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# Edge Detection & Boundary Tracing

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EE 528 Digital Image Processing

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# References

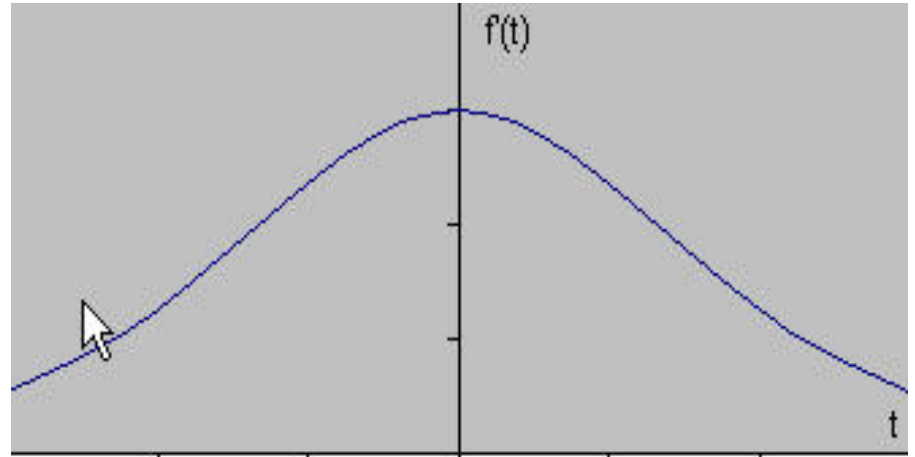
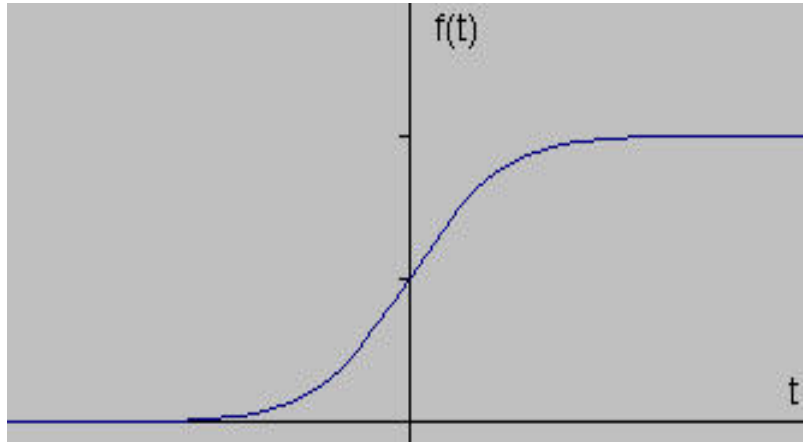
- A.K. Jain, Chapter 9
    - All details for edge detection given in this chapter
  - Milan Sonka's class notes on boundary tracing
  - Other webpages listed where needed
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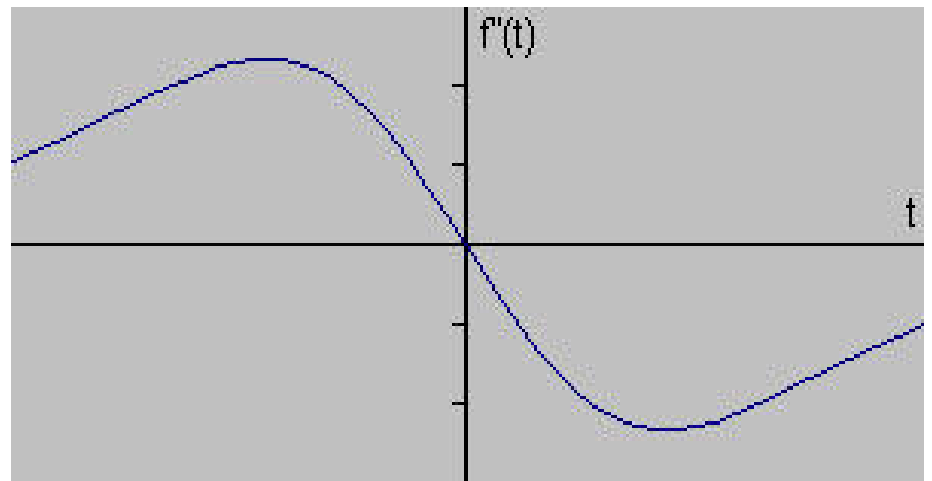
# Edge Detection Methods

- Discrete approx. of gradient, & threshold the gradient norm image
    - Edge: large gradient magnitude
  - Second derivative, & zero crossing detect
    - Edge: max or min of gradient along gradient direction
    - Weak edges (gradual variation) detected better, less chance of multiple edge responses
  - Derivative: enhances noise, 2<sup>nd</sup> derivative: worse
  - Band-pass filtering: some smoothing followed by taking the first or second derivative, e.g. LoG
  - Compass operators
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# Edges in 1D



Taken from <http://www.pages.drexel.edu/~weg22/edge.html>



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# Edge detection operators

- **First derivative:** Sobel, Roberts, Prewitts operators
    - Smooth in one direction, differentiate in the other
    - Apply in x and y directions, and take norm of the result
    - $\text{Arctan}(G_y/G_x) = \text{gradient direction (perpendicular to edge direction)}$
  - **Second derivative + smoothing:** Marr-Hildreth operator or LoG
    - Gaussian prefiltering followed by computing Laplacian
    - Works better when grey level transitions are smooth
    - An approximation to LoG is the Mexican hat (difference of Gaussians of different variance)
  - **Compass:** directional first derivative masks (Sobel or Prewitts)
  - **Canny's edge detector:** most commonly used.
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# Examples



First derivative method:  
misses some edges



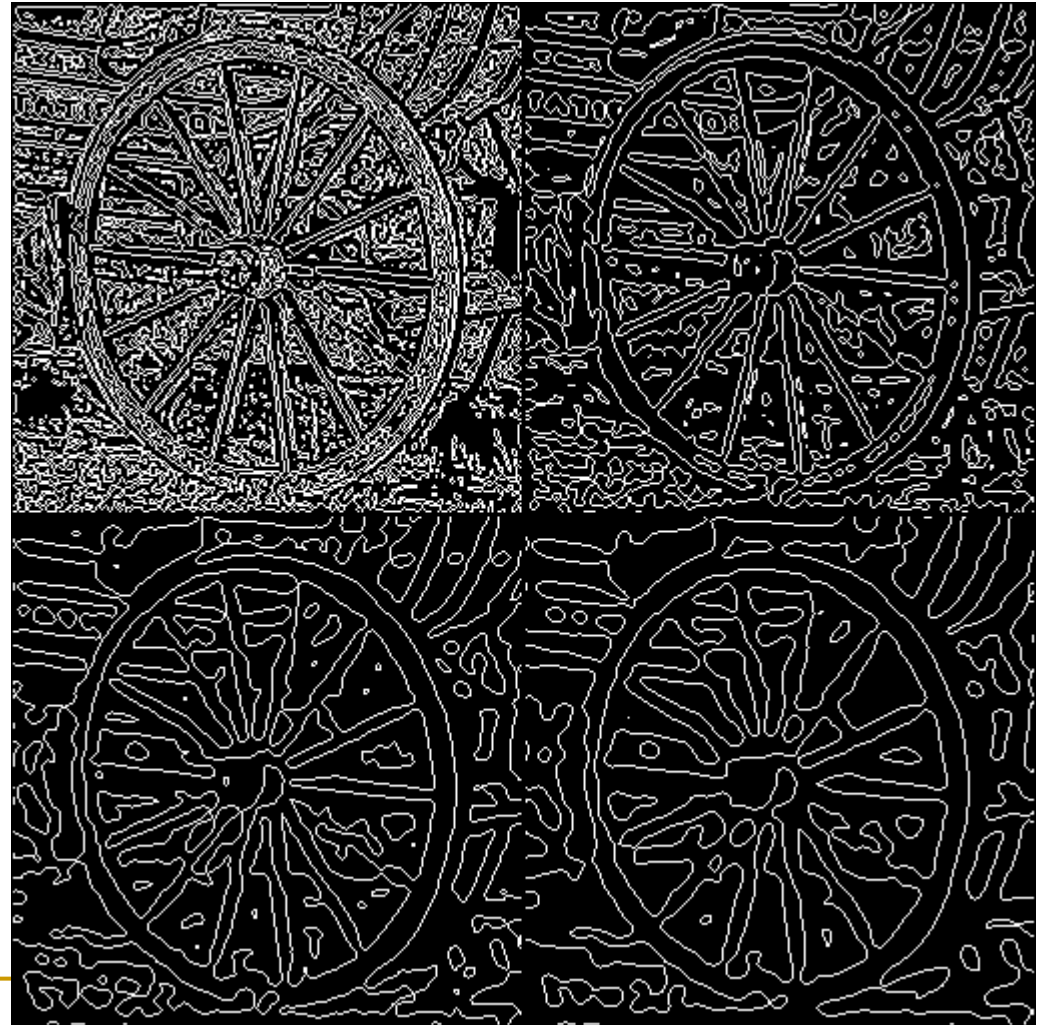
Laplacian:  
more sensitive to noise

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# LoG edge detection

- Zero crossings always lie on closed contours and so the output from the zero crossing detector is usually a binary image with single pixel thickness lines showing the positions of the zero crossing points.
  - Often occur at 'edges' in images, but also occur anywhere where both x and y gradients change sign
    - e.g. occur where roughly uniform intensity (very small image gradient which increases & decreases)
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# LoG with increasing sigma





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# Detecting zero crossings

- Simplest: threshold the LoG image, i.e. mark all points with LoG magnitude below a threshold as zero
    - Problem: multiple edge responses
  - Choose points where LoG magnitude smaller than all its 4 neighbors
    - Risk of missing some edge points
  - Zero crossing: LoG sign change in at least one direction
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# Canny's edge detector

- 1983, MS student at MIT
  - Designed an operator that minimizes probability of missing an edge, probability of false detection of edges, good localization
  - Restricted solution to linear shift-invariant operators
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# Main Idea of Canny

- Smooth the image using a Gaussian kernel: **reduce false alarms**
- Take gradient & compute gradient magnitude & gradient direction (quantify direction to multiples of 45 degrees)
- Perform **non-maximal suppression**: **localization**
  - Suppress a point if its gradient magnitude is smaller than either of its two neighbors along the gradient direction
- **Hysteresis**: two thresholds TL, TH
  - Suppress all points with magnitude  $< TH$
  - If a point has magnitude  $> TL$  and is linking two points with magnitude  $> TH$ , then keep it : **reduce misses**

# Applying Canny

Taken from <http://www.pages.drexel.edu/~weg22/edge.html>



Some edges missing  
(before hysteresis step)

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# Compass Operators

- Compute magnitude of directional derivative in 4 directions – 0, 45, 90, 135 degree
  - Maximum of the derivative values gives gradient magnitude
  - Threshold gradient magnitude
  
  - Alternatively, if only want to look for 45 degree edges: can do that.
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# Boundary Tracing & Edge Linking

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# Boundary Tracing

- Given a “segmented” image (an image with foreground pixels labeled 1 and background pixels labeled zero), trace either boundary of the foreground
    - May need to trace inner boundary (outermost pixels of foreground) or outer boundary (innermost pixels of background): `bwtraceboundary` command in MATLAB
    - Or if foreground, background labeled 1, -1, may use a zero level set searching method to get subpixel coordinates of boundary: `contour` command in MATLAB
  - Segmentation: discussed in next handout, simplest way to segment is to threshold intensity values
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# Boundary Tracing Algorithm links

- [http://www.mathworks.com/access/helpdesk\\_r13/help/toolbox/images/enhanc11.html](http://www.mathworks.com/access/helpdesk_r13/help/toolbox/images/enhanc11.html)
  - <http://www.icaen.uiowa.edu/~dip/LECTURE/Segmentation2.html#tracing>
  - [http://www.imageprocessingplace.com/DIP/dip\\_downloads/tutorials/contour\\_tracing\\_Abeer\\_George\\_Ghuneim/index.html](http://www.imageprocessingplace.com/DIP/dip_downloads/tutorials/contour_tracing_Abeer_George_Ghuneim/index.html)
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# MATLAB functions

- **contour**: gives you the contour location in sub-pixel coordinates. Need to have object & background labeled as 1, -1 (not 1,0)
  - **Inner boundary**: gives the locations of the outermost pixels of the object
    - `bwtraceboundary`
    - `bwboundaries` (for multiple objects)
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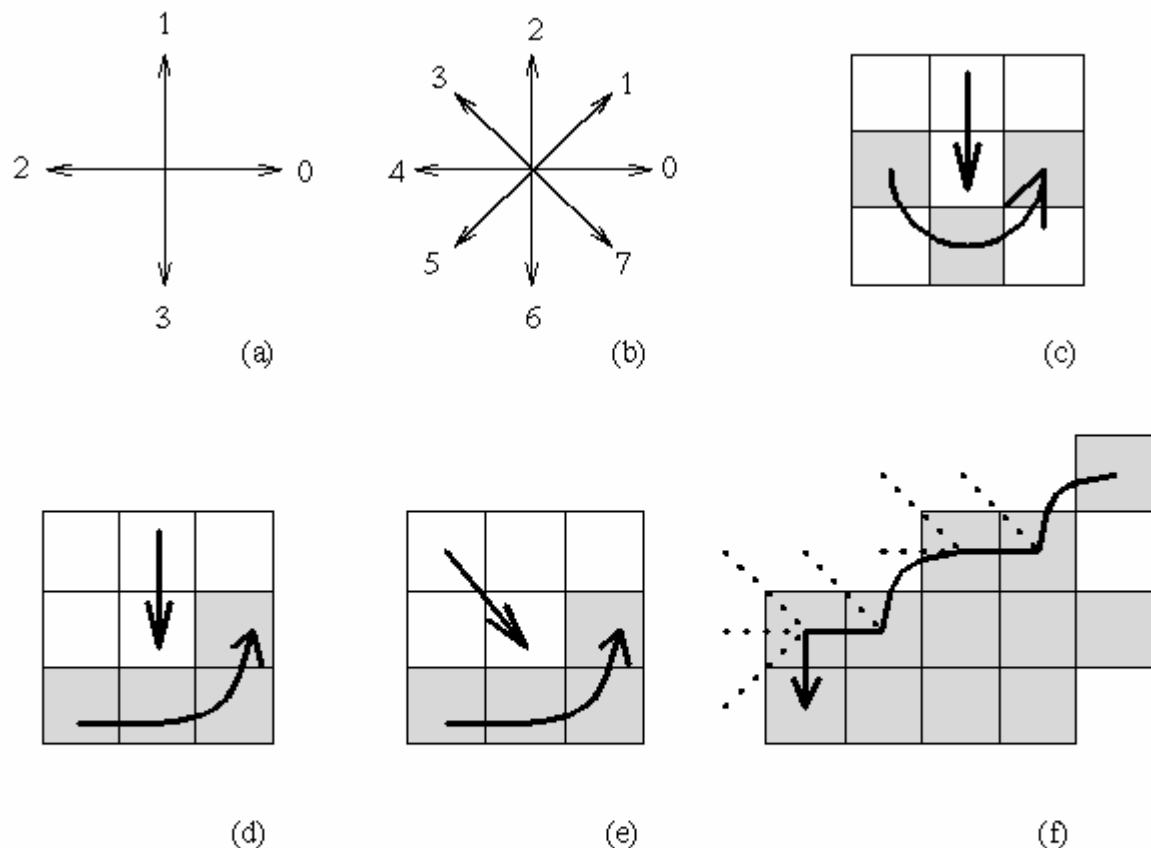
# 4 connected versus 8 connected

- 4 connected neighbors
  - 8 connected neighbors
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Algorithm 5.6: Inner boundary tracing

1. Search the image from top left until a pixel of a new region is found; this pixel  $P_0$  then has the minimum column value of all pixels of that region having the minimum row value. Pixel  $P_0$  is a starting pixel of the region border. Define a variable  $dir$  which stores the direction of the previous move along the border from the previous border element to the current border element. Assign
  - (a)  $dir = 0$  if the border is detected in 4-connectivity (Figure 5.13a)
  - (b)  $dir = 7$  if the border is detected in 8-connectivity (Figure 5.13b)
2. Search the  $3 \times 3$  neighborhood of the current pixel in an anti-clockwise direction, beginning the neighborhood search in the pixel positioned in the direction
  - (a)  $(dir + 3) \bmod 4$  (Figure 5.13c)
  - (b)  $(dir + 7) \bmod 8$  if  $dir$  is *even* (Figure 5.13d)
  - $(dir + 6) \bmod 8$  if  $dir$  is *odd* (Figure 5.13e)

The first pixel found with the same value as the current pixel is a new boundary element  $P_n$ . Update the  $dir$  value.
3. If the current boundary element  $P_n$  is equal to the second border element  $P_1$ , and if the previous border element  $P_{n-1}$  is equal to  $P_0$ , stop. Otherwise repeat step (2).
4. The detected inner border is represented by pixels  $P_0 \dots P_{n-2}$ .

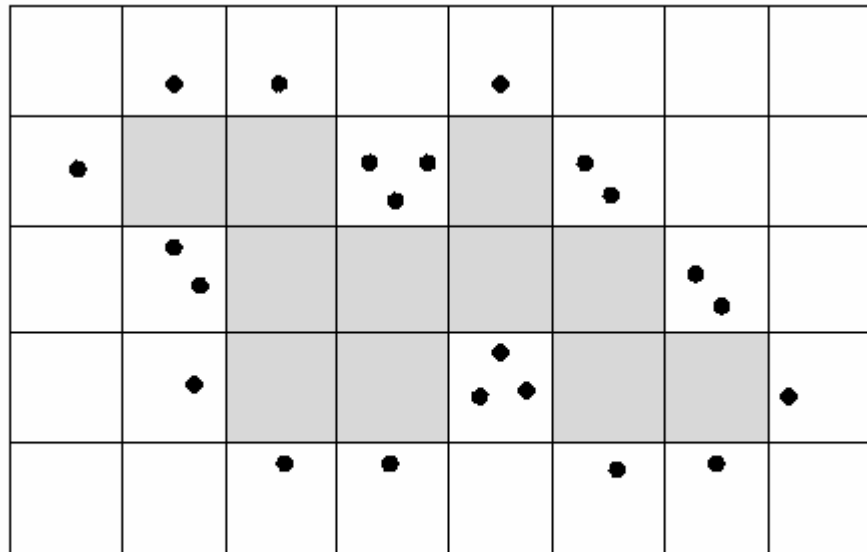


**Figure 5.13** *Inner boundary tracing: (a) Direction notation, 4-connectivity, (b) 8-connectivity, (c) pixel neighborhood search sequence in 4-connectivity, (d),(e) search sequence in 8-connectivity, (f) boundary tracing in 8-connectivity (dashed lines show pixels tested during the border tracing).*

# Outer Boundary tracing

Algorithm 5.7: Outer boundary tracing

1. Trace the inner region boundary in 4-connectivity until done.
  2. The outer boundary consists of all non-region pixels that were tested during the search process; if some pixels were tested more than once, they are listed more than once in the outer boundary list.
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**Figure 5.14** *Outer boundary tracing; • denotes outer border elements. Note that some pixels may be listed several times.*

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# Edge Linking

- Goal: take edge map, convert to a linked boundary representation
    - Can be closed or open boundary
  - Convert the edge map with gradient magnitude and gradient directions into a weighted graph
  - Use dynamic programming (based on Bellman's optimality principle) to find the shortest path from origin to destination
    - Much faster than brute force optimization
    - Idea explained in class
    - Also read pages 359-362 of AK Jain.
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# Main idea of Dynamic Programming

- Given an objective function  $S(x_1, \dots, x_N)$  where  $x_1, \dots, x_N$  are the vertices and  $S$  is the sum of edge weights when traversing in the sequence  $x_1, x_2, \dots, x_N$
  - Find  $\phi(x_N) = \max_{x_1, \dots, x_{N-1}} S(x_1, \dots, x_N)$ . The argument maximizing this gives you the path
    - $S$  can be split as:  
$$S(x_1, \dots, x_N) = S(x_1, \dots, x_{N-1}) + f(x_{N-1}, x_N)$$
  - Whenever the above holds, the max can be simplified as
$$\begin{aligned}\phi(x_N) &= \max_{x_{N-1}} [ f(x_{N-1}, x_N) + \max_{x_1, \dots, x_{N-2}} S(x_1, \dots, x_{N-1}) ] \\ &= \max_{x_{N-1}} [ f(x_{N-1}, x_N) + \phi(x_{N-1}) ]\end{aligned}$$
    - This can be implemented as a recursive algorithm
  - Details in class or in the book
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