

VIDEO DENOISING VIA ONLINE SPARSE AND LOW-RANK MATRIX DECOMPOSITION

Han Guo and Namrata Vaswani

ECE dept, Iowa State University, Ames, IA, USA

Email: {hanguo,namrata}@iastate.edu

ABSTRACT

Video denoising refers to the problem of removing “noise” from a video sequence. Here the term “noise” is used in a broad sense to refer to any corruption or outlier or interference that is not the quantity of interest. In this work, we develop a novel approach to video denoising that is based on the idea that most noisy or corrupted videos can be split into two parts - the approximate “low-rank” layer and the “sparse layer”. We first splitting the given video into these two layers, and then apply an existing state-of-the-art denoising algorithm on each layer. We show, using extensive experiments, that our denoising approach outperforms the state-of-the-art denoising algorithms.

Index Terms— denoising, sparse and low-rank matrix

1. INTRODUCTION

Video denoising refers to the problem of removing “noise” from a video sequence. Here the term “noise” is used in a broad sense to refer to any corruption or outlier or interference that is not the quantity of interest.

In the last few decades there has been a lot of work on video denoising. Many of the approaches extend image denoising ideas to 3D by also exploiting dependencies across the temporal dimension. An important example of this is “grouping and collaboratively filtering” approaches which try to search for similar image patches both within an image frame and across nearby frames, followed by collaboratively filtering the noise from the stack of matched patches [1, 2, 3, 4, 5]. One of the most effective methods for image denoising, Block Matching and 3D filtering (BM3D) [2], is from this category of techniques. In BM3D, similar image blocks are stacked in a 3D array followed by applying a noise shrinkage operator in a transform domain. In its video version, VBM3D [6], the method is generalized to video denoising by searching for similar blocks across multiple frames. Another related work [7, 8] either uses matrix completion [7] or sparse and low rank matrix approximation [8] on grouped image patches to remove outliers.

Other recent works on video denoising include approaches that use motion compensation algorithms from the video com-

pression literature followed by denoising of similar nearby blocks [9, 10]; and approaches that use wavelet transform based [11, 12, 13] and discrete cosine transform (DCT) based [14] denoising solutions. Very recent video denoising methods include algorithms based on learning a sparsifying transform [15, 16, 17, 18].

Within the image denoising literature, the most promising recent approaches are based on deep learning [19, 20, 21].

In this paper, we develop a novel approach to video denoising, called *Layering Denoising*, that is based on the idea that most noisy or corrupted videos can be split into two parts - the approximate “low-rank” layer and the “sparse layer”. Here “low-rank” layer means that the matrix formed by each image of this layer arranged as a column vector is low-rank. The “sparse” layer is similarly defined. The low-rank plus sparse assumption for corrupted videos can be seen in many denoising scenarios:

- In traditional denoising scenario, consider videos that are corrupted either by very large variance Gaussian noise, or a combination of salt-and pepper noise (or other impulsive noise) and small variance Gaussian noise. For these type of videos, the large magnitude part of the noise, together with the foreground person / object in the video, form the “sparse layer”, while the background (slowly-changing in many applications, e.g., video surveillance) with small noise approximately forms the “low-rank” layer. The goal is to remove the Gaussian or mixed noise.
- In low-light videos of moving targets/objects, the denoising goal is to “see” the barely visible moving targets (sparse), from the slowly-changing dark background, which is low-rank and is considered as noise.
- In background editing applications, the slowly-changing background is corrupted by sparse foreground objects (outliers), and the denoising goal is to only recover the background.

Our algorithm proceeds by first splitting the given video into “sparse layer” and “low-rank layer”. This is followed by applying an existing state-of-the-art denoising algorithm

on each layer. For separating the video, we use a combination of an existing batch technique called principal components' pursuit (PCP) [22] and a recently proposed online and dynamic technique called Recursive Projected Compressive Sensing (ReProCS) [23, 24]. We initialize using PCP and use ReProCS afterwards (since, as shown in earlier work [24], it is faster and has better separation performance for videos where the sparse layer is either correlated over time or has large support size). This is followed by VBM3D on each of the two layers. In doing this, VBM3D exploits the specific characteristics of each layer and is able to find more matched blocks to filter over.

The performance of our algorithm is compared both with some of the best solutions from existing sparse + low-rank decomposition literature [25, 26, 27, 28, 29, 30, 31] as well as with just using VBM3D directly on the video. We also compare with one recent deep learning based image denoising solution [19] and an approach that makes use of sparse and low-rank matrix approximation on grouped image patches [8]. We provide comparisons for two denoising scenarios. The first is traditional denoising scenario, i.e., to remove add-on noise from the video. The noise can be Gaussian or a combination of Gaussian and salt and pepper noise. The second denoising scenario is to “see” object in the low-light environment. We show that our algorithm can label the moving object as the sparse layer.

1.1. Notation

In this paper, $P = \text{approx-basis}(\mathcal{M}, b\%)$ means that P is the $b\%$ left singular vectors' matrix for \mathcal{M} . $\text{PCP}(\mathcal{M})$ implements the PCP algorithm on data \mathcal{M} . $\text{Std-est}(\mathcal{M})$ denotes estimating the standard deviation from \mathcal{M} . $\text{VBM3D}(\mathcal{M}, \sigma)$ implements the VBM3D algorithm on data \mathcal{M} with input standard deviation σ .

1.2. Problem Formulation

We denote the observed video frames at time t by M_t . In general, $M_t = \text{Img}_t + W_t$, where Img_t denotes the clean image and W_t is the add-on noise, e.g., i.i.d. Gaussian or mixed noise. We write $M_t = S_t + L_t + W_t$ where S_t is sparse, modeling the foreground object and L_t lies in a low-dimensional subspace modeling the slowly-changing background. The denoising goal can be recovering Img_t , recovering S_t or recovering L_t .

2. THE LAYERING-DENOISING ALGORITHM

We explain the algorithm as following:

Initialization. Take a batch of initial video frames $[M_1, M_2, \dots, M_{t_{\text{train}}}]$ as training data and use stable-PCP [32] to separate it into a sparse matrix and a low-rank matrix $[L_1, L_2, \dots, L_{t_{\text{train}}}]$. Do SVD on $[L_1, L_2, \dots, L_{t_{\text{train}}}]$ and

retain the top left singular vectors, denoted by \hat{P} .

Splitting phase. For $t \geq t_{\text{train}} + 1$, we split M_t into two layers \hat{S}_t and \hat{L}_t . Firstly, M_t is projected to the space orthogonal to $\text{range}(\hat{P})$ to get the projected measurement vector,

$$y_t := (I - \hat{P}\hat{P}')M_t = \Phi M_t. \quad (1)$$

If we rewrite W_t as $W_t = O_t + N_t$ where entries of O_t have large magnitude comparable to S_t , and N_t is the remaining, y_t can be expressed as

$$y_t = \Phi(S_t + O_t) + \beta_t \text{ where } \beta_t := \Phi(L_t + N_t). \quad (2)$$

We solve

$$\min_x \|x\|_1 \text{ s.t. } \|y_t - \Phi x\|_2 \leq \xi \quad (3)$$

and denote its solution by \hat{S}_t which is an approximation of $S_t + O_t$. \hat{L}_t is obtained by simply subtracting \hat{S}_t from M_t .

Denoising phase. We perform VBM3D on \hat{S}_t and \hat{L}_t . Note that VBM3D here can be replaced with any other denoisers based on need. Their input standard deviations are estimated from $[\hat{S}_t, \dots, \hat{S}_{t_{\text{train}}}]$ and $[\hat{L}_t, \dots, \hat{L}_{t_{\text{train}}}]$ respectively. The final denoised output is simply the sum of the denoised layer \hat{S}_t and \hat{L}_t , i.e., $I_{\text{denoised},t} = S_{\text{denoised},t} + L_{\text{denoised},t}$, or just one of $I_{\text{denoised},t}$ and $L_{\text{denoised},t}$ depends on the application.

Subspace Update phase (Optional). In long videos the span of the L_t 's will change with time. Hence one needs to update the subspace estimate \hat{P} every so often. This can be done efficiently using the projection-PCA algorithm proposed in [24].

3. EXPERIMENTS

3.1. Removing Add-on Noise

In this part we compare our proposed denoise scheme with VBM3D, a deep learning image denoising method called Multi Layer Perceptron (MLP) [19], and an algorithm that uses sparse and low-rank matrix approximation on grouped patches [8] which we call SLMA for short, on several video datasets that can be downloaded from <http://www.ece.iastate.edu/~hanguo/denoise.html>. The denoised output of Algorithm 1 here refers to $\mathcal{I}_{\text{denoised}} = S_{\text{denoised}} + L_{\text{denoised}}$. The codes for algorithms being compared are downloaded from the authors' webpage. The available MLP code contains parameters that are trained solely from image patches that were corrupted with Gaussian noise with $\sigma = 25$ and hence the denoising performance is best with $\sigma = 25$ and deteriorates for other noise levels.

We present a thorough comparison on the Curtain and Lobby dataset, and summarize comparisons on other datasets in Table 1. The noise being added to the original image frames are Gaussian ($\sigma = 25$), Gaussian ($\sigma = 25$) plus salt and pepper noisy, and Gaussian ($\sigma = 70$). The input σ for all algorithms is estimated from the noisy data rather than given the

Algorithm 1 Layering-Denoising**Input:** $M_1, M_2, \dots, M_{t_{\max}}$;**Initialization:**Obtain $[L_1, \dots, L_{t_{\text{train}}}]$ from $\text{PCP}([M_1, \dots, M_{t_{\text{train}}}]$); $\hat{P} \leftarrow \text{approx-basis}(\frac{1}{\sqrt{t_{\text{train}}}}[L_1, \dots, L_{t_{\text{train}}}], 95\%)$ **Phase 1: Split M_t into two layers**

1. $\hat{\sigma} \leftarrow \text{Std-est}([M_1, \dots, M_{t_{\text{train}}}]$)
2. Apply ReProCS on M_t :
 - (a) Compute \hat{S}_t as the solution of simple- ℓ_1 minimization (3).
 - (b) $\hat{L}_t \leftarrow M_t - \hat{S}_t$

Phase 2: Denoising

1. $\hat{\sigma}_{\text{fg}} \leftarrow \text{Std-est}([\hat{S}_1, \dots, \hat{S}_{t_{\text{train}}}]$
 $\hat{\sigma}_{\text{bg}} \leftarrow \text{Std-est}([\hat{L}_1, \dots, \hat{L}_{t_{\text{train}}}]$
2. $\mathcal{S}_{\text{denoised}} \leftarrow \text{VBM3D}([\hat{S}_1, \dots, \hat{S}_{t_{\max}}], \hat{\sigma}_{\text{fg}})$
 $\mathcal{L}_{\text{denoised}} \leftarrow \text{VBM3D}([\hat{L}_1, \dots, \hat{L}_{t_{\max}}], \hat{\sigma}_{\text{bg}})$
3. $\mathcal{I}_{\text{denoised}} = \mathcal{S}_{\text{denoised}} + \mathcal{L}_{\text{denoised}}$

Output: $\mathcal{I}_{\text{denoised}}, \mathcal{S}_{\text{denoised}}, \mathcal{L}_{\text{denoised}}$

true value. We computed the frame-wise PSNRs for each case in Fig. 4 and Fig. 5 and show sample visual comparisons in Fig. 1 and Fig. 2. It can be seen in Fig. 4 and Fig. 5 that Algorithm 1 outperforms all other algorithms in all three noise level – the PSNR is the highest in almost all image frames. Visually, Algorithm 1 is able to recover more details of the images while other algorithms either fail or cause severe blurring effect.

We present the comparison on other datasets in Table 1. The noise being added to the original video is Gaussian, with standard deviation σ increases from 25 to 70. As can be seen in the table, Algorithm 1 outperforms other algorithms as well.

3.2. Denoising in Low-light Environment

Here we test the performance of denoising in low-light environment, i.e., to see target signal in the low-light environment. The video was taken in a dark environment where a barely visible person walked through the hallway. The algorithms being compared are foreground/background separation techniques – PCP, RSL [25], GRASTA [26], background subtraction, and video denoising approach VBM3D. The output we are using here is $S_{\text{denoised},t}$ and only its support (properly thresholded) is shown for ease of display. Fig. 3 shows that VBM3D is not capable of observing the walking person while our algorithm 1 can successfully mark the interested foreground per-

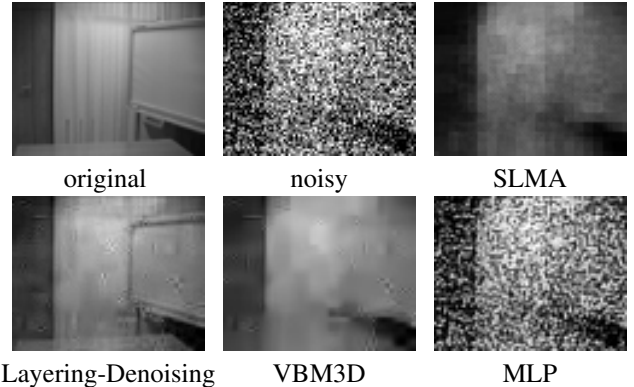


Fig. 1. Visual comparison of denoising performance for the Curtain dataset for very large Gaussian noise ($\sigma = 70$)

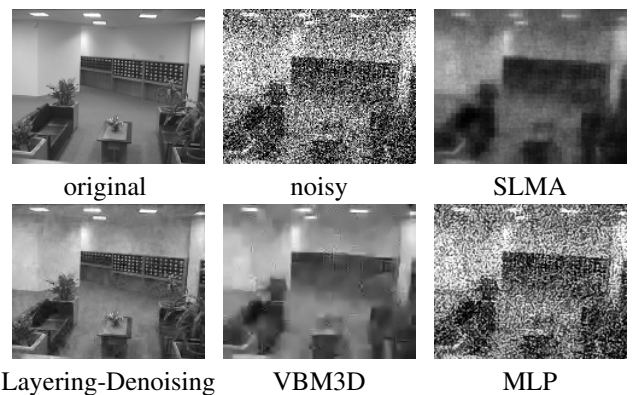


Fig. 2. Visual comparison of denoising performance for the Lobby dataset for very large Gaussian noise ($\sigma = 70$)

son and the result is slightly better than or as good as other foreground/background separation techniques.

4. CONCLUSION

In this paper we develop a denoising scheme which enhances the denoising performance of the state-of-the-art algorithm VBM3D, and is able to achieve denoising in a broad sense – observing interested signal in low-light environment or filtering out large but sparse noise from slow changing videos followed by using of VBM3D to remove the small noise. In general, splitting the video first results in a relatively clean low-rank layer since the large noise goes to the sparse layer in the ℓ_1 minimization (3). The clean layer improves the “grouping” accuracy in VBM3D. In fact one can replace VBM3D with other denoisers (procedures) to deal with specific noise models.

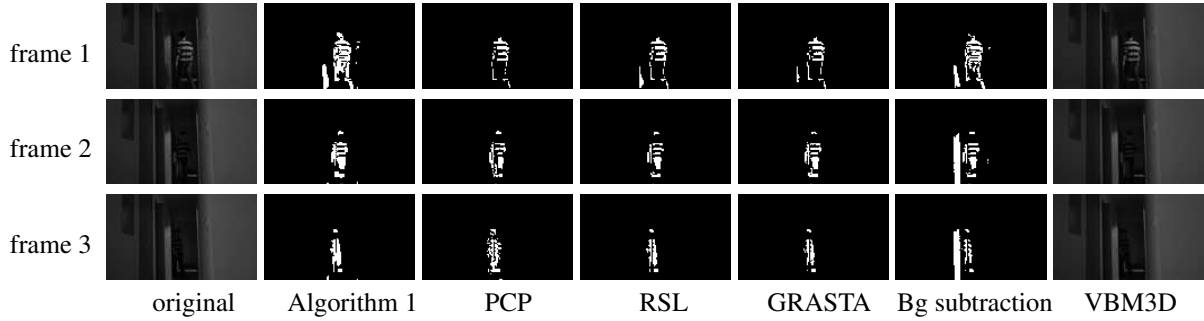


Fig. 3. Ability of “seeing” in the dark for three sample frames. From left to right: original dark image, results by Layering Denoising, PCP, RSL GRASTA, background subtraction and VBM3D.

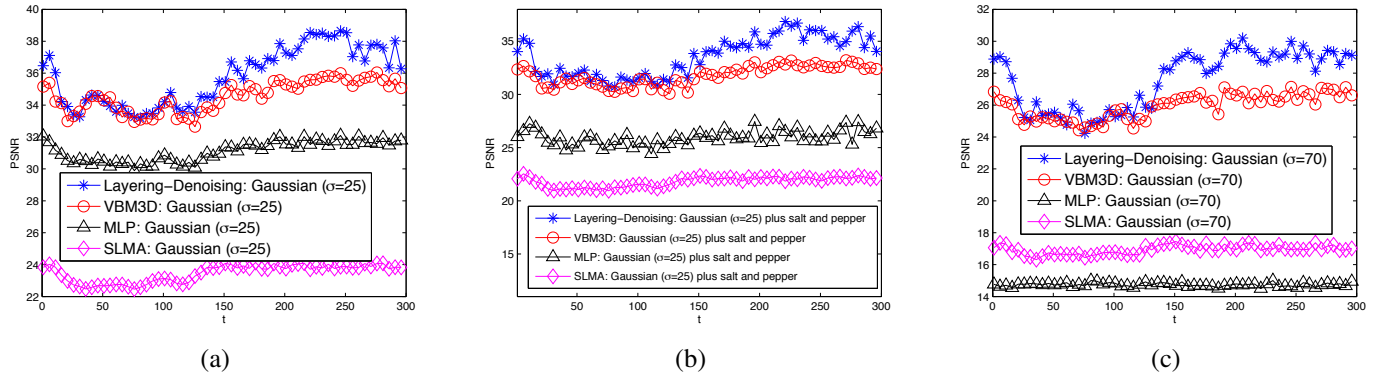


Fig. 4. Frame-wise PSNR for Curtain dataset with different noise level: (a) Gaussian noise with $\sigma = 25$, (b) Gaussian noise ($\sigma = 25$) plus salt and pepper noise, (c) Gaussian noise with $\sigma = 70$.

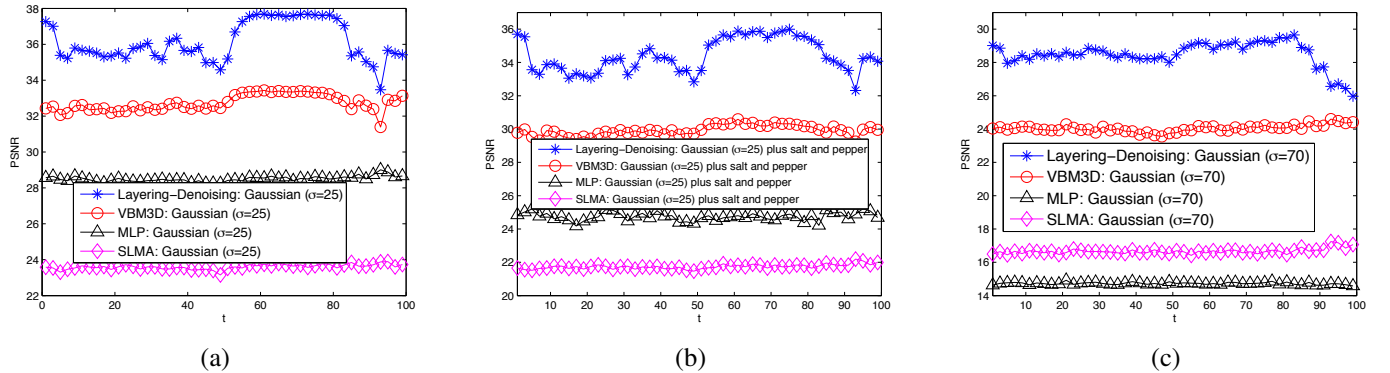


Fig. 5. Frame-wise PSNR for Lobby dataset with different noise level: (a) Gaussian noise with $\sigma = 25$, (b) Gaussian noise ($\sigma = 25$) plus salt and pepper noise, (c) Gaussian noise with $\sigma = 70$.

σ	fountain				airport			
	Layering-Denoising	VBM3D	MLP	SLMA	Layering-Denoising	VBM3D	MLP	SLMA
25	31.22	31.11	26.86	22.93	30.28	30.12	25.53	21.17
30	30.62	30.08	25.67	21.85	29.63	29.08	24.54	20.49
50	28.61	25.99	18.53	18.55	27.59	24.64	18.83	17.98
70	26.19	22.08	14.85	16.25	24.87	20.25	15.20	15.90

Table 1. Comparison of denoising performance: PSNR

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