

P1. (10 points) Problem 2.36 in the textbook.

P2. (10 points) Problem 2.51 in the textbook.

P3. (10 points) Problem 2.52 in the textbook.

P4. (10 points) Problem 2.53 in the textbook.

P5. (10 points) Implement the following functions at the same time into one PLA with 3 inputs, four AND gates (in AND plane), and two OR gates in OR plane.

$$f_1 = x_1' x_2' x_3' + x_1' x_2 x_3' + x_1' x_2' x_3 + x_1 x_2 x_3$$

$$f_2 = x_1' x_2' x_3' + x_1 x_2' x_3' + x_1' x_2' x_3 + x_1 x_2 x_3$$

P6. (25 points) Use a K-map to simplify the following functions in SOP forms **as much as possible**:

(a)  $f(a) = \sum m(0,1)$

(b)  $f(a,b,c) = \sum m(0,3,5,6)$

(c)  $f(a,b,c) = a'bc' + a'b'c + a'bc + ab'c + abc$

(d)  $f(a,b,c,d) = \sum m(0,2,5,8,9,10,12,13,14,15)$

(e)  $f(a,b,c,d) = \sum m(1,7,9,10,11,12,13,15)$

P7. (25 points) A four-variable function that is equal to 1 if any three or all four of its variables are equal to 1 is called a *majority* function.

(a) Write the truth table for the majority function.

(b) Use a K-map to derive the simplest expression for this majority function.

(c) Suppose that the input combinations with equal number of zeros and ones will never occur. Now simplify the function using a K-map.

(d) Derive the simplest expression for the majority function of part (c) by using a K-map and the product-of-sums form.

(e) Compare the costs of your answers to part (c) and part (d) in terms of the number of gates and inputs.