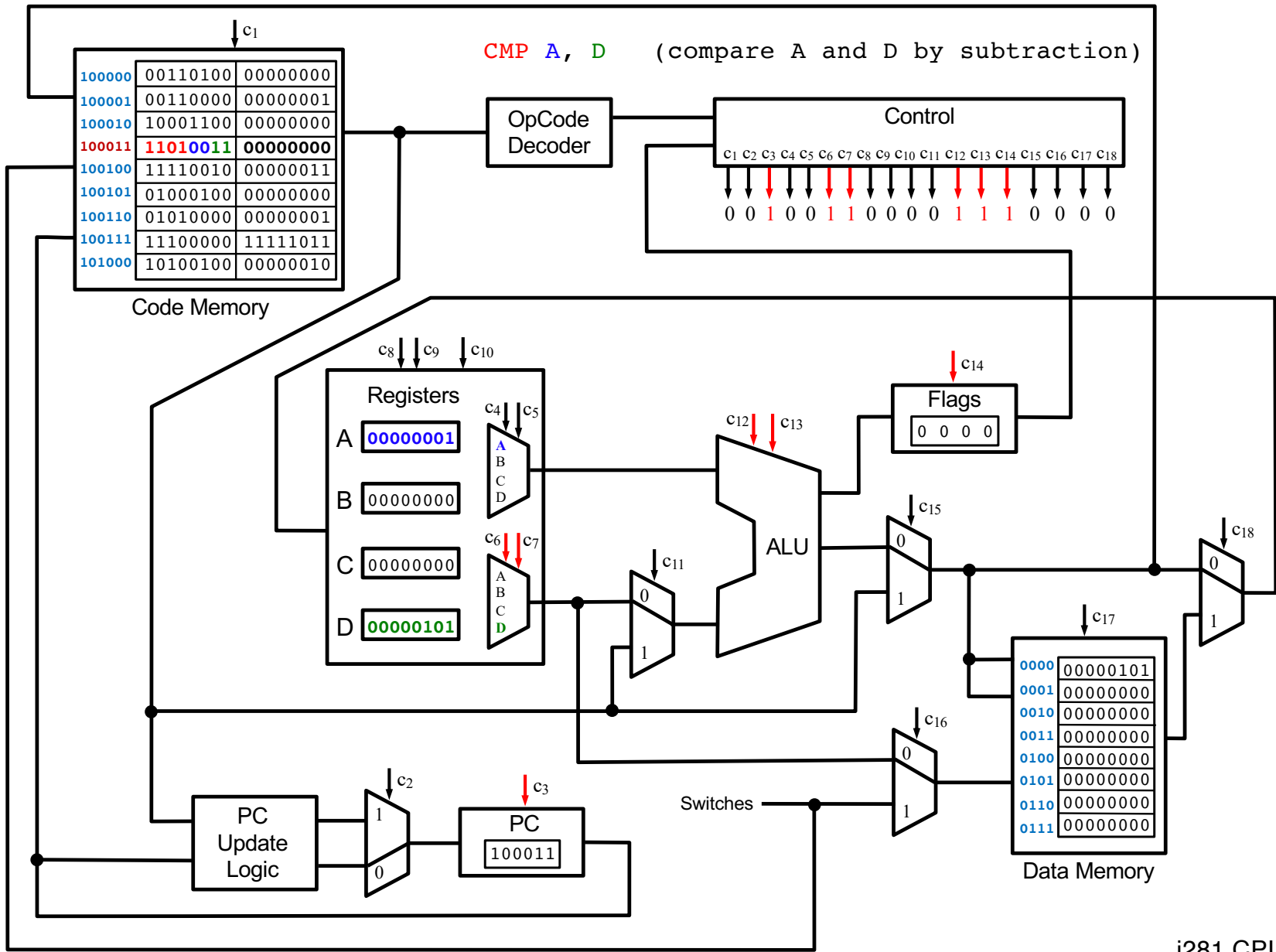
i281 CPU



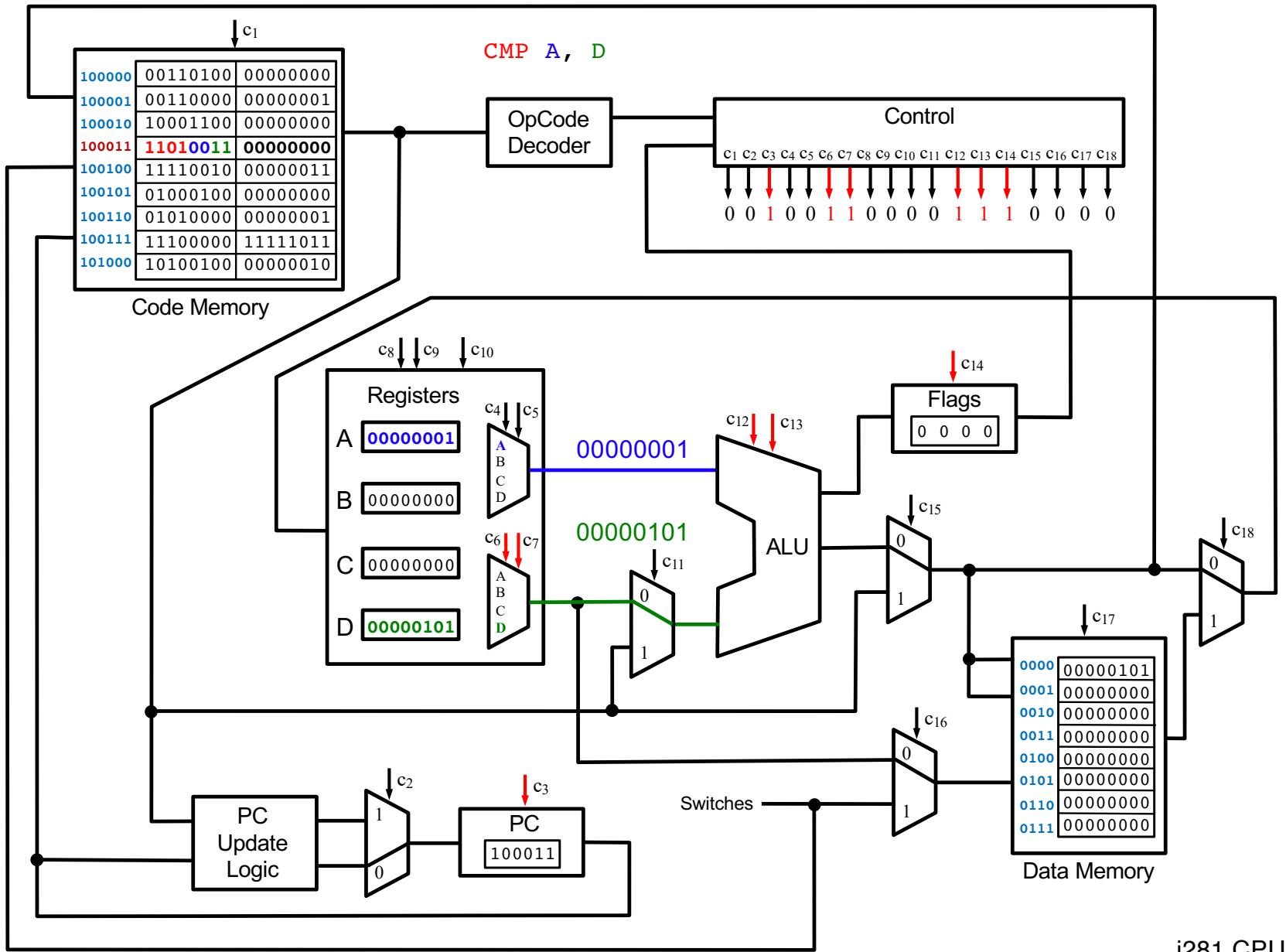
i281 CPU



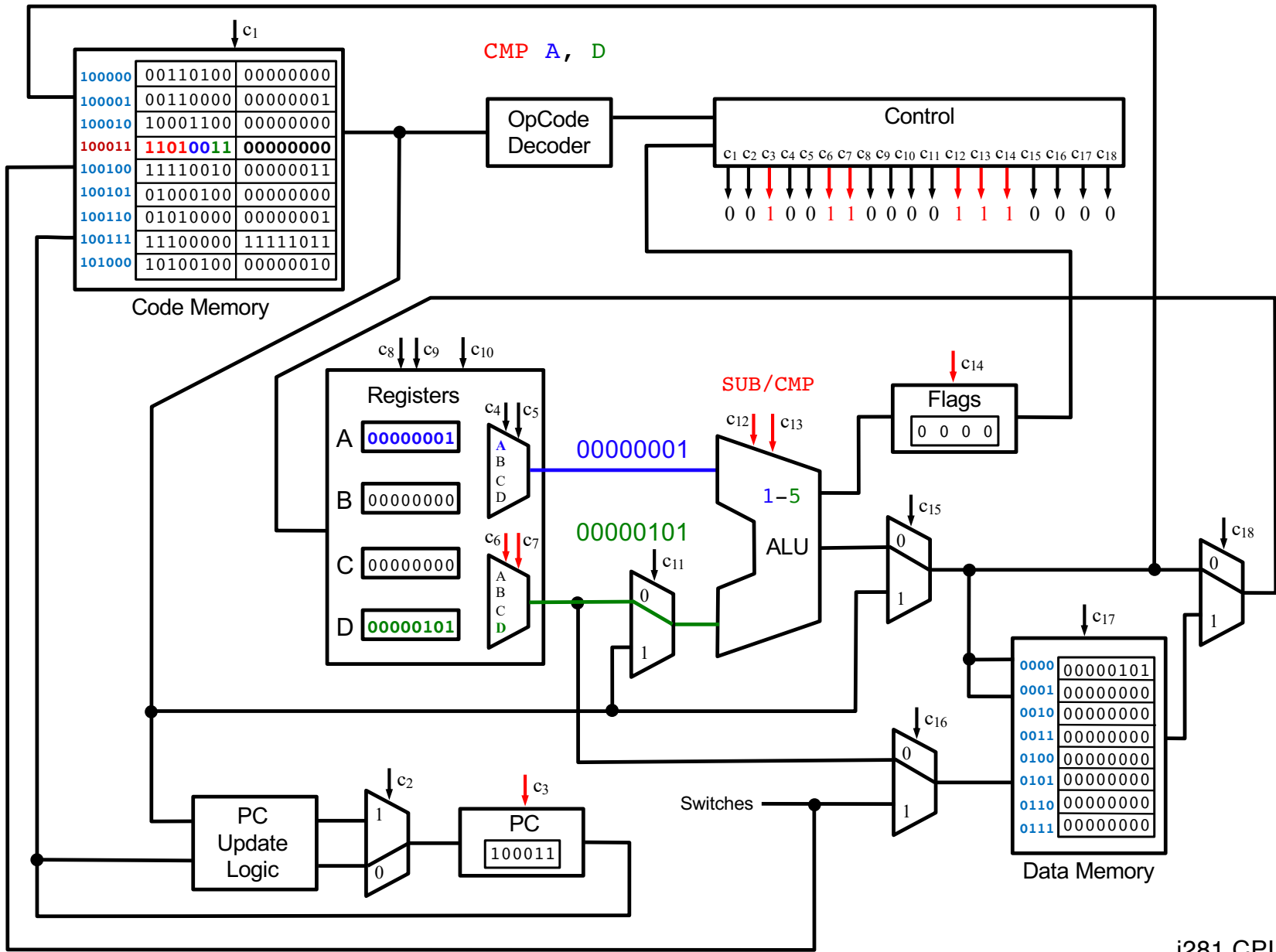
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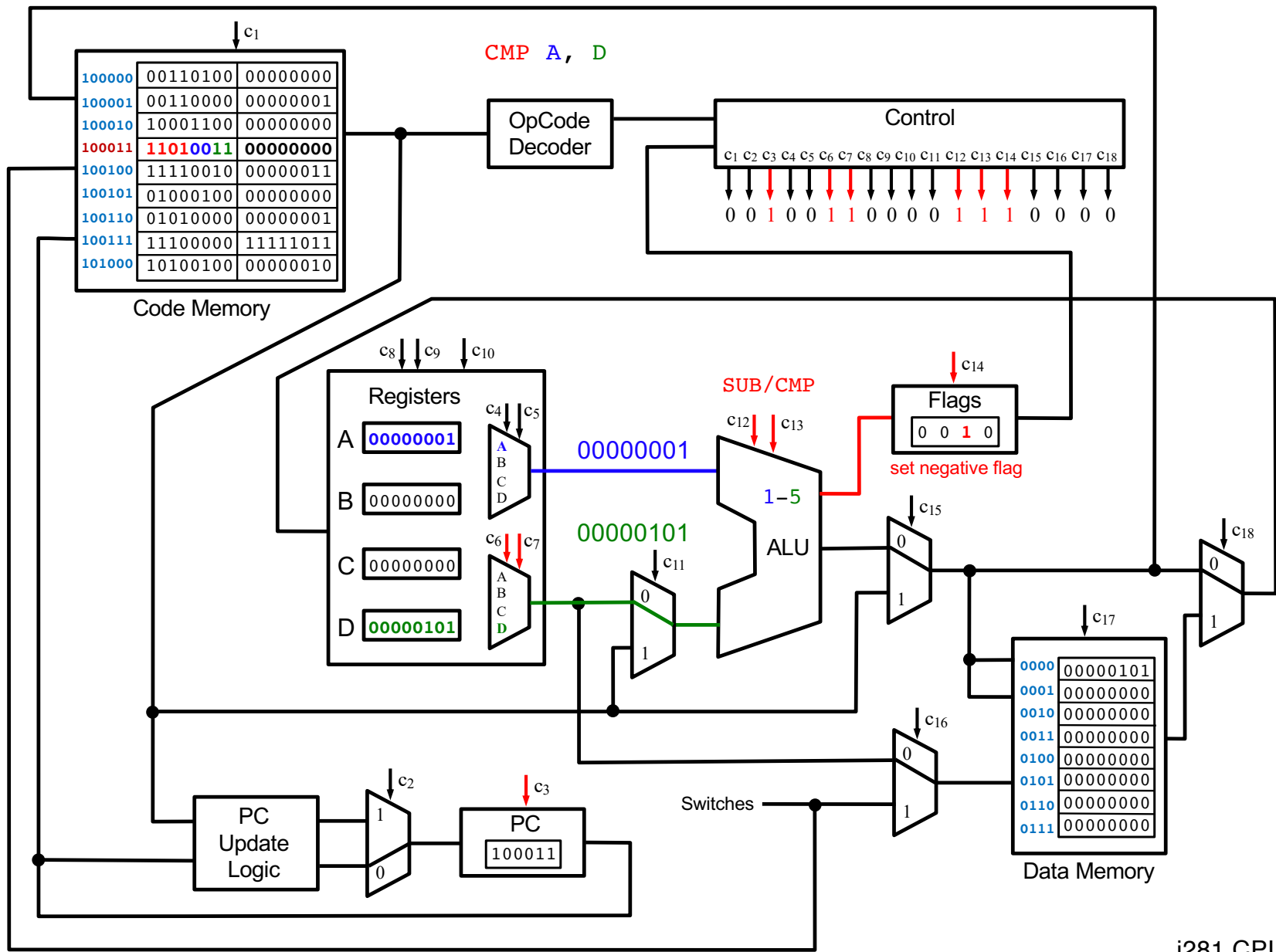
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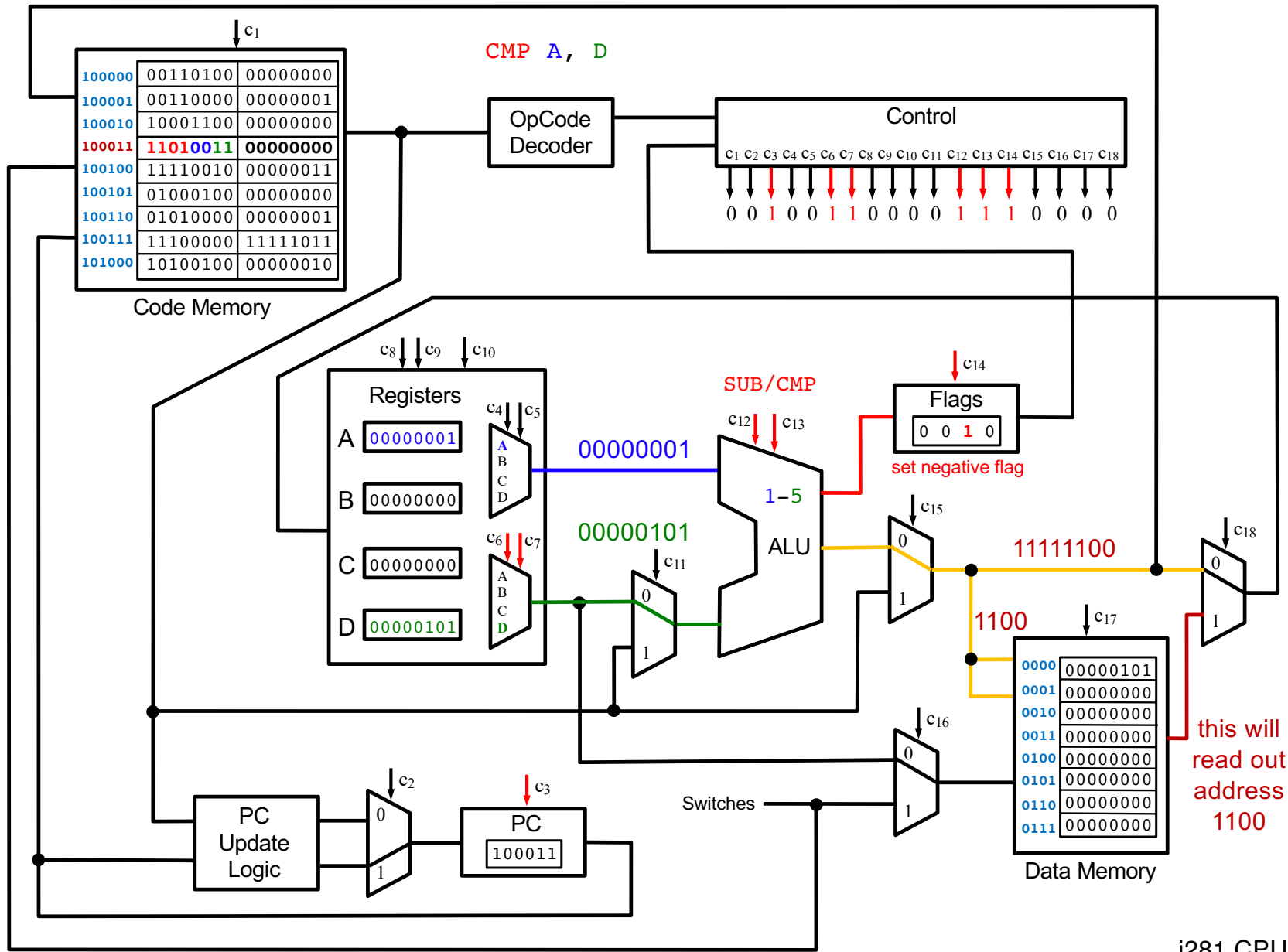
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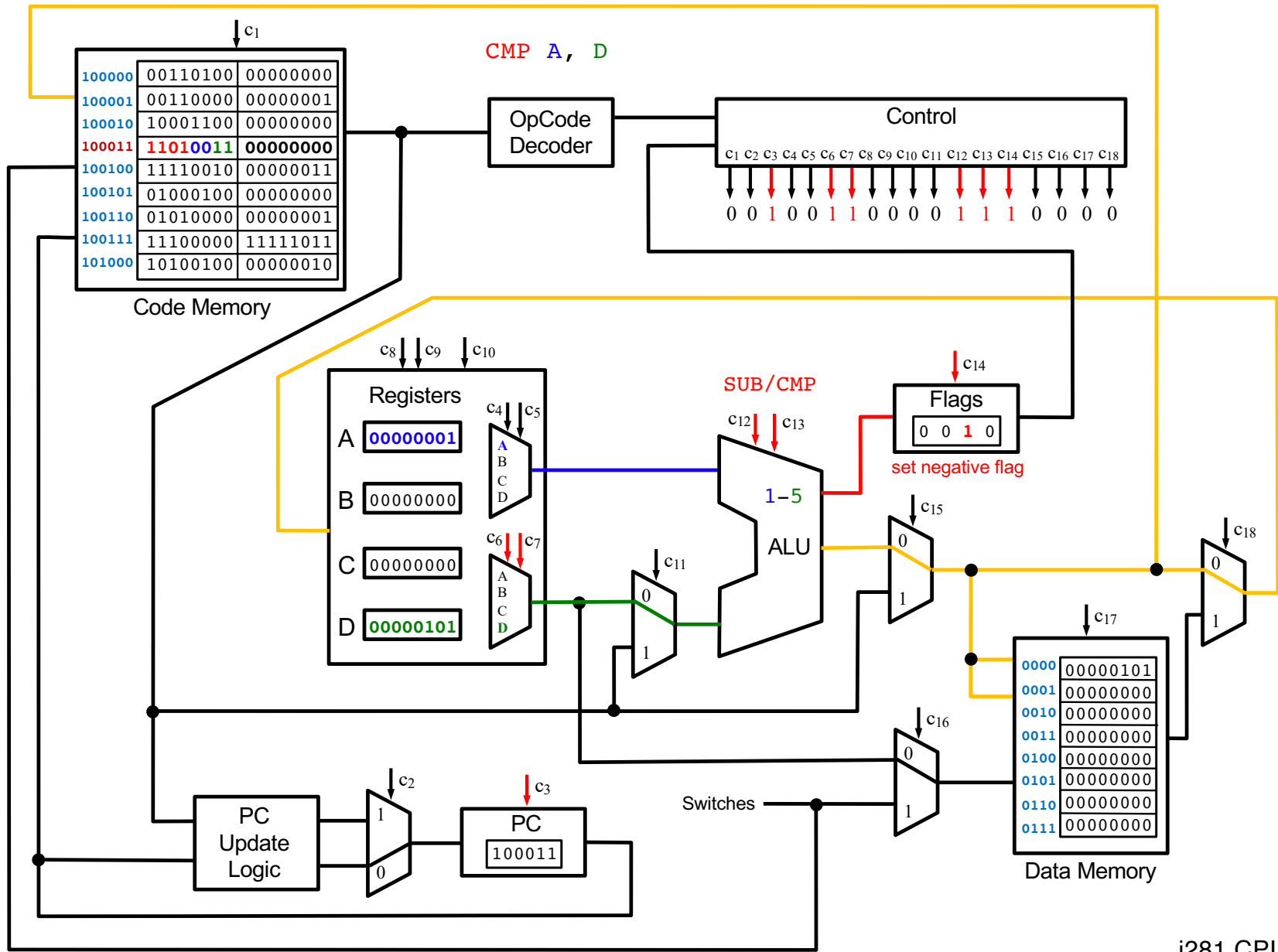
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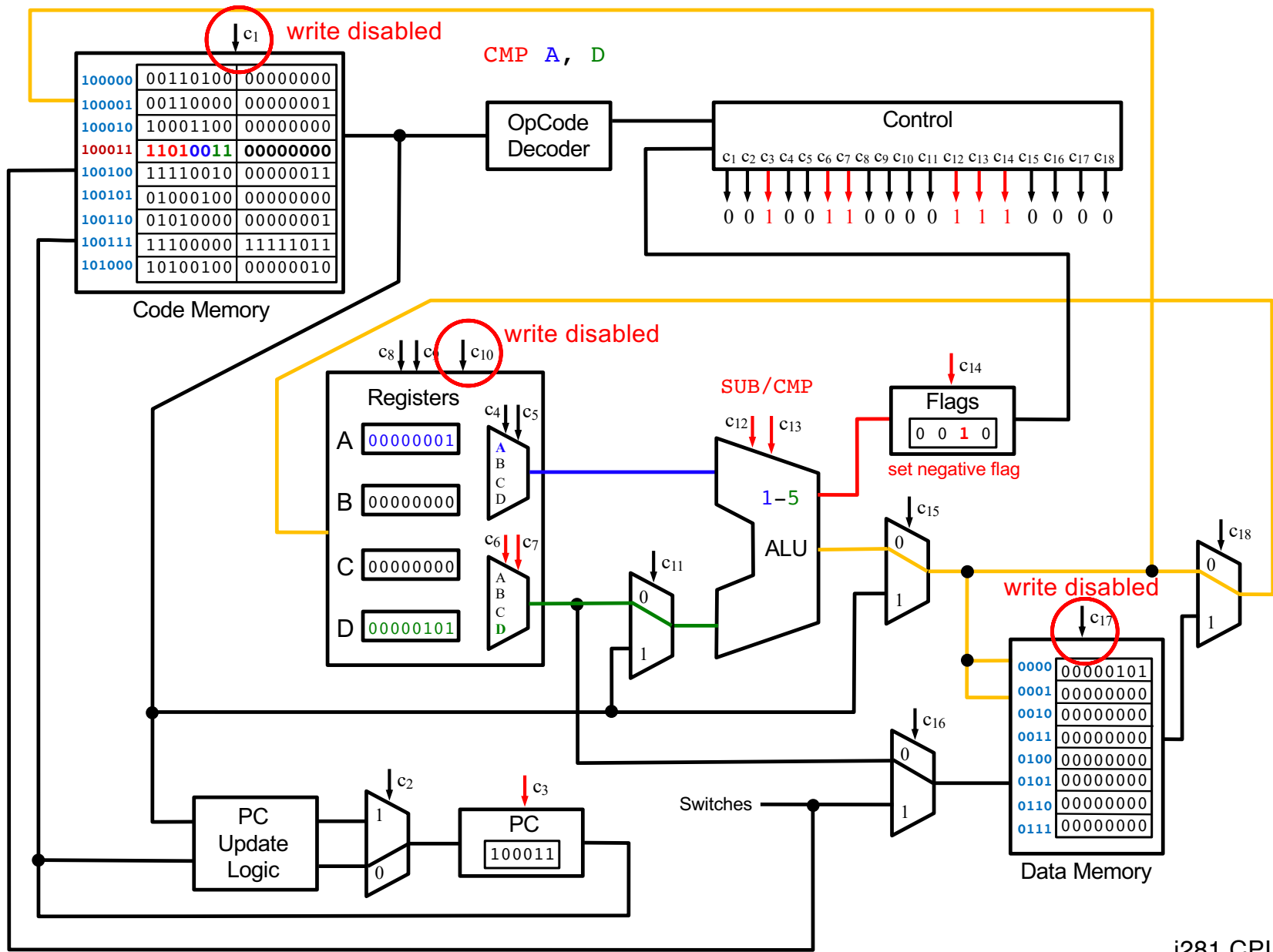
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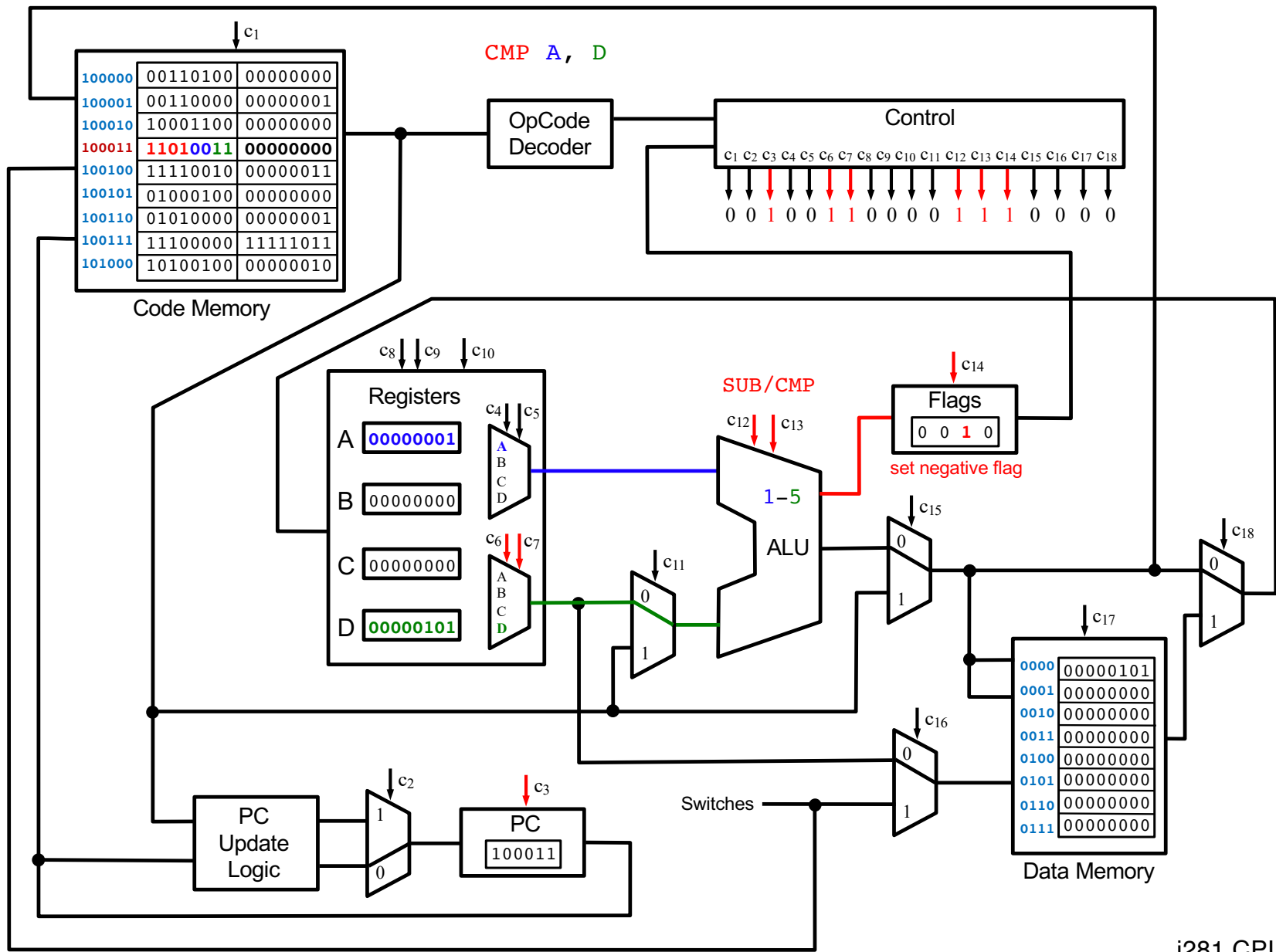
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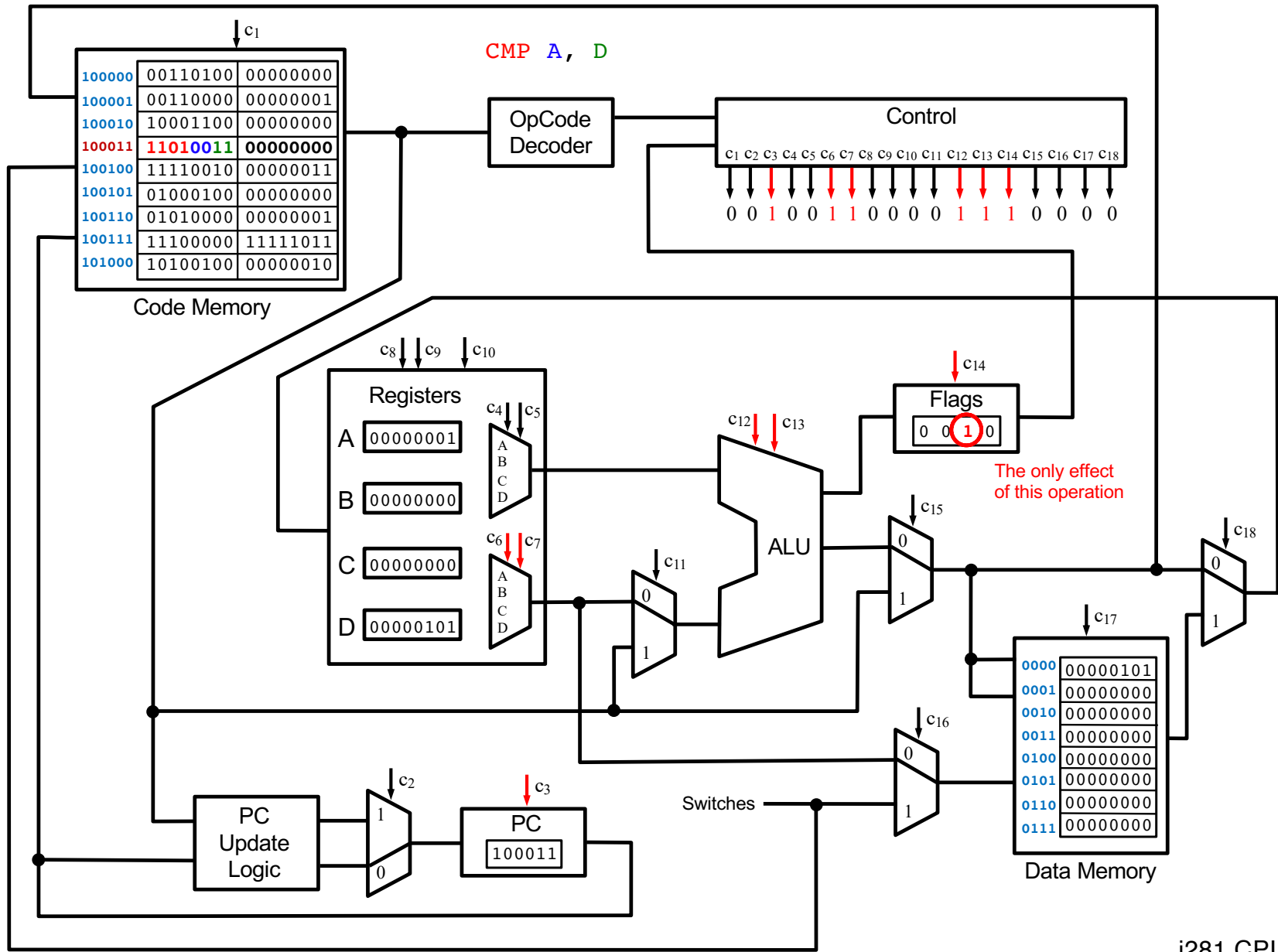
i281 CPU



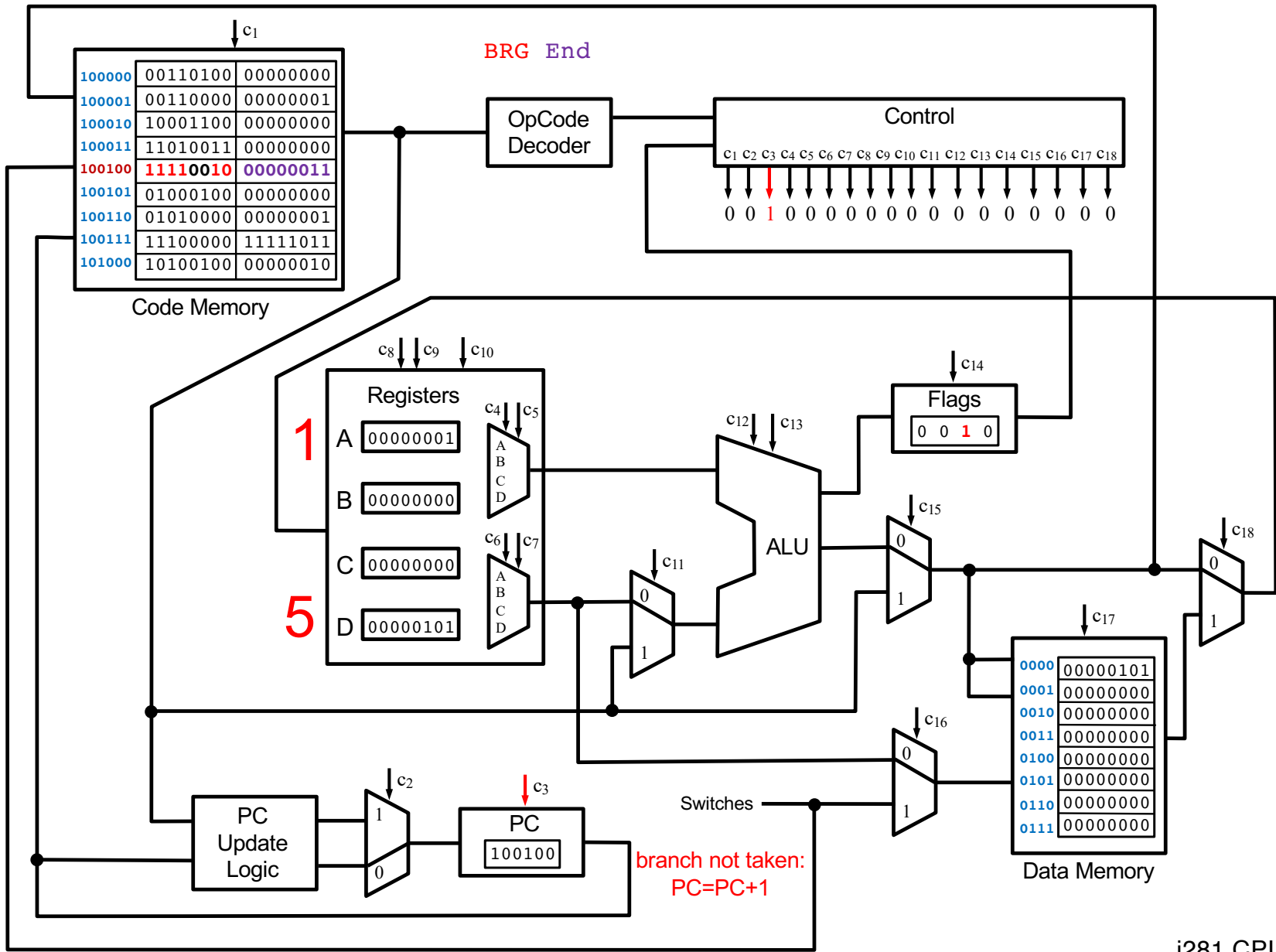
i281 CPU



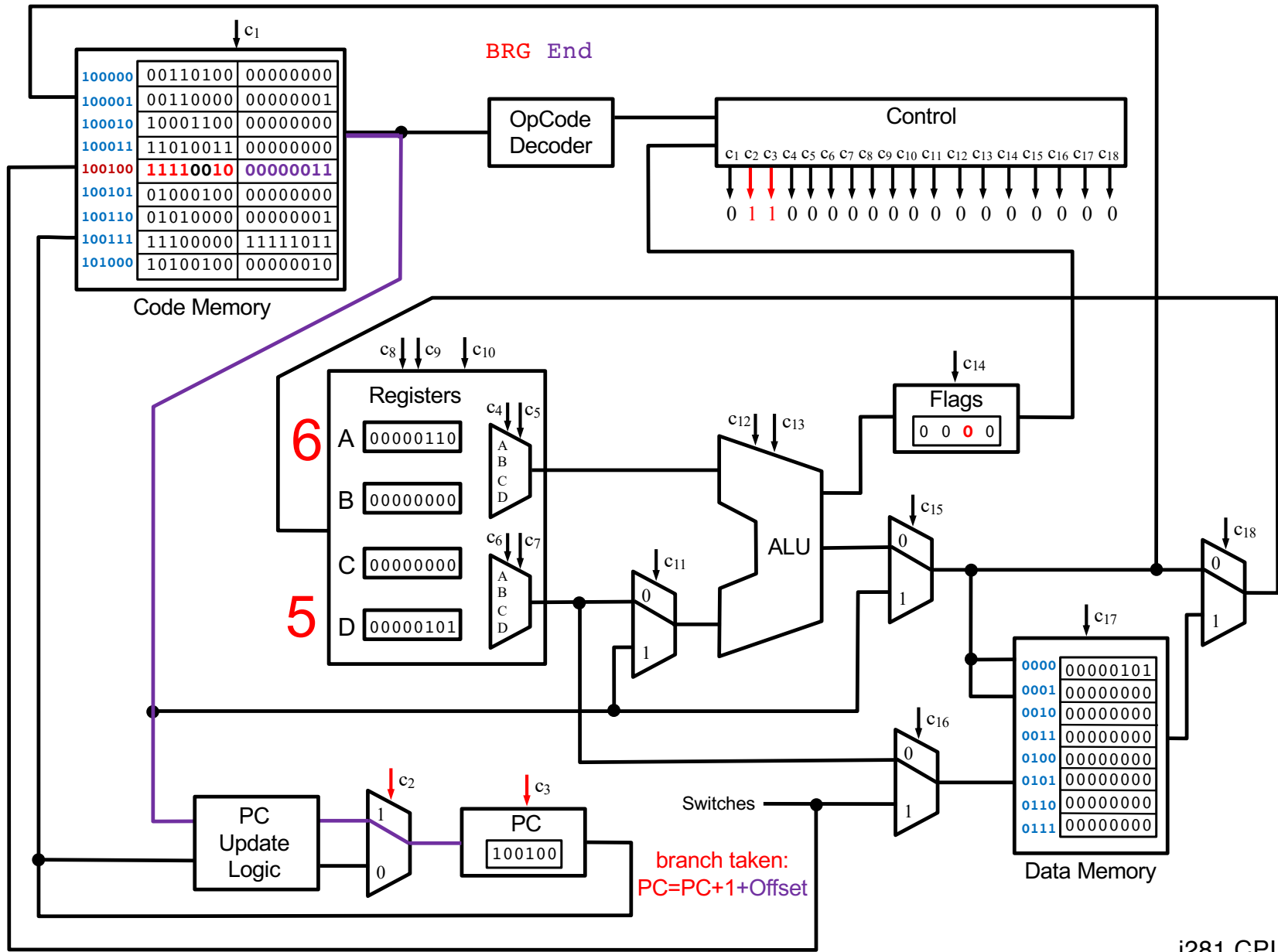
i281 CPU



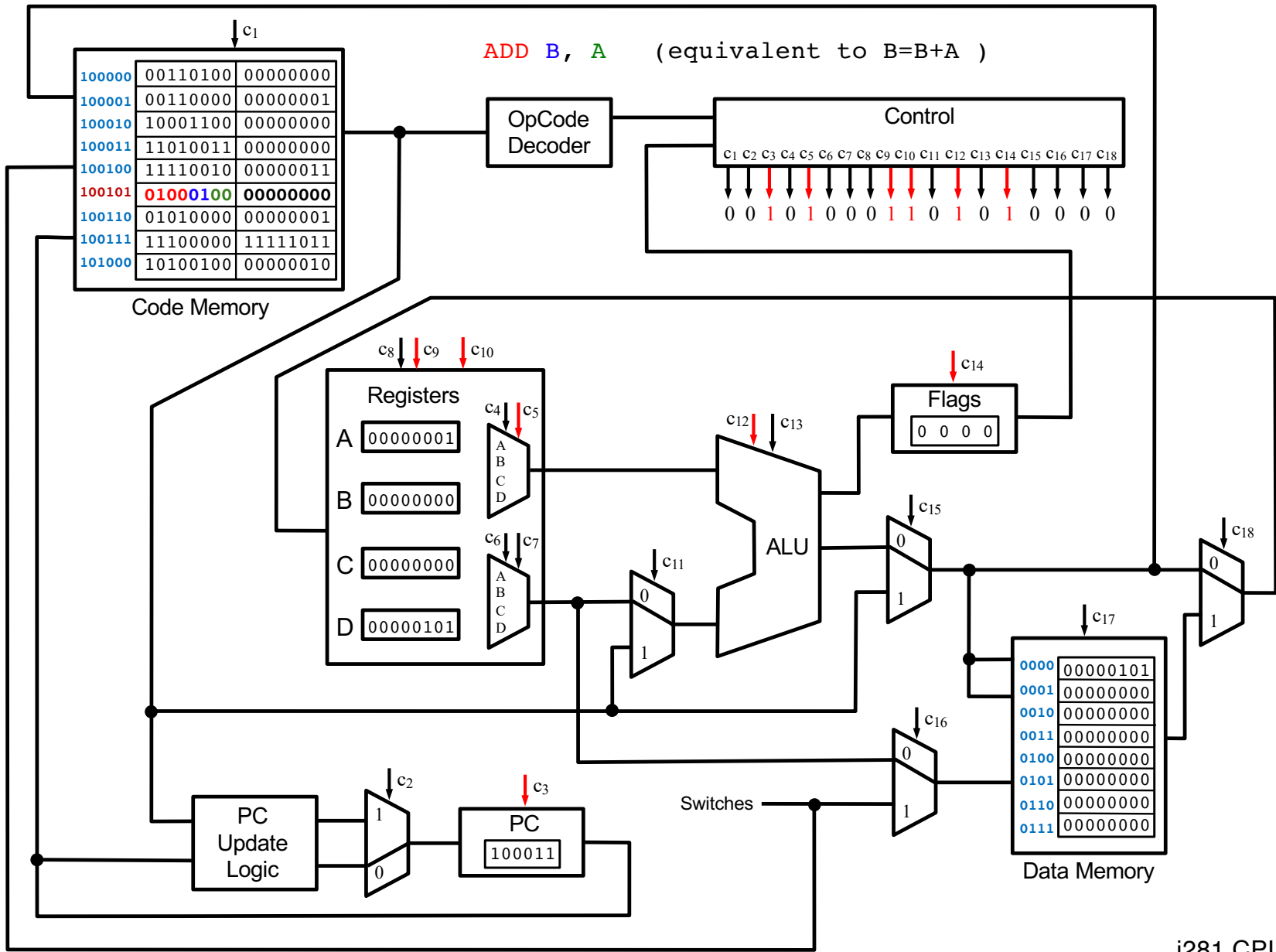
i281 CPU



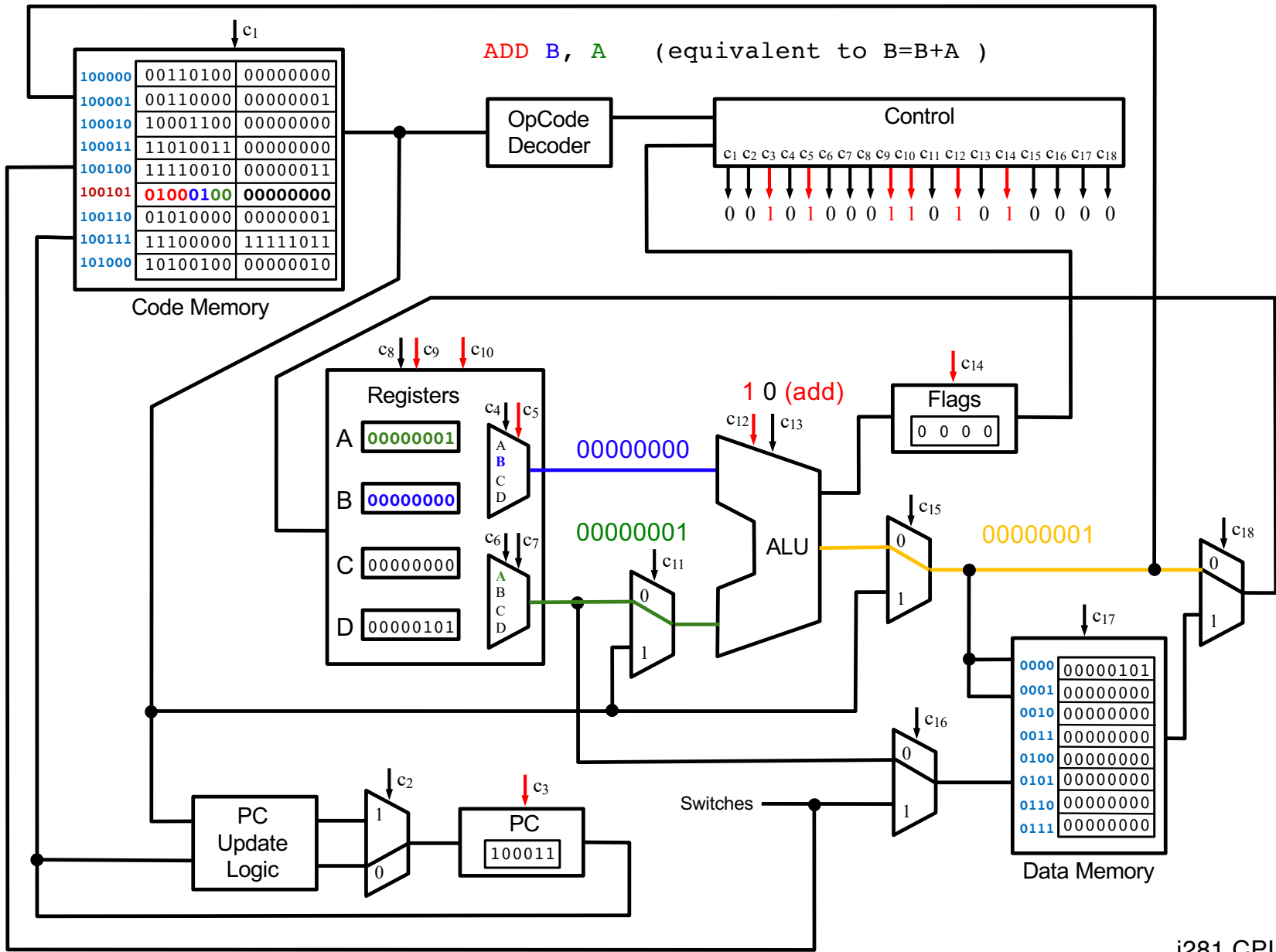
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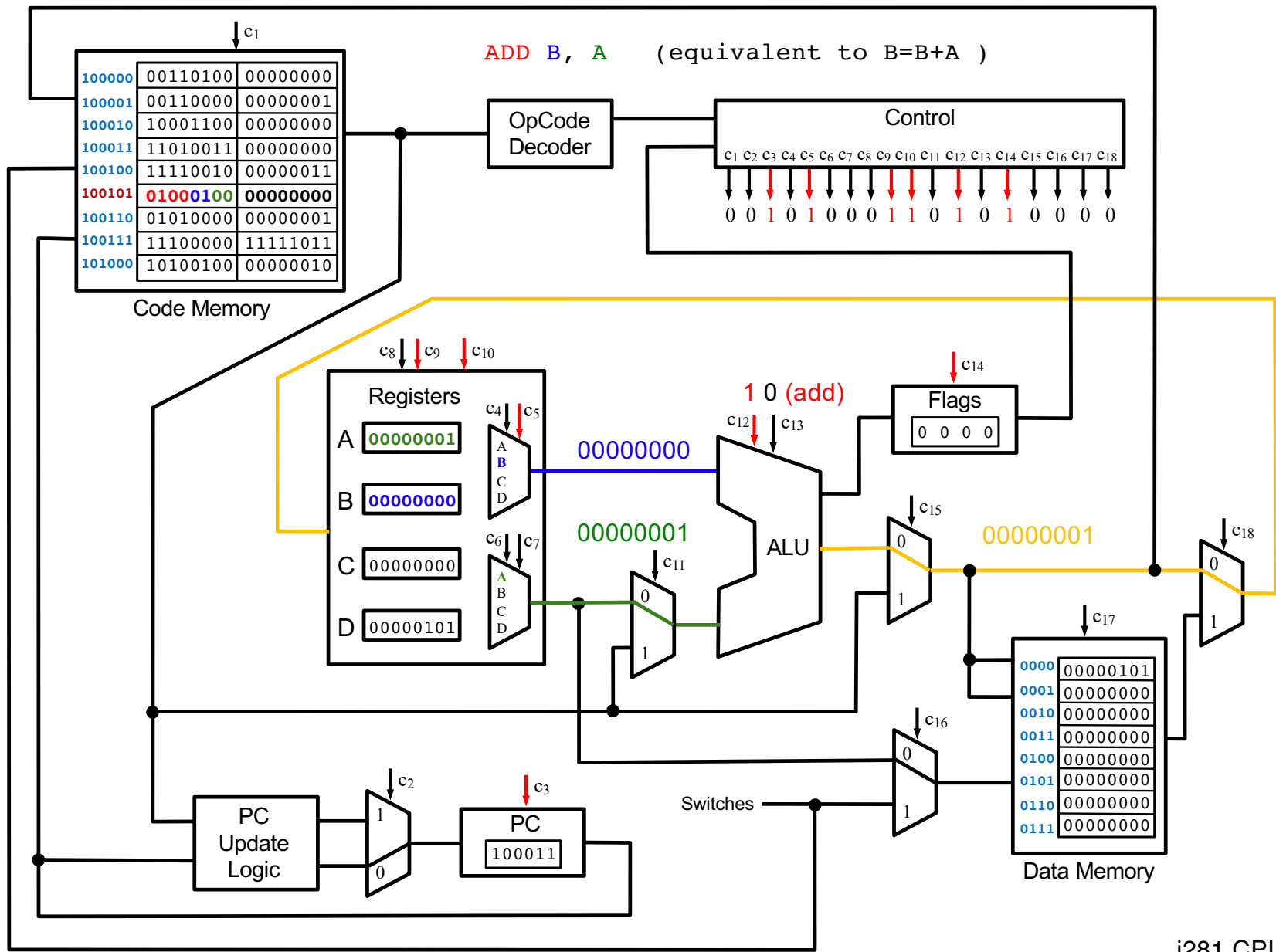
i281 CPU



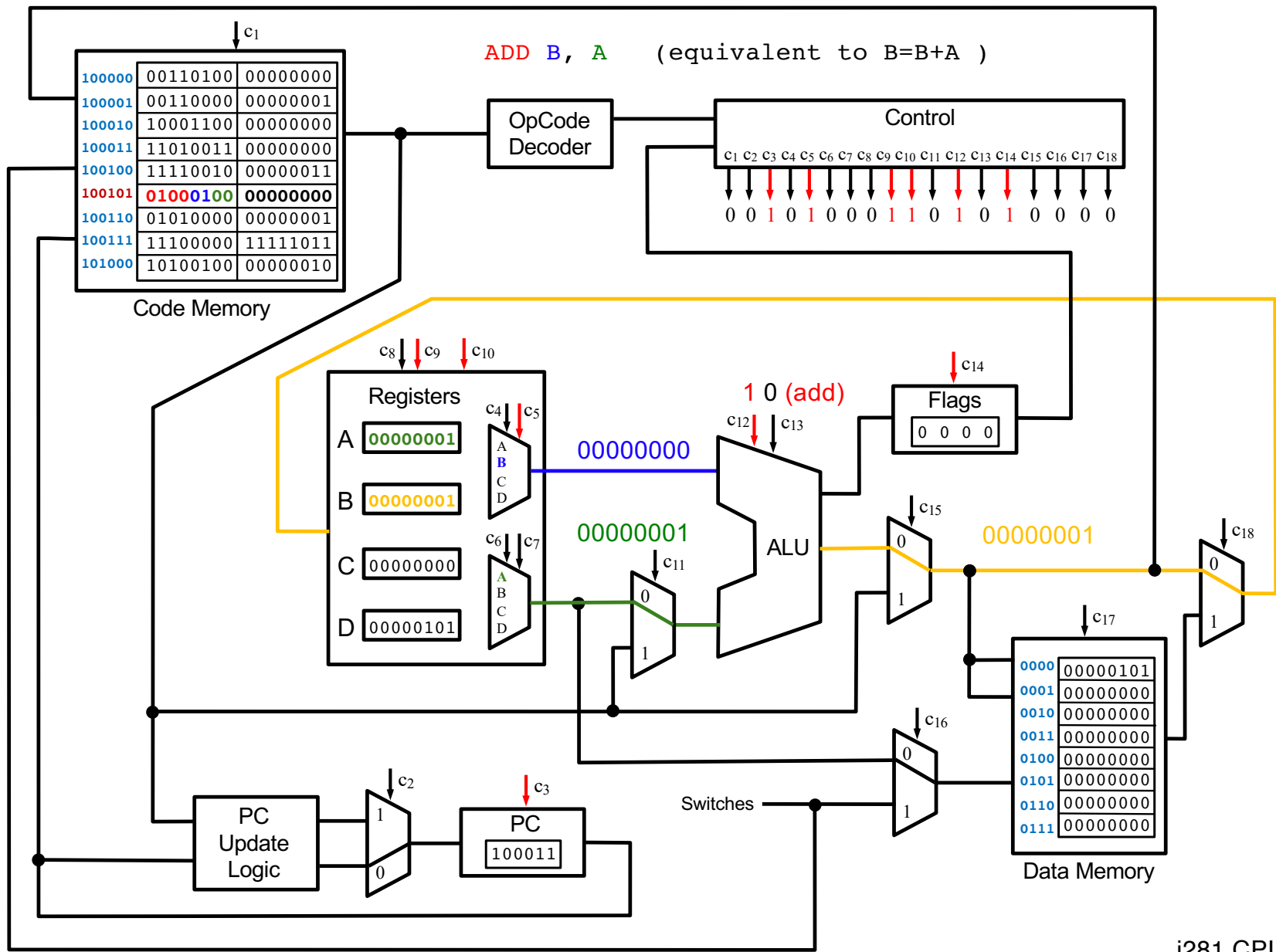
i281 CPU



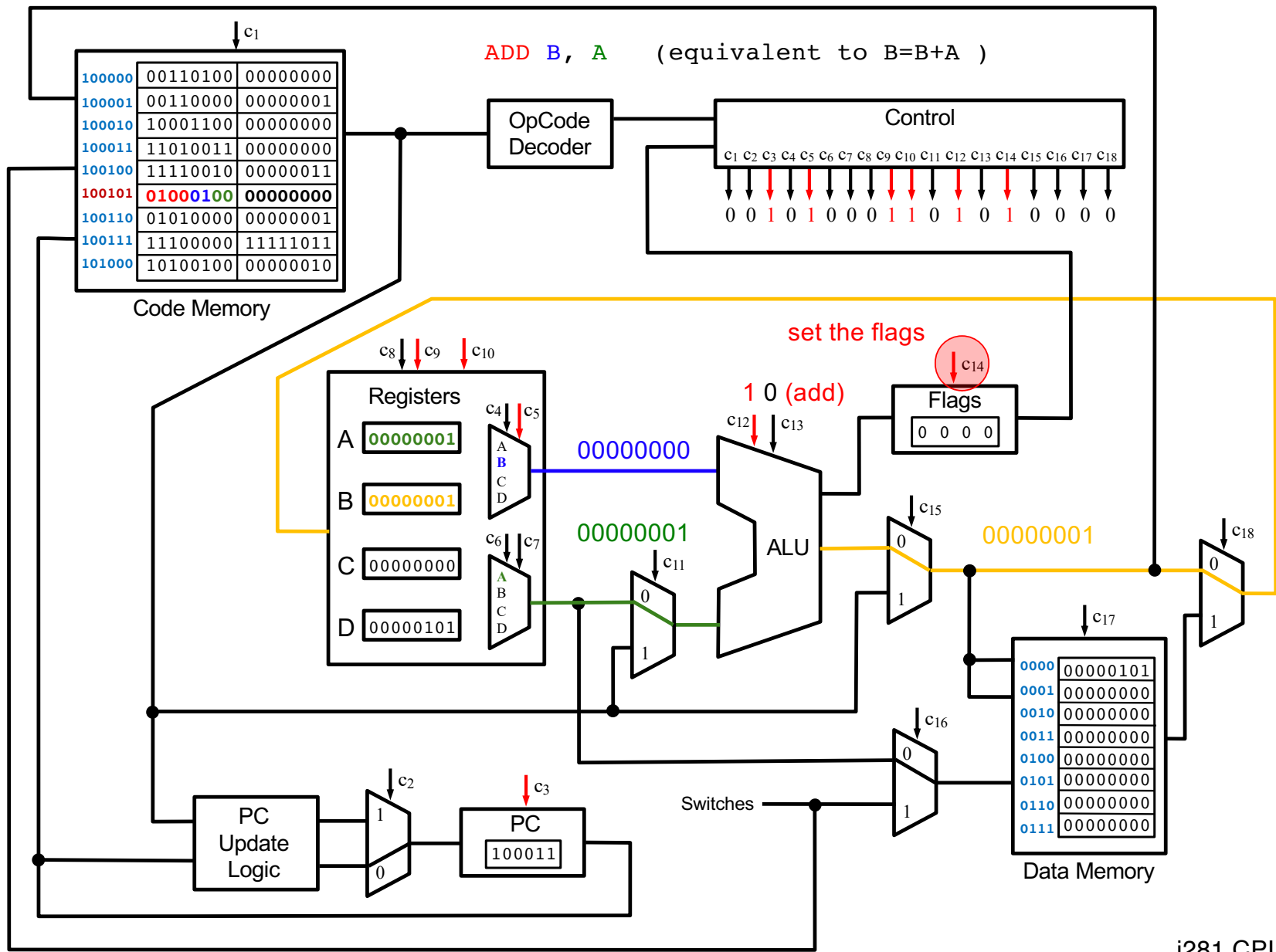
i281 CPU



i281 CPU



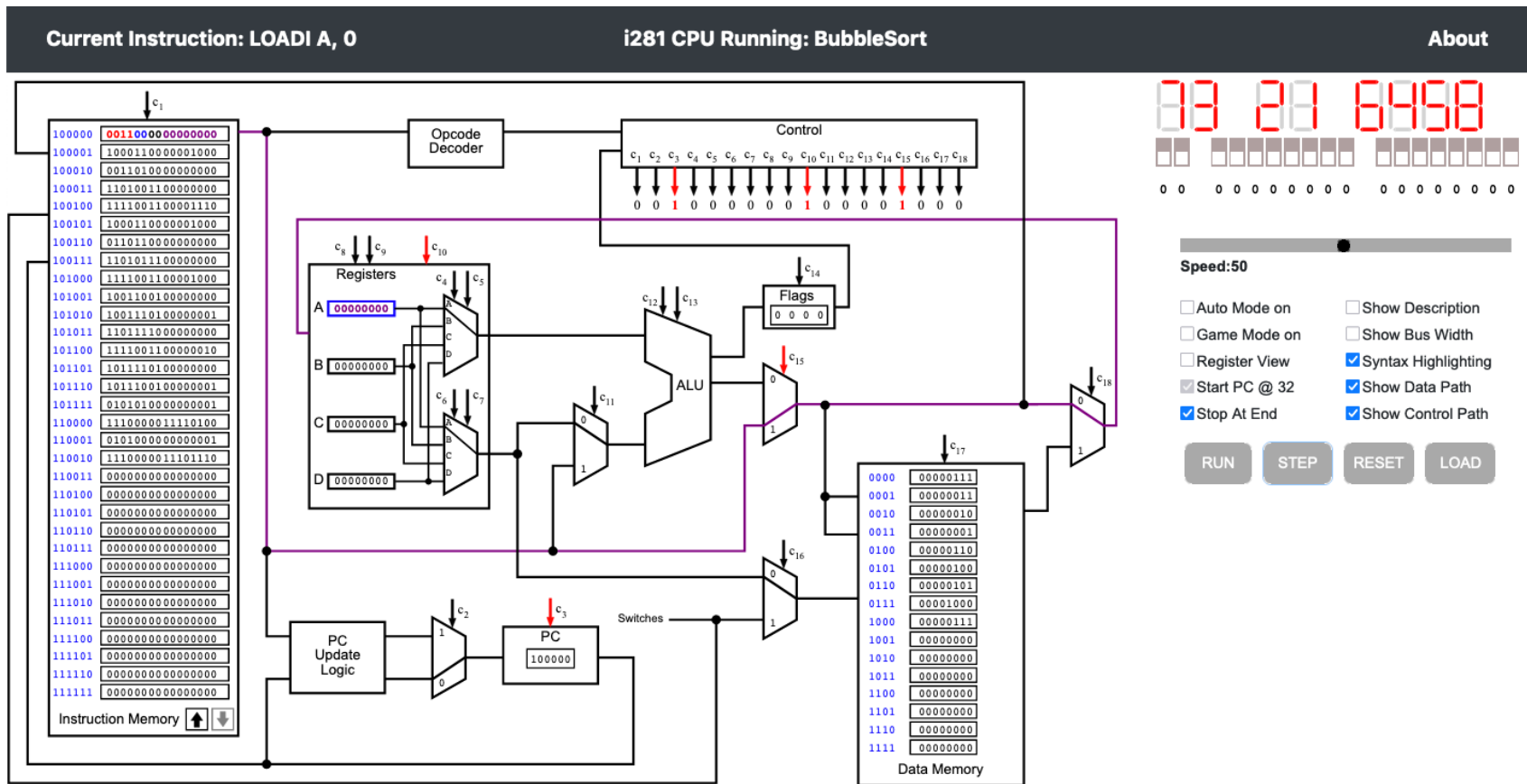
i281 CPU



i281 CPU

**For more examples
try the i281 simulator**

i281 Simulator



To try the simulator, go to the class web page and follow the link.

Questions?

THE END