

P1. (10 points) Draw a state transition diagram for:

- A state machine that reads in a sequence of binary digits, one at a time, and stops when it has read in a total of five 1s (need not be consecutive). To "stop" the machine, merely have it loop repeatedly in a final state.
- A state machine that stops when it has read in at least three consecutive 1s followed by a 0.

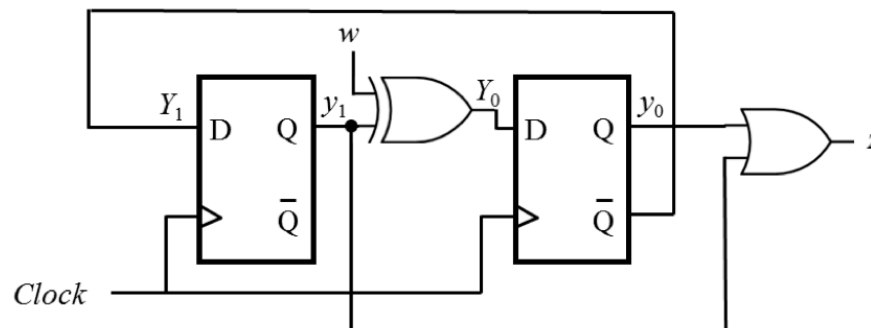
P2. (15 points) Design a three-bit counter-like circuit controlled by the input w . If $w=0$, then the counter subtracts 1 from its contents (acting like a normal down-counter). If $w=1$, then the counter adds 2 to its contents, wrapping around if the count has to become 8 or 9. Thus if the current state is 6 (or 7) and $w=1$, then the next state is 0 (or 1). Use D flip-flops in your circuit. Let y_2, y_1 , and y_0 be the current state values.

- Draw a state diagram for the machine.
- Construct a state assignment table including the next state and output.
- Write the simplified expressions for the next state and output logic.

P3. (10 points) Repeat P2 using T flip-flops in your circuit.

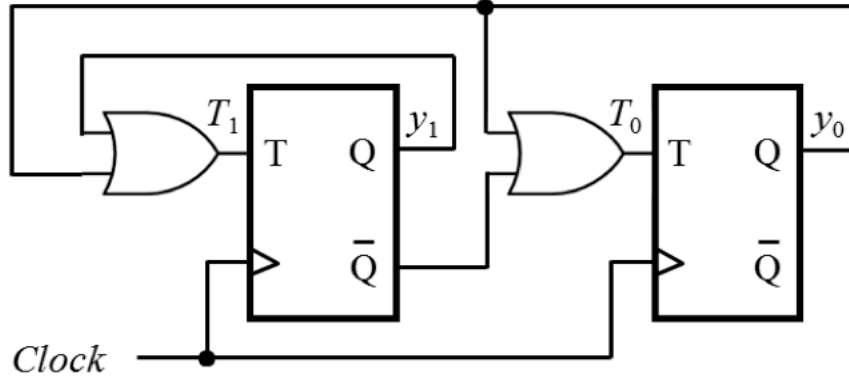
P4. (10 points) Derive a minimal state table for a single-input and single-output Moore-type FSM that produces an output of 1 if in the input sequence it detects either 110 or 101 patterns. Overlapping sequences should be detected. Repeat this problem for a Mealy-type FSM.

P5. (15 points) A FSM has two D flip-flops, an input w , and an output z . The circuit diagram is shown below.



- (5 points) Find the logic expressions of Y_1 , Y_0 , and the output z .
- (5 points) Show the state-assigned table of the FSM.
- (5 points) Draw the state diagram of the FSM.

P6. (10 points) A two-bit counter has the following circuit diagram. The output is $z_1z_0 = y_1y_0$.



- (5 points) Draw the state diagram of the counter.
- (5 points) What is the repeated counting sequence of this counter?

P7. (20 points) Consider the following state table for a FSM.

Present State	Next State		Output z
	$w=0$	$w=1$	
A	A	B	0
B	B	C	1
C	C	D	0
D	D	A	1

- (5 points) Draw the state diagram of the FSM.
- (3 points) Draw the circuit diagram of the FSM using D flip-flops.
- (3 points) Perform state minimization to minimize the number of states. Show your partitions in the procedure.
- (3 points) Draw the new state diagram of the minimized FSM.
- (3 points) Draw the circuit diagram of the minimized FSM using D flip-flops.
- (3 points) Compare the circuits in (b) and (e), what is the benefit of state minimization?

P8. (10 points) The arbiter FSM defined in section 8.8 (Figure 8.72) may cause device 3 to never get serviced if devices 1 and 2 continuously keep raising requests, so that in the Idle state it always happens that either device 1 or device 2 has an outstanding request. Modify the proposed FSM to ensure that device 3 will get serviced in that situation. That is, if it raises a request, then devices 1 and 2 will be serviced only once before device 3 is granted its request.