

CprE 281 Recitation 05 Solutions

- $$X'Y + XZ + YZ = X'Y + XZ + YZX + YZX'$$
 by 14a

$$= X'Y + X'YZ + XZ + XZY$$
 by 10a and 10b multiple times

$$= X'Y + XZ$$
 by 13a twice

Intuitively, YZ is partially covered by $X'Y$ and partially covered by XZ .

- $$QP + Q'R' + PR' = QP + Q'R'$$

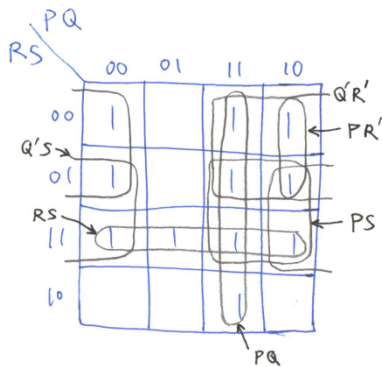
$$RS + R'P + SP = RS + R'P$$

$$RS + R'Q' + SQ' = RS + R'Q'$$

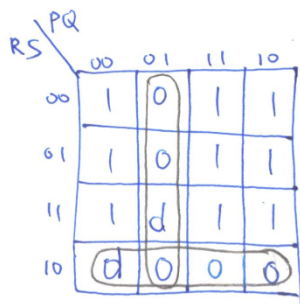
 Hence, PR' , SP and SQ' can be eliminated.

$$Z = PQ + RS + Q'R'$$

- Same expression as in Part 2.



- Min-cost implementation is the canonical POS: $Z = (P+Q')(R'+S)$.



- Notice the similarity between the K-map of Z in Part 2 and F in Part 4.
 In order to minimize the number of AND gates,

$$Z = PQ + RS + Q'R'$$

$$F = PR' + RS + Q'R'$$

 There are only 4 distinct product terms.