



CprE 281: Digital Logic

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<http://www.ece.iastate.edu/~alexs/classes/>

NAND and NOR Logic Networks

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Iowa State University, Ames, IA
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Administrative Stuff

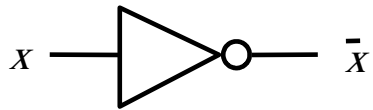
- **HW2 is due today**

Administrative Stuff

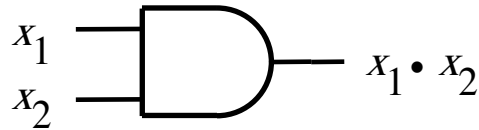
- **HW3 is out**
- **It is due on Monday Sep 16 @ 4pm.**
- **Please write clearly on the first page (in BLOCK CAPITAL letters) the following three things:**
 - **Your First and Last Name**
 - **Your Student ID Number**
 - **Your Lab Section Letter**
 - **Staple all of your pages together**

Quick Review

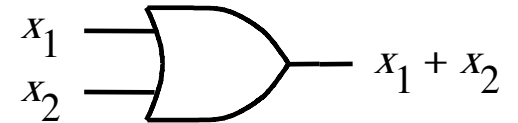
The Three Basic Logic Gates



NOT gate

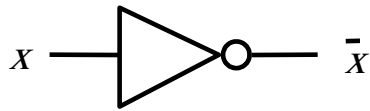


AND gate



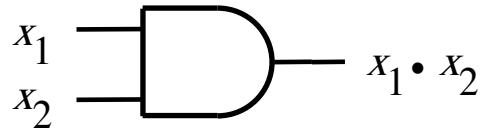
OR gate

Truth Table for NOT



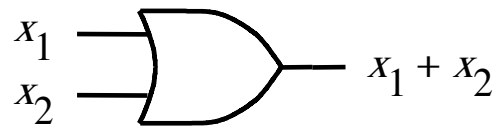
x	\bar{x}
0	1
1	0

Truth Table for AND



x_1	x_2	$x_1 \cdot x_2$
0	0	0
0	1	0
1	0	0
1	1	1

Truth Table for OR



x_1	x_2	$x_1 + x_2$
0	0	0
0	1	1
1	0	1
1	1	1

DeMorgan's Theorem

$$15a. \quad \overline{x \cdot y} = \bar{x} + \bar{y}$$

$$15b. \quad \overline{x + y} = \bar{x} \cdot \bar{y}$$

Synthesize the Following Function

x_1	x_2	$f(x_1, x_2)$
0	0	1
0	1	1
1	0	0
1	1	1

1) Split the function into a sum of 4 functions

x_1	x_2	$f(x_1, x_2)$		$f_{00}(x_1, x_2)$	$f_{01}(x_1, x_2)$	$f_{10}(x_1, x_2)$	$f_{11}(x_1, x_2)$
0	0	1		1	0	0	0
0	1	1		0	1	0	0
1	0	0		0	0	1	0
1	1	1		0	0	0	1

1) Split the function into a sum of 4 functions

x_1	x_2	$f(x_1, x_2)$	$f_{00}(x_1, x_2)$	$f_{01}(x_1, x_2)$	$f_{10}(x_1, x_2)$	$f_{11}(x_1, x_2)$
0	0	1	1	0	0	0
0	1	1	0	1	0	0
1	0	0	0	0	1	0
1	1	1	0	0	0	1

$$f(x_1, x_2) = 1 \cdot f_{00} + 1 \cdot f_{01} + 0 \cdot f_{10} + 1 \cdot f_{11}$$

2) Write the expressions for all four

x_1	x_2	$f(x_1, x_2)$	$f_{00}(x_1, x_2)$	$f_{01}(x_1, x_2)$	$f_{10}(x_1, x_2)$	$f_{11}(x_1, x_2)$
0	0	1	1	0	0	0
0	1	1	0	1	0	0
1	0	0	0	0	1	0
1	1	1	0	0	0	1

$$f(x_1, x_2) = \underbrace{1 \cdot f_{00}} + \underbrace{1 \cdot f_{01}} + \underbrace{0 \cdot f_{10}} + \underbrace{1 \cdot f_{11}}$$

2) Write the expressions for all four

x_1	x_2	$f(x_1, x_2)$	$f_{00}(x_1, x_2)$	$f_{01}(x_1, x_2)$	$f_{10}(x_1, x_2)$	$f_{11}(x_1, x_2)$
0	0	1	1	0	0	0
0	1	1	0	1	0	0
1	0	0	0	0	1	0
1	1	1	0	0	0	1

$$f(x_1, x_2) = \underbrace{1 \cdot f_{00}}_{\bar{x}_1 \bar{x}_2} + \underbrace{1 \cdot f_{01}}_{\bar{x}_1 x_2} + \underbrace{0 \cdot f_{10}}_0 + \underbrace{1 \cdot f_{11}}_{x_1 x_2}$$

3) Then just add them together

x_1	x_2	$f(x_1, x_2)$	$f_{00}(x_1, x_2)$	$f_{01}(x_1, x_2)$	$f_{10}(x_1, x_2)$	$f_{11}(x_1, x_2)$
0	0	1	1	0	0	0
0	1	1	0	1	0	0
1	0	0	0	0	1	0
1	1	1	0	0	0	1

$$f(x_1, x_2) = \underbrace{1 \cdot f_{00}} + \underbrace{1 \cdot f_{01}} + \underbrace{0 \cdot f_{10}} + \underbrace{1 \cdot f_{11}}$$

$$f(x_1, x_2) = \bar{x}_1 \bar{x}_2 + \bar{x}_1 x_2 + 0 + x_1 x_2$$

3) Then just add them together

x_1	x_2	$f(x_1, x_2)$		$f_{00}(x_1, x_2)$	$f_{01}(x_1, x_2)$	$f_{10}(x_1, x_2)$	$f_{11}(x_1, x_2)$
0	0	1		1	0	0	0
0	1	1		0	1	0	0
1	0	0		0	0	1	0
1	1	1		0	0	0	1

$$f(x_1, x_2) = \bar{x}_1\bar{x}_2 + \bar{x}_1x_2 + 0 + x_1x_2$$

Sum-of-Products Form

(uses the **ones** of the function)

Sum-of-Products Form

(for the AND logic function)

Row number	x_1	x_2	Minterm	$f(x_1, x_2)$
0	0	0	$m_0 = \bar{x}_1\bar{x}_2$	0
1	0	1	$m_1 = \bar{x}_1x_2$	0
2	1	0	$m_2 = x_1\bar{x}_2$	0
3	1	1	$m_3 = x_1x_2$	1

Sum-of-Products Form

(for the AND logic function)

Row number	x_1	x_2	Minterm	$f(x_1, x_2)$
0	0	0	$m_0 = \bar{x}_1\bar{x}_2$	0
1	0	1	$m_1 = \bar{x}_1x_2$	0
2	1	0	$m_2 = x_1\bar{x}_2$	0
3	1	1	$m_3 = x_1x_2$	1

Sum-of-Products Form

(for the AND logic function)

Row number	x_1	x_2	Minterm	$f(x_1, x_2)$
0	0	0	$m_0 = \bar{x}_1 \bar{x}_2$	0
1	0	1	$m_1 = \bar{x}_1 x_2$	0
2	1	0	$m_2 = x_1 \bar{x}_2$	0
3	1	1	$m_3 = x_1 x_2$	1

$$f(x_1, x_2) = m_3 = x_1 x_2$$

(In this case there is just one product and there is no need for a sum)

Another Example

Sum-of-Products Form

Row number	x_1	x_2	Minterm	$f(x_1, x_2)$
0	0	0	$m_0 = \bar{x}_1\bar{x}_2$	1
1	0	1	$m_1 = \bar{x}_1x_2$	1
2	1	0	$m_2 = x_1\bar{x}_2$	0
3	1	1	$m_3 = x_1x_2$	1

Sum-of-Products Form

Row number	x_1	x_2	Minterm	$f(x_1, x_2)$
0	0	0	$m_0 = \bar{x}_1\bar{x}_2$	1
1	0	1	$m_1 = \bar{x}_1x_2$	1
2	1	0	$m_2 = x_1\bar{x}_2$	0
3	1	1	$m_3 = x_1x_2$	1

Sum-of-Products Form

Row number	x_1	x_2	Minterm	$f(x_1, x_2)$
0	0	0	$m_0 = \bar{x}_1\bar{x}_2$	1
1	0	1	$m_1 = \bar{x}_1x_2$	1
2	1	0	$m_2 = x_1\bar{x}_2$	0
3	1	1	$m_3 = x_1x_2$	1

$$\begin{aligned}f &= m_0 \cdot 1 + m_1 \cdot 1 + m_2 \cdot 0 + m_3 \cdot 1 \\&= m_0 + m_1 + m_3 \\&= \bar{x}_1\bar{x}_2 + \bar{x}_1x_2 + x_1x_2\end{aligned}$$

Product-of-Sums Form

(uses the **zeros** of the function)

Product-of-Sums Form (for the OR logic function)

Row number	x_1	x_2	Maxterm	$f(x_1, x_2)$
0	0	0	$M_0 = x_1 + x_2$	0
1	0	1	$M_1 = x_1 + \bar{x}_2$	1
2	1	0	$M_2 = \bar{x}_1 + x_2$	1
3	1	1	$M_3 = \bar{x}_1 + \bar{x}_2$	1

Product-of-Sums Form (for the OR logic function)

Row number	x_1	x_2	Maxterm	$f(x_1, x_2)$
0	0	0	$M_0 = x_1 + x_2$	0
1	0	1	$M_1 = x_1 + \bar{x}_2$	1
2	1	0	$M_2 = \bar{x}_1 + x_2$	1
3	1	1	$M_3 = \bar{x}_1 + \bar{x}_2$	1

Product-of-Sums Form (for the OR logic function)

Row number	x_1	x_2	Maxterm	$f(x_1, x_2)$
0	0	0	$M_0 = x_1 + x_2$	0
1	0	1	$M_1 = x_1 + \bar{x}_2$	1
2	1	0	$M_2 = \bar{x}_1 + x_2$	1
3	1	1	$M_3 = \bar{x}_1 + \bar{x}_2$	1

$$f(x_1, x_2) = M_0 = x_1 + x_2$$

(In this case there is just one sum and there is no need for a product)

Another Example

Product-of-Sums Form (for this logic function)

Row number	x_1	x_2	Maxterm	$f(x_1, x_2)$
0	0	0	$M_0 = x_1 + x_2$	0
1	0	1	$M_1 = x_1 + \bar{x}_2$	1
2	1	0	$M_2 = \bar{x}_1 + x_2$	0
3	1	1	$M_3 = \bar{x}_1 + \bar{x}_2$	1

Product-of-Sums Form

(for this logic function)

Row number	x_1	x_2	Maxterm	$f(x_1, x_2)$
0	0	0	$M_0 = x_1 + x_2$	0
1	0	1	$M_1 = x_1 + \bar{x}_2$	1
2	1	0	$M_2 = \bar{x}_1 + x_2$	0
3	1	1	$M_3 = \bar{x}_1 + \bar{x}_2$	1

Product-of-Sums Form (for this logic function)

Row number	x_1	x_2	Maxterm	$f(x_1, x_2)$
0	0	0	$M_0 = x_1 + x_2$	0
1	0	1	$M_1 = x_1 + \bar{x}_2$	1
2	1	0	$M_2 = \bar{x}_1 + x_2$	0
3	1	1	$M_3 = \bar{x}_1 + \bar{x}_2$	1

$$f(x_1, x_2) = M_0 \cdot M_2 = (x_1 + x_2) \cdot (\bar{x}_1 + x_2)$$

More Examples

Example 2.10

Implement the function $f(x_1, x_2, x_3) = \sum m(2, 3, 4, 6, 7)$

Minterms and Maxterms (with three variables)

Row number	x_1	x_2	x_3	Minterm	Maxterm
0	0	0	0	$m_0 = \bar{x}_1\bar{x}_2\bar{x}_3$	$M_0 = x_1 + x_2 + x_3$
1	0	0	1	$m_1 = \bar{x}_1\bar{x}_2x_3$	$M_1 = x_1 + x_2 + \bar{x}_3$
2	0	1	0	$m_2 = \bar{x}_1x_2\bar{x}_3$	$M_2 = x_1 + \bar{x}_2 + x_3$
3	0	1	1	$m_3 = \bar{x}_1x_2x_3$	$M_3 = x_1 + \bar{x}_2 + \bar{x}_3$
4	1	0	0	$m_4 = x_1\bar{x}_2\bar{x}_3$	$M_4 = \bar{x}_1 + x_2 + x_3$
5	1	0	1	$m_5 = x_1\bar{x}_2x_3$	$M_5 = \bar{x}_1 + x_2 + \bar{x}_3$
6	1	1	0	$m_6 = x_1x_2\bar{x}_3$	$M_6 = \bar{x}_1 + \bar{x}_2 + x_3$
7	1	1	1	$m_7 = x_1x_2x_3$	$M_7 = \bar{x}_1 + \bar{x}_2 + \bar{x}_3$

Minterms and Maxterms (with three variables)

Row number	x_1	x_2	x_3	Minterm	Maxterm
0	0	0	0	$m_0 = \bar{x}_1\bar{x}_2\bar{x}_3$	$M_0 = x_1 + x_2 + x_3$
1	0	0	1	$m_1 = \bar{x}_1\bar{x}_2x_3$	$M_1 = x_1 + x_2 + \bar{x}_3$
2	0	1	0	$m_2 = \bar{x}_1x_2\bar{x}_3$	$M_2 = x_1 + \bar{x}_2 + x_3$
3	0	1	1	$m_3 = \bar{x}_1x_2x_3$	$M_3 = x_1 + \bar{x}_2 + \bar{x}_3$
4	1	0	0	$m_4 = x_1\bar{x}_2\bar{x}_3$	$M_4 = \bar{x}_1 + x_2 + x_3$
5	1	0	1	$m_5 = x_1\bar{x}_2x_3$	$M_5 = \bar{x}_1 + x_2 + \bar{x}_3$
6	1	1	0	$m_6 = x_1x_2\bar{x}_3$	$M_6 = \bar{x}_1 + \bar{x}_2 + x_3$
7	1	1	1	$m_7 = x_1x_2x_3$	$M_7 = \bar{x}_1 + \bar{x}_2 + \bar{x}_3$

$$f(x_1, x_2, x_3) = \sum m(2, 3, 4, 6, 7)$$

- **The SOP expression is:**

$$\begin{aligned} f &= m_2 + m_3 + m_4 + m_6 + m_7 \\ &= \bar{x}_1 x_2 \bar{x}_3 + \bar{x}_1 x_2 x_3 + x_1 \bar{x}_2 \bar{x}_3 + x_1 x_2 \bar{x}_3 + x_1 x_2 x_3 \end{aligned}$$

- **This could be simplified as follows:**

$$\begin{aligned} f &= \bar{x}_1 x_2 (\bar{x}_3 + x_3) + x_1 (\bar{x}_2 + x_2) \bar{x}_3 + x_1 x_2 (\bar{x}_3 + x_3) \\ &= \bar{x}_1 x_2 + x_1 \bar{x}_3 + x_1 x_2 \\ &= (\bar{x}_1 + x_1) x_2 + x_1 \bar{x}_3 \\ &= x_2 + x_1 \bar{x}_3 \end{aligned}$$

Example 2.12

Implement the function $f(x_1, x_2, x_3) = \prod M(0, 1, 5)$,

which is equivalent to $f(x_1, x_2, x_3) = \sum m(2, 3, 4, 6, 7)$

Minterms and Maxterms (with three variables)

Row number	x_1	x_2	x_3	Minterm	Maxterm
0	0	0	0	$m_0 = \bar{x}_1\bar{x}_2\bar{x}_3$	$M_0 = x_1 + x_2 + x_3$
1	0	0	1	$m_1 = \bar{x}_1\bar{x}_2x_3$	$M_1 = x_1 + x_2 + \bar{x}_3$
2	0	1	0	$m_2 = \bar{x}_1x_2\bar{x}_3$	$M_2 = x_1 + \bar{x}_2 + x_3$
3	0	1	1	$m_3 = \bar{x}_1x_2x_3$	$M_3 = x_1 + \bar{x}_2 + \bar{x}_3$
4	1	0	0	$m_4 = x_1\bar{x}_2\bar{x}_3$	$M_4 = \bar{x}_1 + x_2 + x_3$
5	1	0	1	$m_5 = x_1\bar{x}_2x_3$	$M_5 = \bar{x}_1 + x_2 + \bar{x}_3$
6	1	1	0	$m_6 = x_1x_2\bar{x}_3$	$M_6 = \bar{x}_1 + \bar{x}_2 + x_3$
7	1	1	1	$m_7 = x_1x_2x_3$	$M_7 = \bar{x}_1 + \bar{x}_2 + \bar{x}_3$

$$f(x_1, x_2, x_3) = \Pi M(0, 1, 5)$$

- **The POS expression is:**

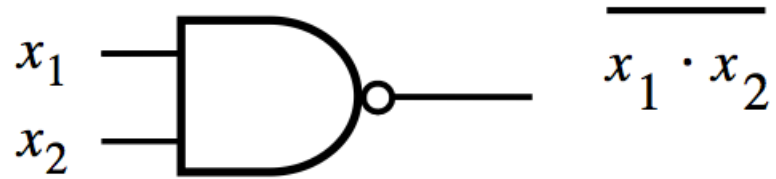
$$\begin{aligned} f &= M_0 \cdot M_1 \cdot M_5 \\ &= (x_1 + x_2 + x_3)(x_1 + x_2 + \bar{x}_3)(\bar{x}_1 + x_2 + \bar{x}_3) \end{aligned}$$

- **This could be simplified as follows:**

$$\begin{aligned} f &= (x_1 + x_2 + x_3)(x_1 + x_2 + \bar{x}_3)(x_1 + x_2 + \bar{x}_3)(\bar{x}_1 + x_2 + \bar{x}_3) \\ &= ((x_1 + x_2) + x_3)((x_1 + x_2) + \bar{x}_3)(x_1 + (x_2 + \bar{x}_3))(\bar{x}_1 + (x_2 + \bar{x}_3)) \\ &= ((x_1 + x_2) + x_3\bar{x}_3)(x_1\bar{x}_1 + (x_2 + \bar{x}_3)) \\ &= (x_1 + x_2)(x_2 + \bar{x}_3) \end{aligned}$$

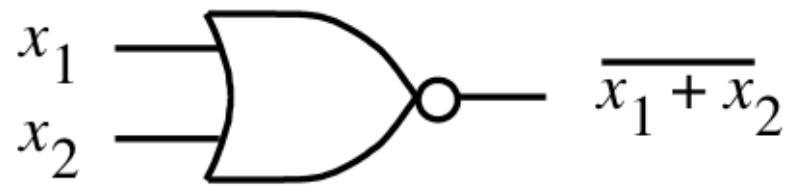
Two New Logic Gates

NAND Gate



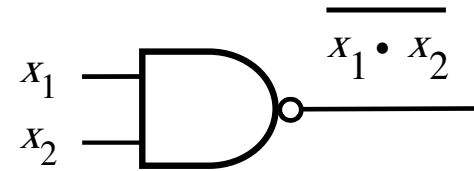
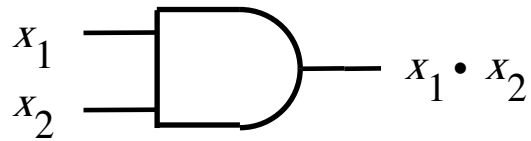
x_1	x_2	f
0	0	1
0	1	1
1	0	1
1	1	0

NOR Gate



x_1	x_2	f
0	0	1
0	1	0
1	0	0
1	1	0

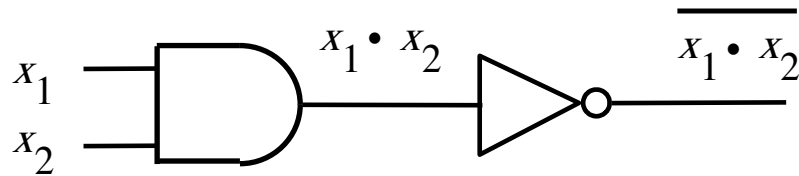
AND vs NAND



x_1	x_2	f
0	0	0
0	1	0
1	0	0
1	1	1

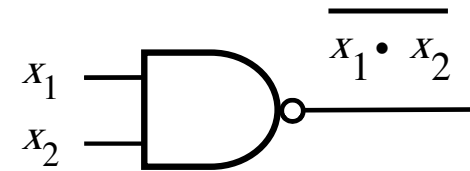
x_1	x_2	f
0	0	1
0	1	1
1	0	1
1	1	0

AND followed by NOT = NAND



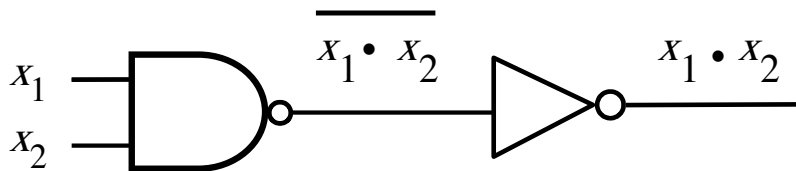
x_1	x_2	f
0	0	0
0	1	0
1	0	0
1	1	1

f
1
1
1
0



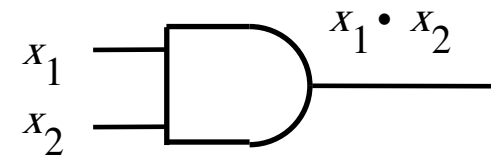
x_1	x_2	f
0	0	1
0	1	1
1	0	1
1	1	0

NAND followed by NOT = AND



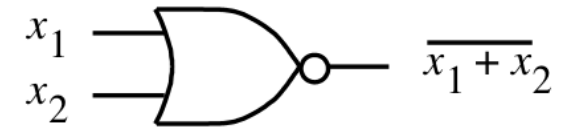
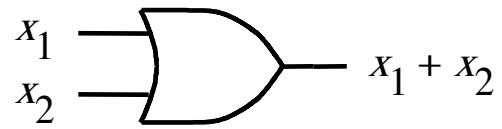
x_1	x_2	f
0	0	1
0	1	1
1	0	1
1	1	0

f
0
0
0
1



x_1	x_2	f
0	0	0
0	1	0
1	0	0
1	1	1

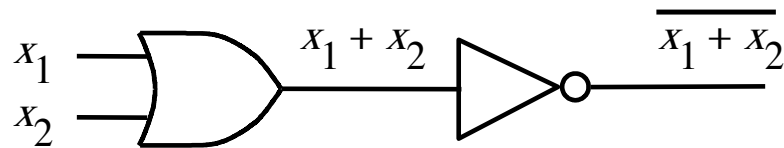
OR vs NOR



x_1	x_2	f
0	0	0
0	1	1
1	0	1
1	1	1

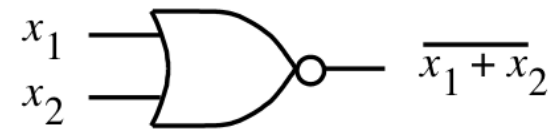
x_1	x_2	f
0	0	1
0	1	0
1	0	0
1	1	0

OR followed by NOT = NOR



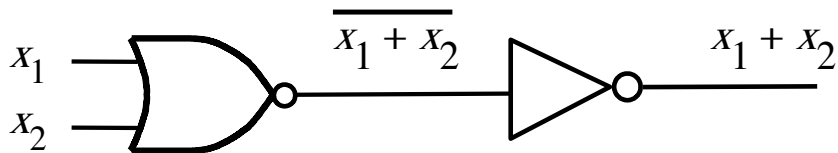
x_1	x_2	f
0	0	0
0	1	1
1	0	1
1	1	1

f
1
0
0
0



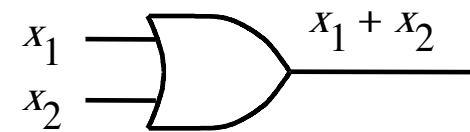
x_1	x_2	f
0	0	1
0	1	0
1	0	0
1	1	0

NOR followed by NOT = OR



x_1	x_2	f
0	0	1
0	1	0
1	0	0
1	1	0

f
0
1
1
1



x_1	x_2	f
0	0	0
0	1	1
1	0	1
1	1	1

Why do we need two more gates?

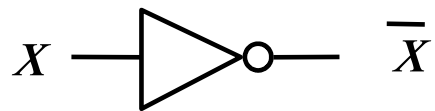
Why do we need two more gates?

They can be implemented with fewer transistors.

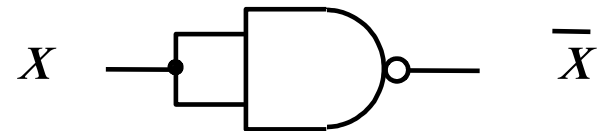
(more about this later)

**They are simpler to implement,
but are they also useful?**

Building a NOT Gate with NAND

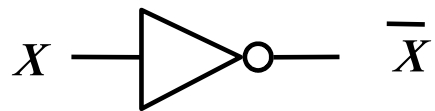


x	\bar{x}
0	1
1	0

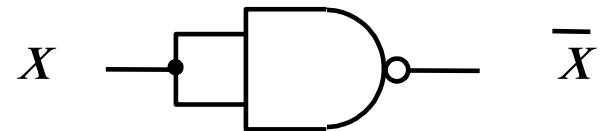


x	x	f
0	0	1
0	1	1
1	0	1
1	1	0

Building a NOT Gate with NAND



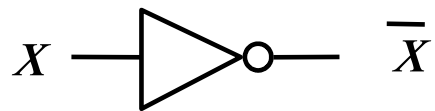
x	\bar{x}
0	1
1	0



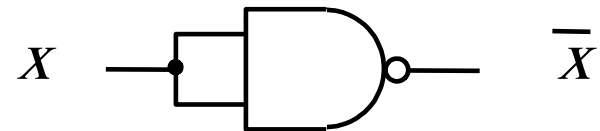
x	x	f
0	0	1
1	1	0

impossible combinations

Building a NOT Gate with NAND



x	\bar{x}
0	1
1	0



x	x	f
0	0	1
1	1	0

impossible combinations

Thus, the two truth tables are equal!

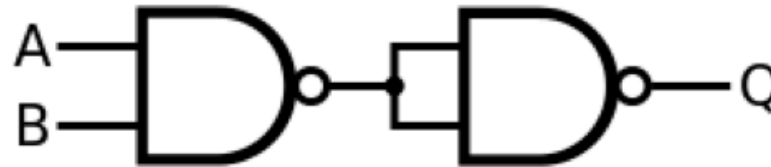
Building an AND gate with NAND gates

Desired AND Gate



$$Q = A \text{ AND } B$$

NAND Construction



$$= \text{NOT}(\text{NOT}(A \text{ AND } B))$$

Truth Table

Input A	Input B	Output Q
0	0	0
0	1	0
1	0	0
1	1	1

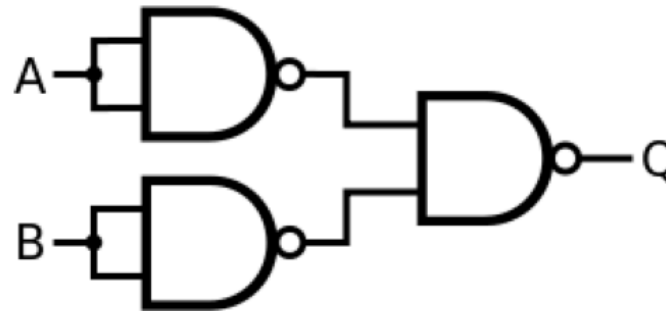
Building an OR gate with NAND gates

Desired OR Gate



$$Q = A \text{ OR } B$$

NAND Construction



$$= \text{NOT} [\text{NOT}(A \text{ AND } A) \text{ AND } \text{NOT}(B \text{ AND } B)]$$

Truth Table

Input A	Input B	Output Q
0	0	0
0	1	1
1	0	1
1	1	1

Implications

Implications

**Any Boolean function can be implemented
with only NAND gates!**

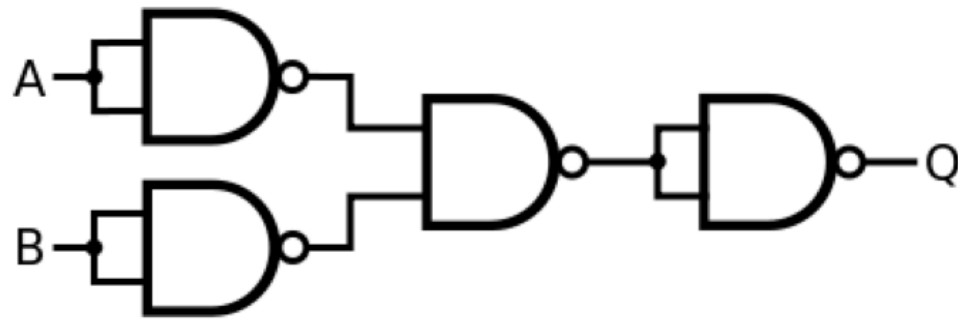
NOR gate with NAND gates

Desired NOR Gate



$$Q = \text{NOT}(A \text{ OR } B)$$

NAND Construction



$$= \text{NOT}\{ \text{NOT}[\text{NOT}(A \text{ AND } A) \text{ AND } \text{NOT}(B \text{ AND } B)] \}$$

Truth Table

Input A	Input B	Output Q
0	0	1
0	1	0
1	0	0
1	1	0

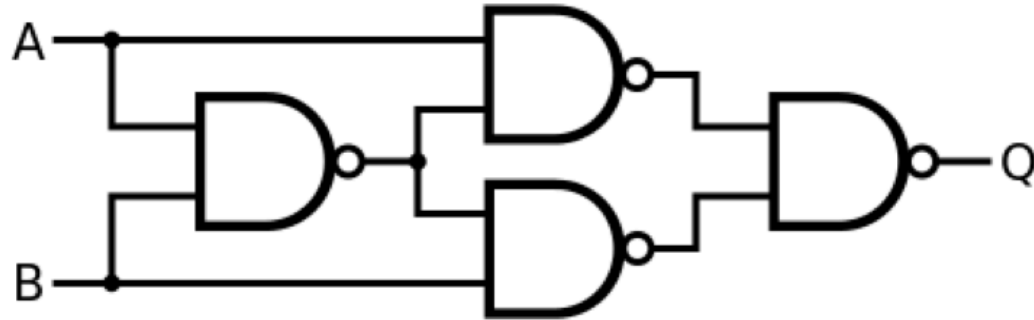
XOR gate with NAND gates

Desired XOR Gate



$$Q = A \text{ XOR } B$$

NAND Construction



$$= \text{NOT} [\text{NOT} \{ A \text{ AND } \text{NOT} (A \text{ AND } B) \} \text{ AND } \text{NOT} \{ B \text{ AND } \text{NOT} (A \text{ AND } B) \}]$$

Truth Table

Input A	Input B	Output Q
0	0	0
0	1	1
1	0	1
1	1	0

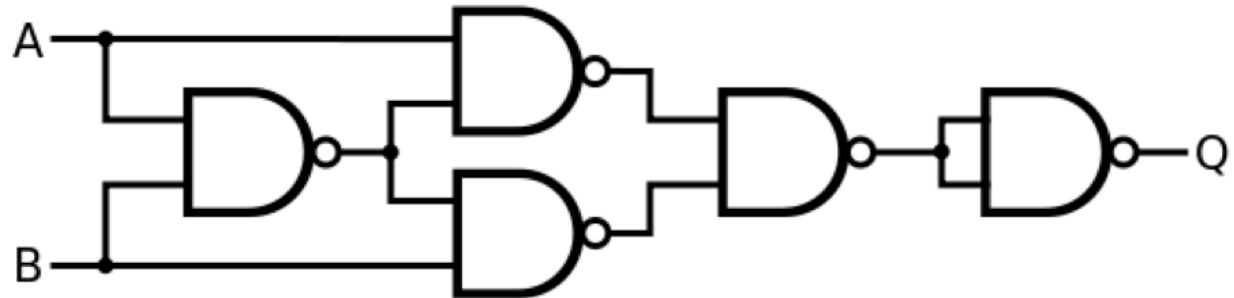
XNOR gate with NAND gates

Desired XNOR Gate



$$Q = \text{NOT}(A \text{ XOR } B)$$

NAND Construction

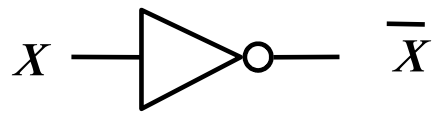


$$= \text{NOT}[\text{NOT}[\text{NOT}\{A \text{ AND } \text{NOT}(A \text{ AND } B)\} \text{ AND } \text{NOT}\{B \text{ AND } \text{NOT}(A \text{ AND } B)\}]]$$

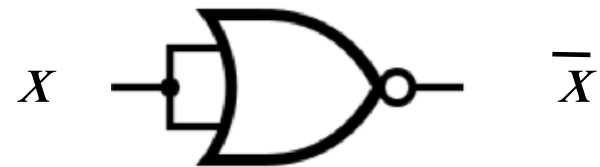
Truth Table

Input A	Input B	Output Q
0	0	1
0	1	0
1	0	0
1	1	1

Building a NOT Gate with NOR

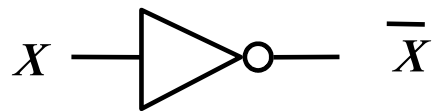


x	\bar{x}
0	1
1	0

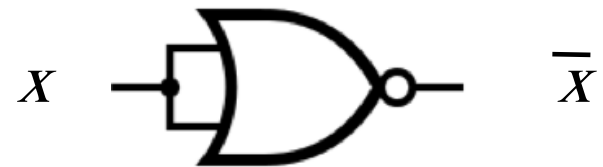


x	x	f
0	0	1
0	1	0
1	0	0
1	1	0

Building a NOT Gate with NOR



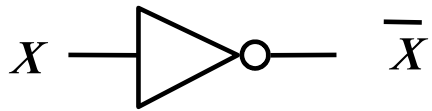
x	\bar{x}
0	1
1	0



x	x	f
0	0	1
[Redacted]		
1	1	0

impossible combinations

Building a NOT Gate with NOR



x	\bar{x}
0	1
1	0



x	x	f
0	0	1
1	1	0

impossible combinations

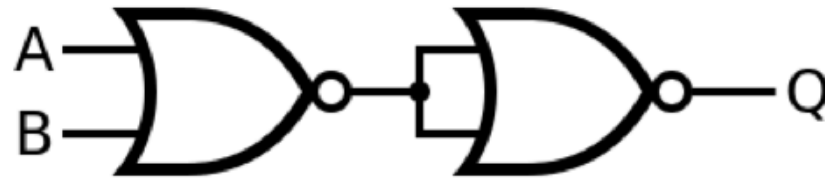
Thus, the two truth tables are equal!

Building an OR gate with NOR gates

Desired Gate



NOR Construction



Truth Table

Input A	Input B	Output Q
0	0	0
0	1	1
1	0	1
1	1	1

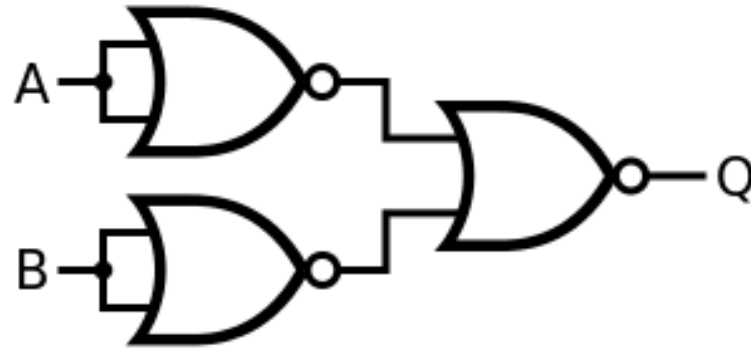
Let's build an AND gate with NOR gates

Let's build an AND gate with NOR gates

Desired Gate



NOR Construction



Truth Table

Input A	Input B	Output Q
0	0	0
0	1	0
1	0	0
1	1	1

Implications

Implications

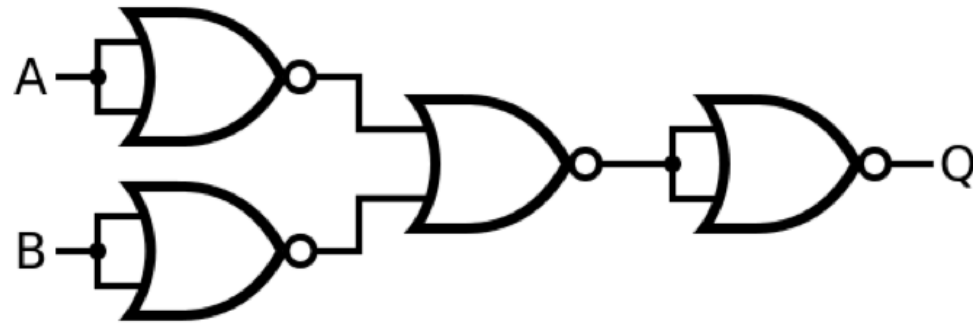
**Any Boolean function can be implemented
with only NOR gates!**

NAND gate with NOR gates

Desired Gate



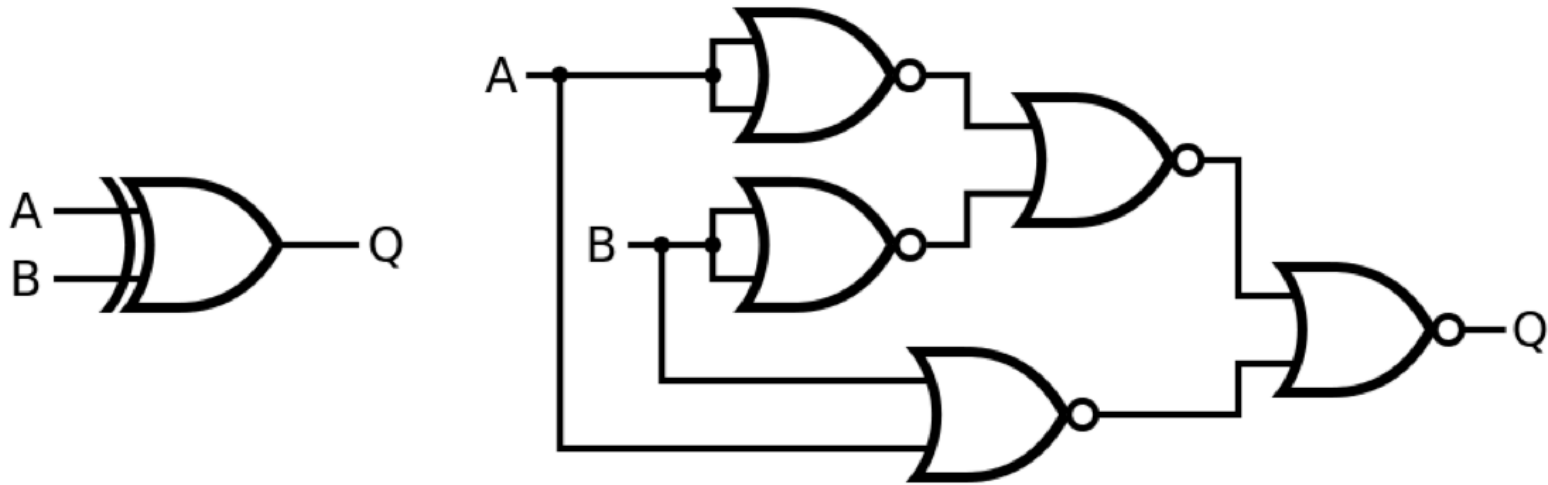
NOR Construction



Truth Table

Input A	Input B	Output Q
0	0	1
0	1	1
1	0	1
1	1	0

XOR gate with NOR gates



Truth Table

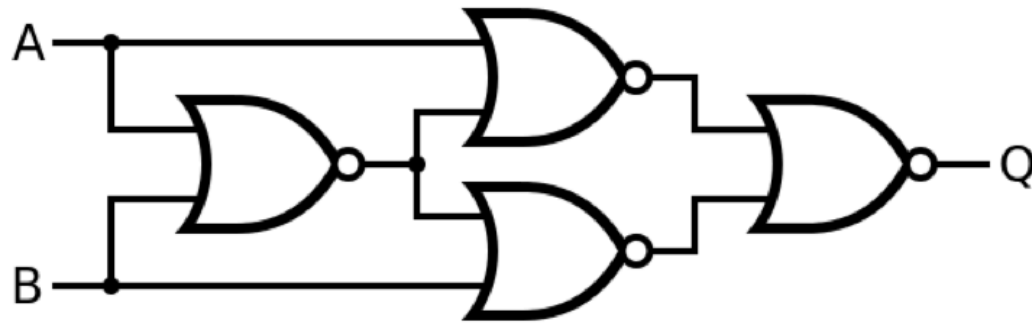
Input A	Input B	Output Q
0	0	0
0	1	1
1	0	1
1	1	0

XNOR gate with NOR gates

Desired XNOR Gate



NOR Construction

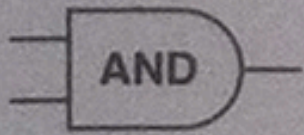


Truth Table

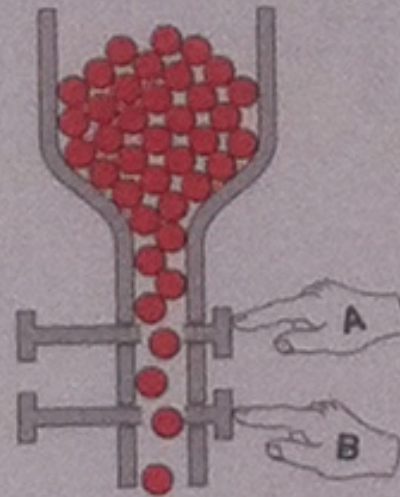
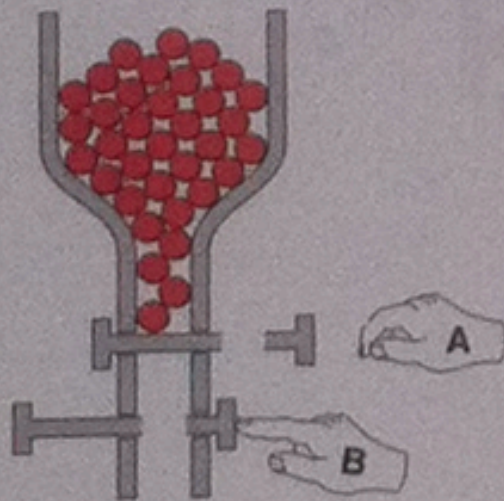
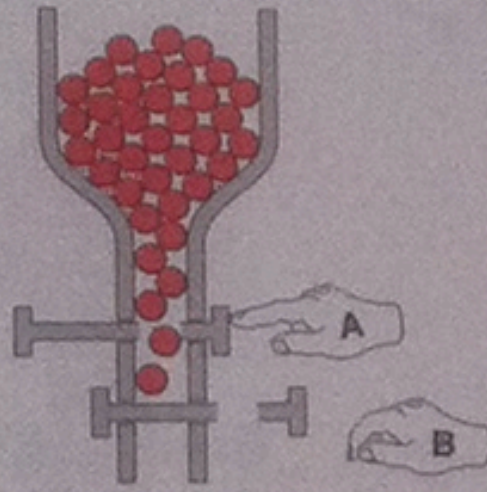
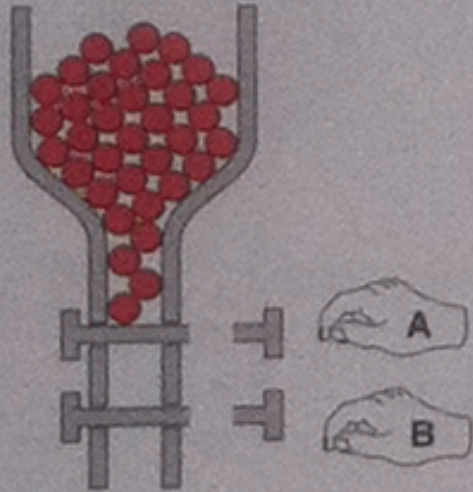
Input A	Input B	Output Q
0	0	1
0	1	0
1	0	0
1	1	1

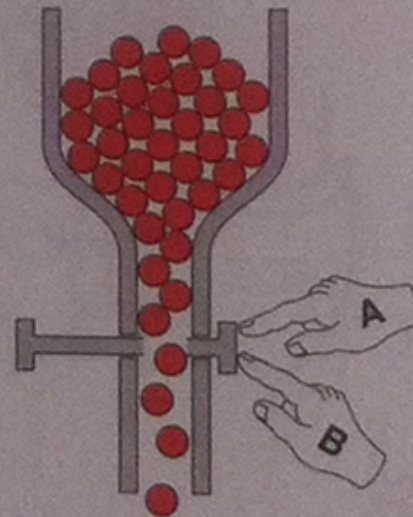
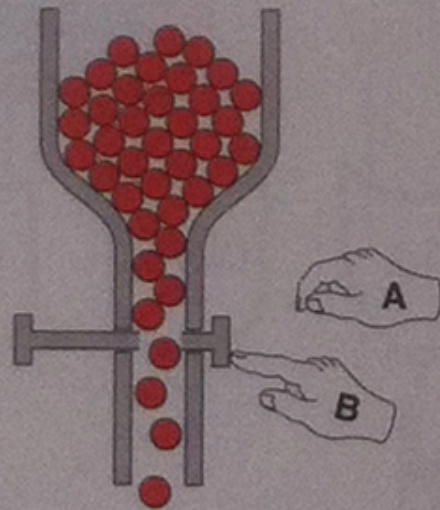
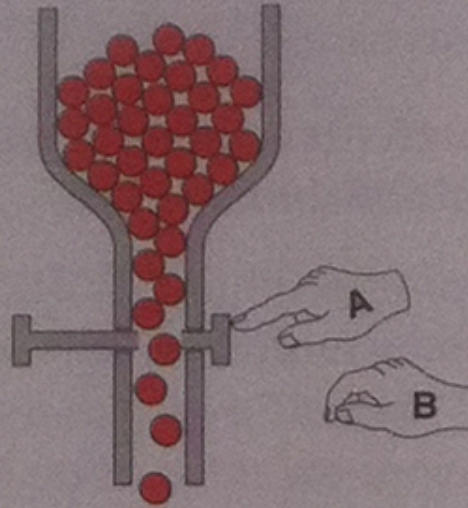
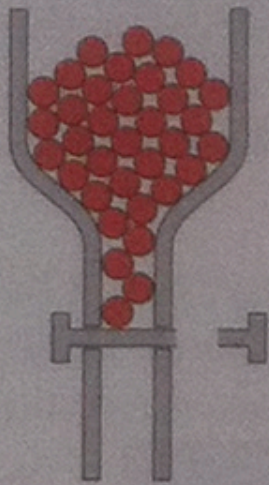
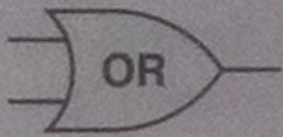
The following examples came from this book



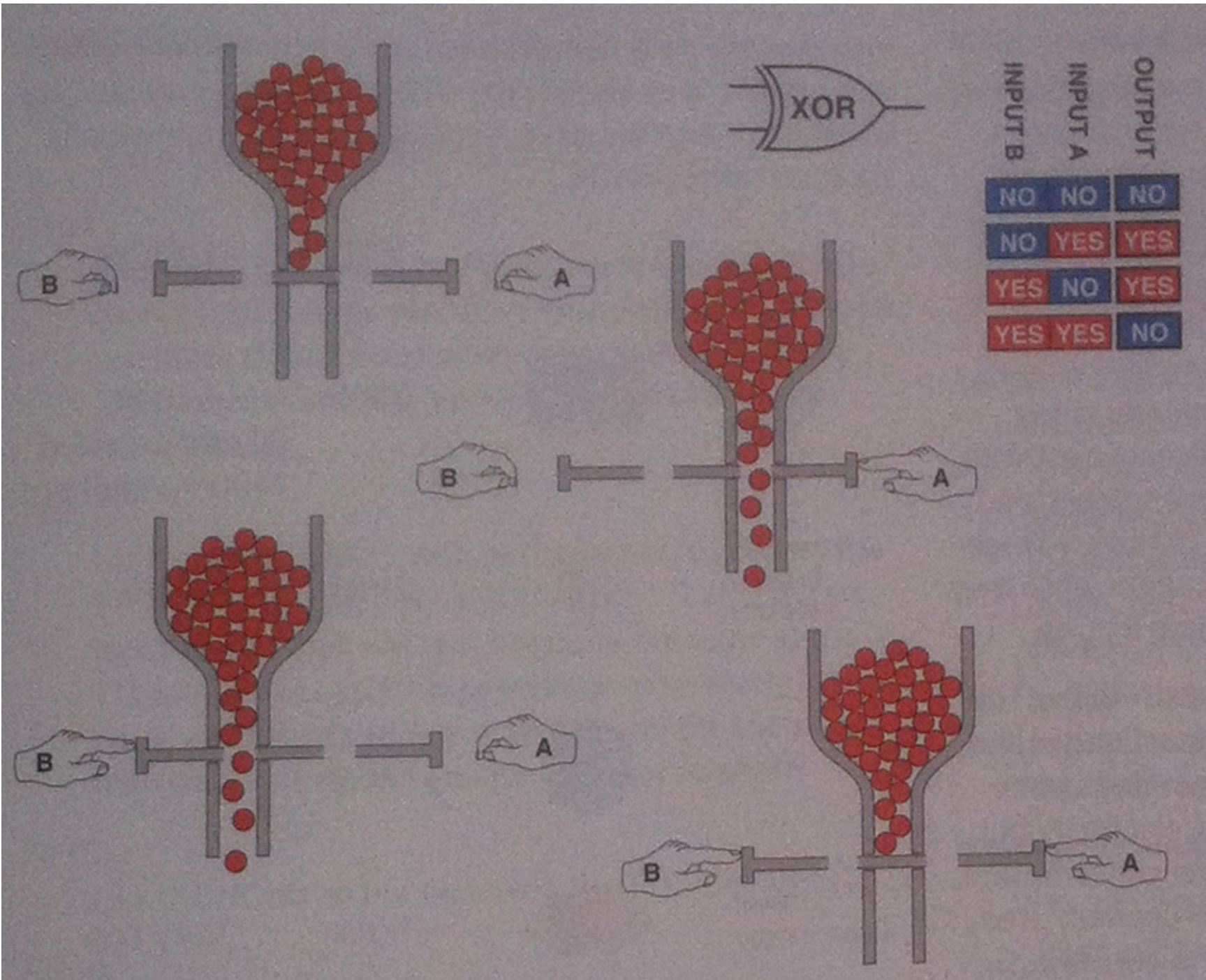


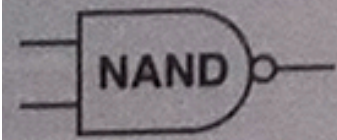
INPUT B	INPUT A	OUTPUT
NO	NO	NO
NO	YES	NO
YES	NO	NO
YES	YES	YES



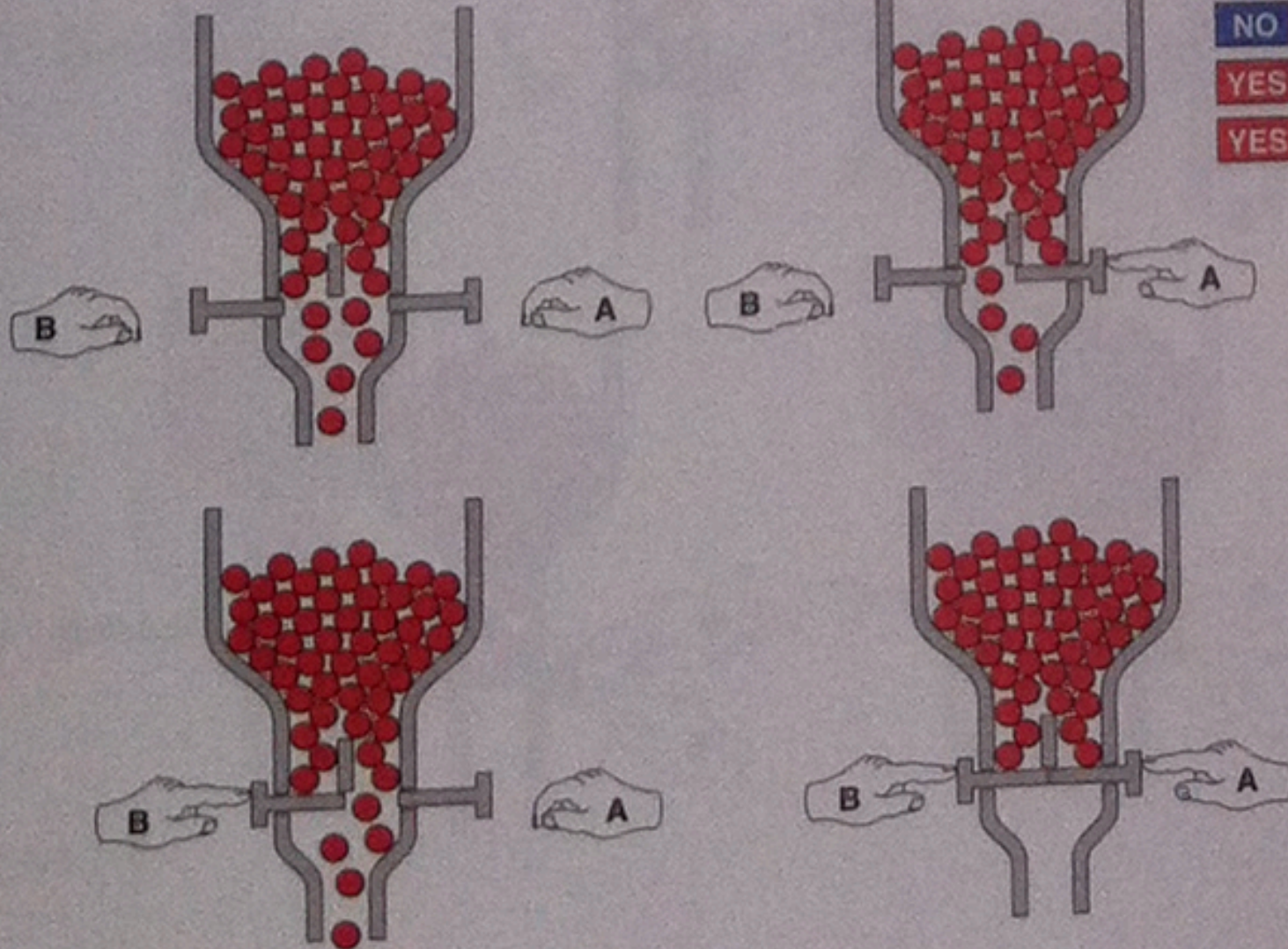


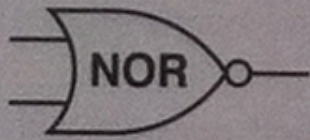
INPUT B	INPUT A	OUTPUT
NO	NO	NO
NO	YES	YES
YES	NO	YES
YES	YES	YES



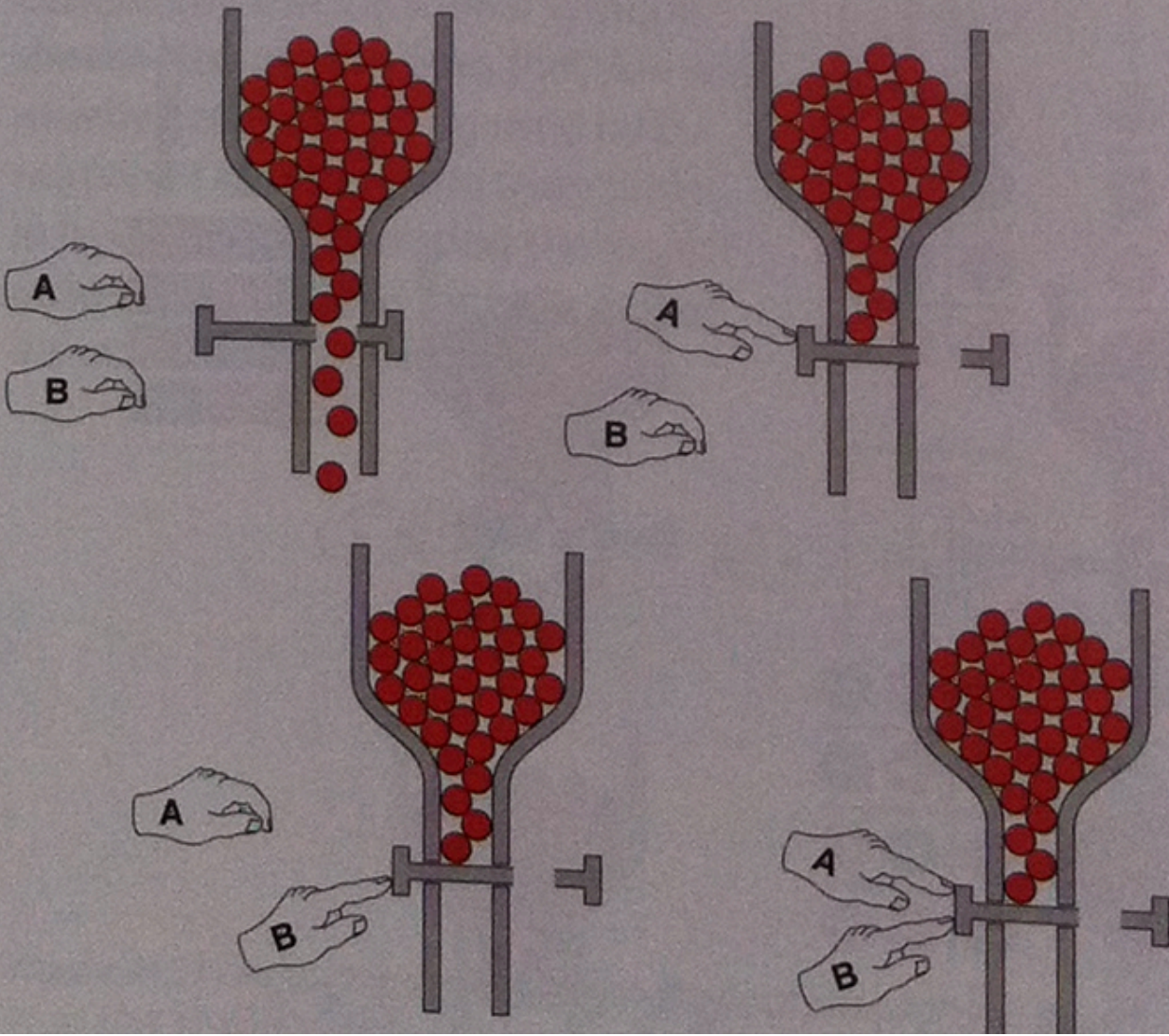


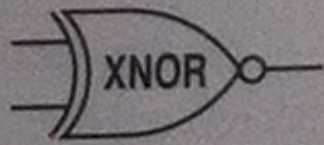
INPUT B	INPUT A	OUTPUT
NO	NO	YES
NO	YES	YES
YES	NO	YES
YES	YES	NO



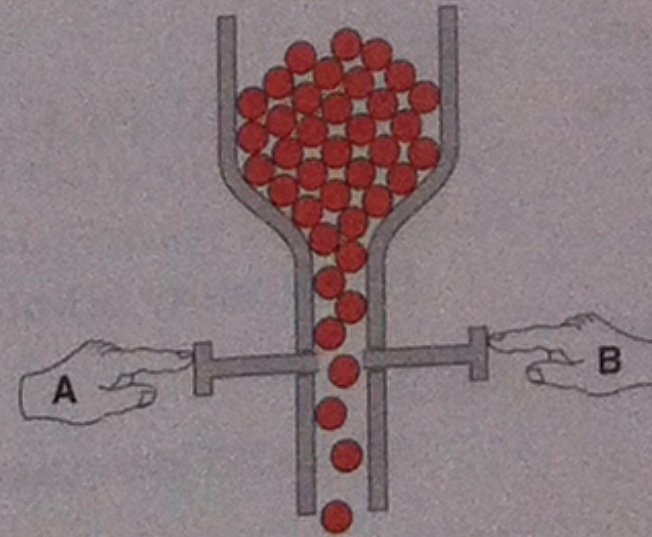
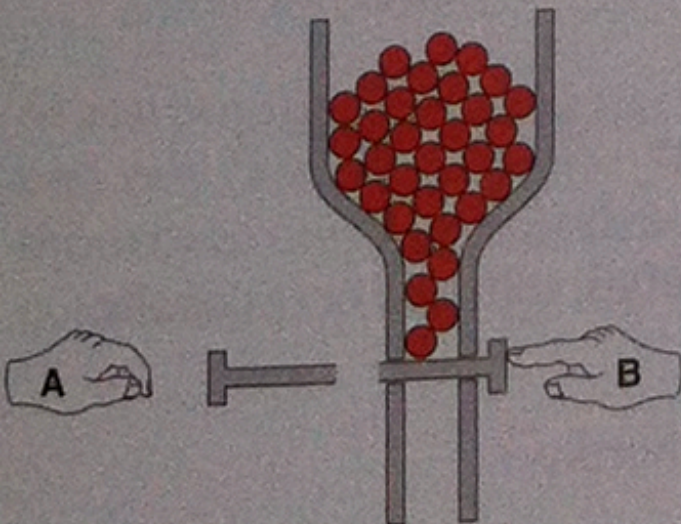
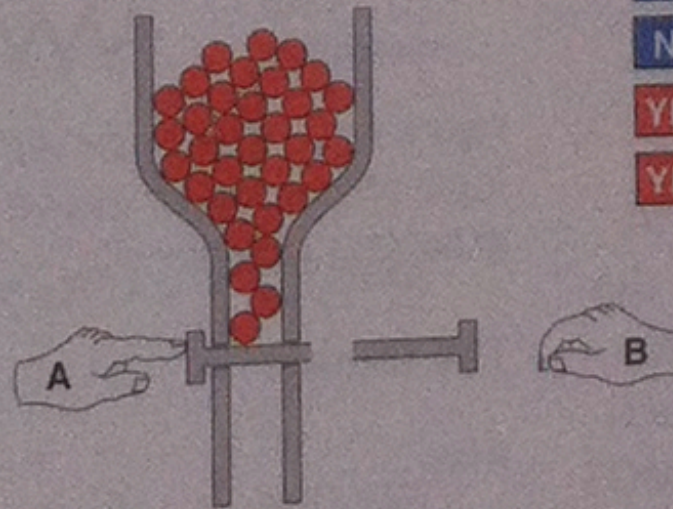
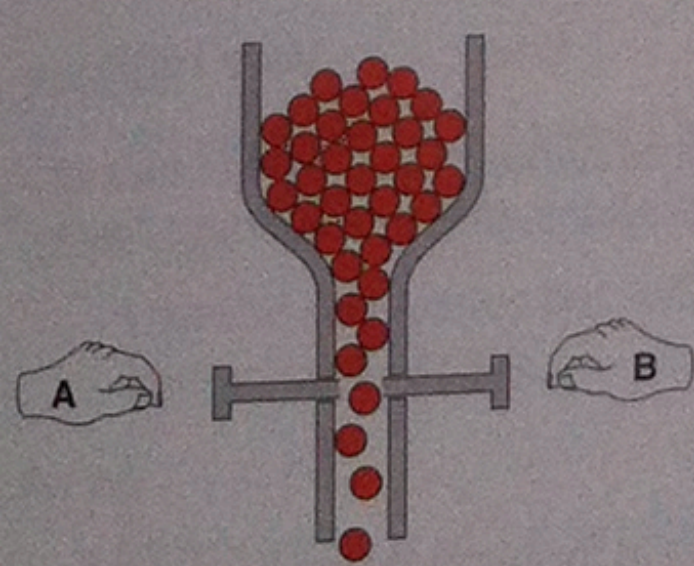


INPUT B	INPUT A	OUTPUT
NO	NO	YES
NO	YES	NO
YES	NO	NO
YES	YES	NO

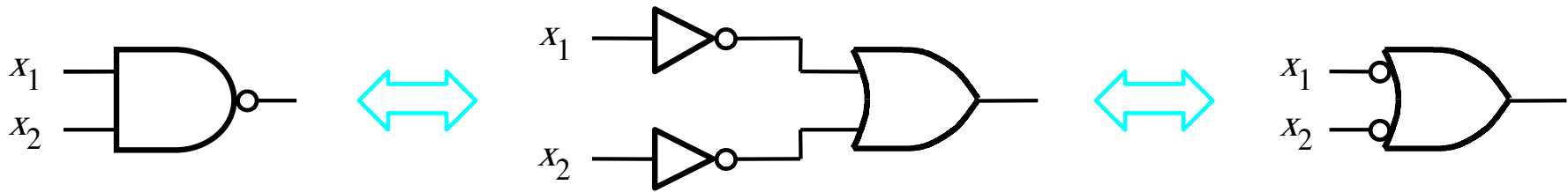




INPUT B	INPUT A	OUTPUT
NO	NO	YES
NO	YES	NO
YES	NO	NO
YES	YES	YES

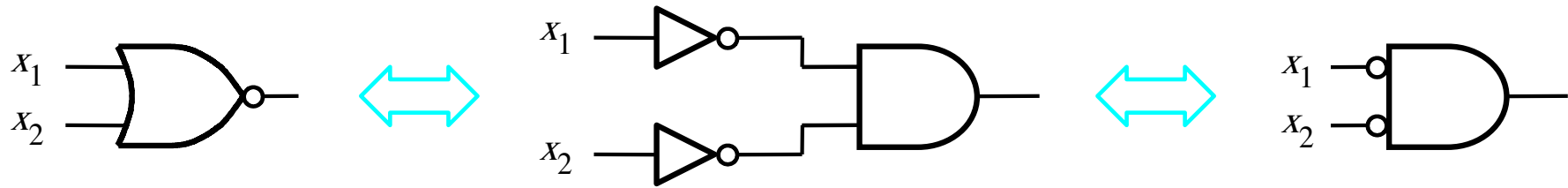


DeMorgan's theorem in terms of logic gates



(a) $\overline{x_1 x_2} = \overline{x_1} + \overline{x_2}$

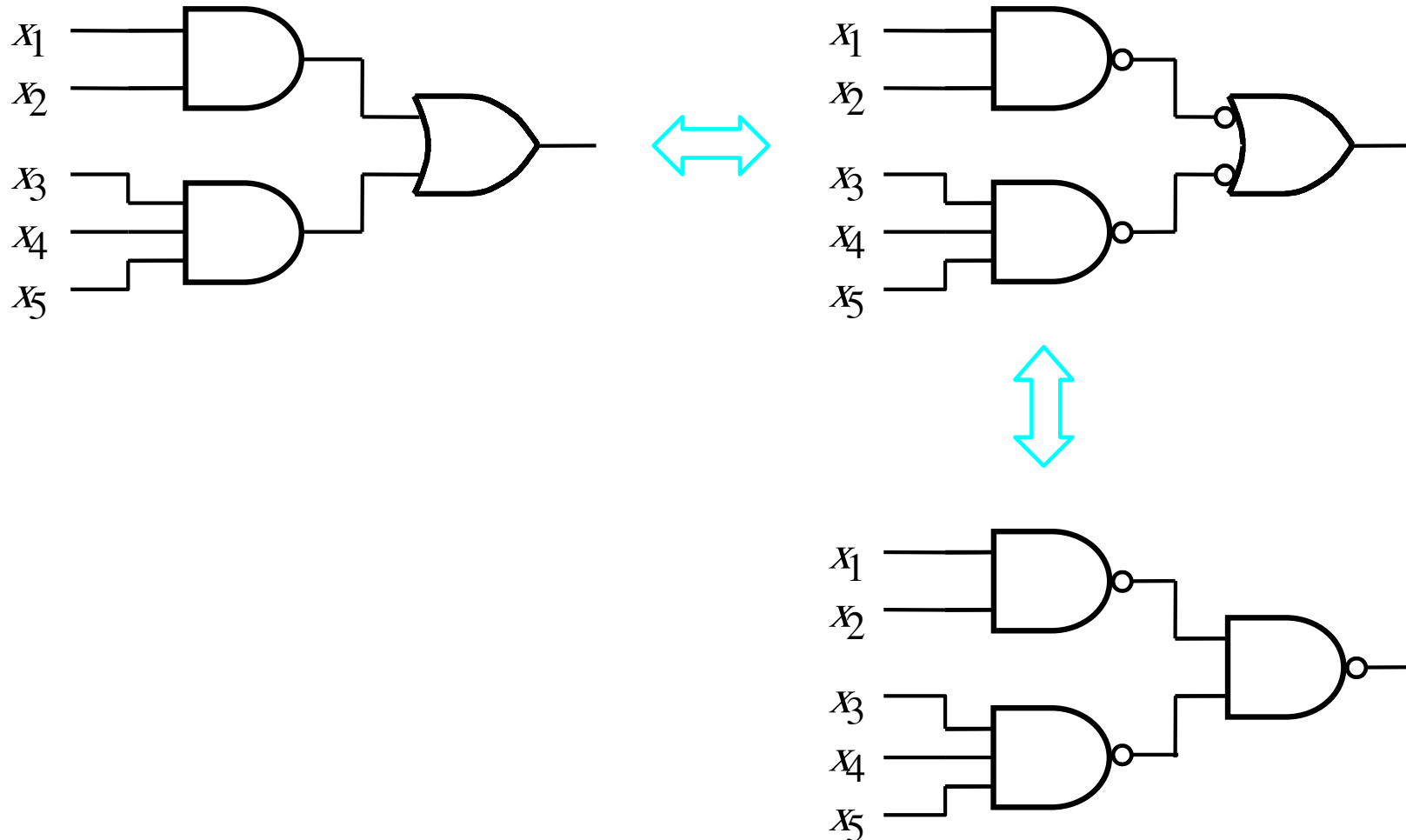
DeMorgan's theorem in terms of logic gates



(b) $\overline{x_1 + x_2} = \overline{x_1} \overline{x_2}$

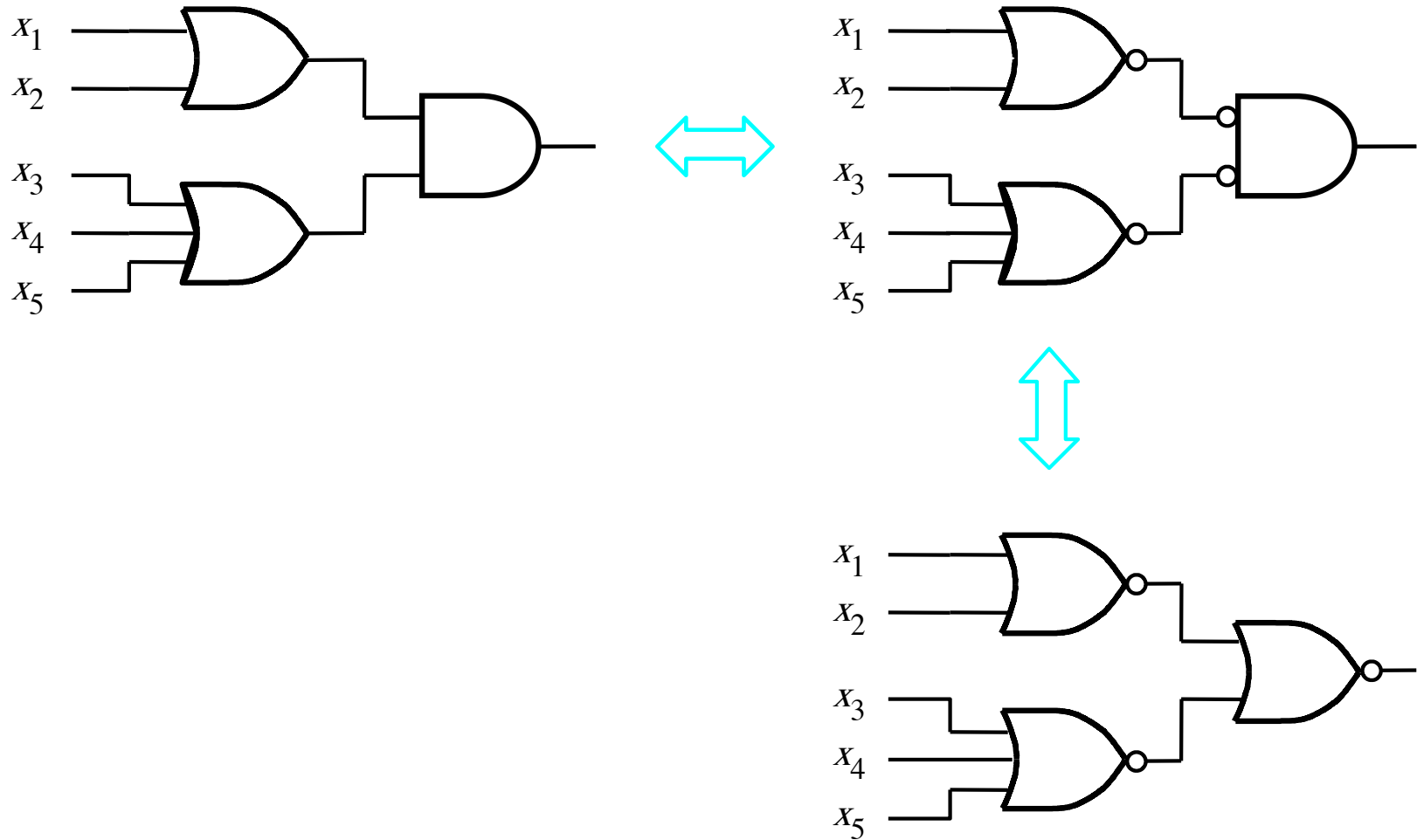
Function Synthesis

Using NAND gates to implement a sum-of-products



[Figure 2.27 from the textbook]

Using NOR gates to implement a product-of-sums



[Figure 2.28 from the textbook]

Example 2.13

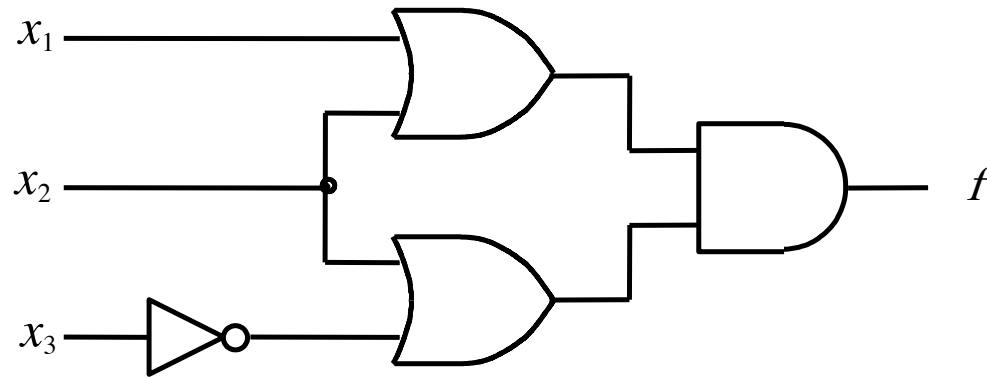
Implement the function $f(x_1, x_2, x_3) = \sum m(2, 3, 4, 6, 7)$ using only NOR gates.

Example 2.13

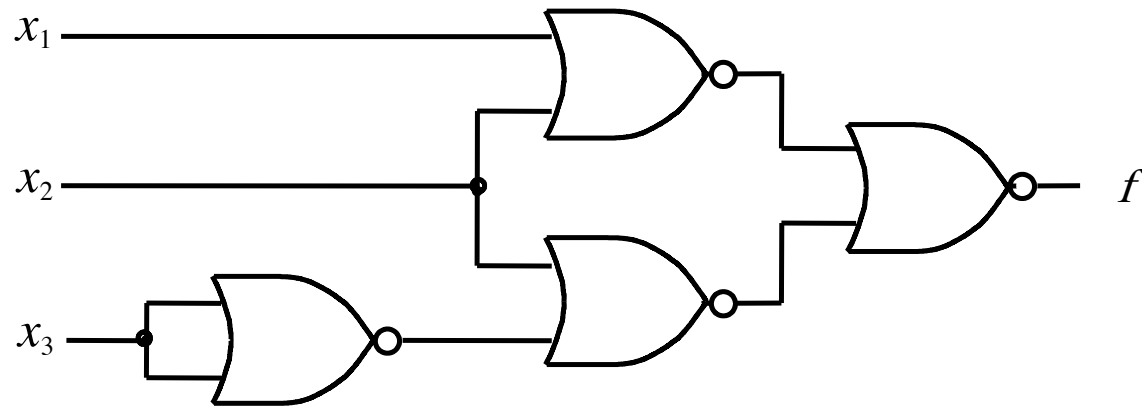
Implement the function $f(x_1, x_2, x_3) = \sum m(2, 3, 4, 6, 7)$ using only NOR gates.

The POS expression is: $f = (x_1 + x_2) (x_2 + \bar{x}_3)$

NOR-gate realization of the function



(a) POS implementation



(b) NOR implementation

Example 2.14

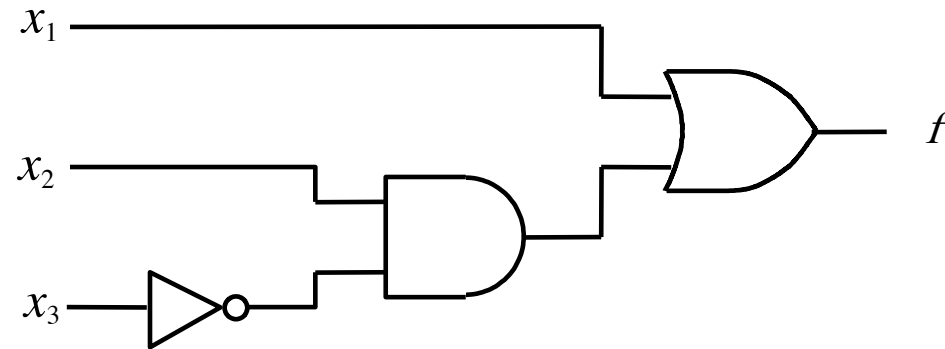
Implement the function $f(x_1, x_2, x_3) = \sum m(2, 3, 4, 6, 7)$ using only NAND gates.

Example 2.14

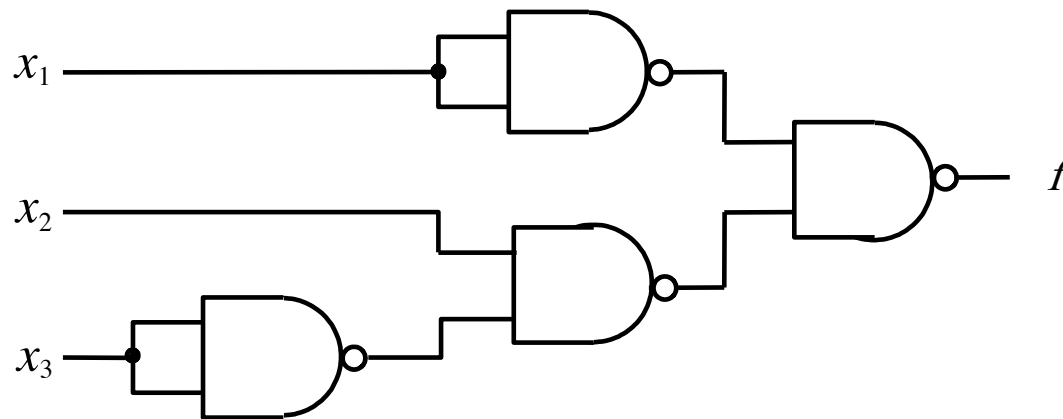
Implement the function $f(x_1, x_2, x_3) = \sum m(2, 3, 4, 6, 7)$ using only NAND gates.

The SOP expression is: $f = x_2 + x_1\bar{x}_3$

NAND-gate realization of the function



(a) SOP implementation



(b) NAND implementation

Questions?

THE END